

**Information Channels in
Labor Markets. On the Resilience
of Referral Hiring**

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Information Channels in Labor Markets. On the Resilience of Referral Hiring

Summary

Economists and sociologists disagree over markets' potential to assume functions typically performed by networks of personal connections, first among them the transmission of information. This paper begins from a model of labor markets where social ties are stronger between similar individuals and firms employing productive workers prefer to rely on personal referrals than to hire on the anonymous market (Montgomery (1991)). However, we allow workers in the market to engage in a costly action that can signal their high productivity, and ask whether the possibility of signaling reduces the reliance on the network. We find that the network is remarkably resilient. To be effective signaling must fulfill two contradictory requirements: unless the signal is extremely precise, it must be expensive or it is not informative; but it must be cheap, or the network can undercut it.

Keywords: Networks, Signaling, Referral hiring, Referral premium

JEL Classification: A14, J31, J41, D83

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1 Introduction

Personalized networks, systems of personal connections that function as privileged channels of information and trust, are part of daily experience. In situations where the reliability of information is particularly important - when applying for a job, when needing fresh capital for a new enterprise, when moving to a new country, when substituting for formal enforcement - their role becomes often crucial, either as means of entering formal markets, or indeed as substitutes for these markets. Hence the ethnic enclaves, both residential and professional, in New York City; the economic weight of the Overseas Chinese in their countries of residence; the success of Medieval networks of merchants, organized along ethnic or religious lines (the Armenians, the Italians, the Jews, the Dutch..). All of these phenomena have in common the essential role played by the personal network, with its rapidity and its freedom from the constraints of unwieldy procedures.¹

As the function of the network is recognized, an important policy question is the extent to which planned interventions or market mechanisms can substitute for personal connections. The question is important both because the networks are often very successful, and thus it would be good to be able to copy them, and because they are by their nature exclusionary, and thus tend to generate resentment and opposition among those excluded. If the networks could be replicated these delicate distributional problems could be faced.

Economists and sociologists usually disagree on the potential for artificial replication of the networks. Not surprisingly, economists tend to be more optimistic, believing that appropriate market mechanisms, encouraged and supported by appropriate policy where necessary, can substitute for the missing personal channels. Sociologists on the other hand, see the personal, non-anonymous link as the essence of the relation, the fundamental, inescapable reason not only for the truthful transmission of information, but for the “trust” that accompanies

¹See, among many others, Braudel (1982), Greif (1993), Kotkin (1992), Rauch (2001), and Redding (1990). The classic studies of personal referrals in labor markets are Rees (1966) and Granovetter (1974). A large literature focussing on labor markets has emerged since, starting with Saloner (1985), Holzer (1988), Staiger (1990), Montgomery (1991), Mortensen and Vishwanath (1994). Ioannides and Datcher Loury (2004) provides an exhaustive review.

the exchange, that trust that can never be approximated by fear of punishment (e.g. Tienda and Raijman (2001), discussing Rauch (2001)).

In this paper, we approach the issue by focusing on one channel of information transmission that seems a plausible alternative to personalized exchanges taking place in a network: the possibility of signaling. Individuals who are not part of the network can take a costly action that signals high productivity, the only relevant information in our model. The question we ask is how effective the availability of the signal is in weakening the reliance on the network. We find that the network is extremely resilient - for the great majority of our parameter space, reliance on the network continues and is profitable, even though signaling does take place in the market and typically leads to more precise information than is being revealed in the network. The reason is, *ex post* at least, obvious: when signaling is informative, it is caught in two contradictory requirements. On one hand, it must be effective in separating the different types - it must induce the more productive type to signal while the less productive type cannot profitably do so. To induce this separation, either the signal is extremely precise, or it must be costly. But at the same time, signaling is competing with reliance on the network - if signaling is costly enough to differentiate among types, then the network is likely to be profitable because it can undercut the cost of information in the market. Indeed, the savings can be enough to expand the network beyond what the acquisition of useful information would dictate, where firms prefer hiring through the network, even when that implies a more than average probability of hiring a less productive worker.

In the next section, we describe the model; in section 3 we describe the main properties of the network that will be exploited repeatedly in solving the model; section 4 characterizes the equilibria of the model, first without and then with signaling; section 5 discusses the resilience of the network and its causes; section 6 describes the main empirical predictions of the model, and section 7 concludes. The Appendix contains some of the proofs.

2 The Model

A model allowing us to study the relative performance of personal connections versus signaling must be very flexible: it must include both a network and a market, which must differ in some substantive way, and it must capture the equilibrium effects linking the two; it must allow workers and firms to choose between networking and signaling, and it must be tractable enough to allow us to study the results' sensitivity to different costs of signaling and different precisions of both mechanisms. Montgomery (1991) proposed a simple, beautiful model that satisfies all our requirements. We start from Montgomery's set-up and adapt it for our purposes.

There is a potentially infinite number of identical infinitely-lived firms and, at any period in time, two overlapping generations of workers, each composed of an equal large number of individuals. Everything we write below will apply to the limit of this number becoming very large. Each firm employs at most one worker. Workers live two periods and work in the second period of their life. In each generation, half of the workers are productive and produce one unit of output when employed (H workers), and half are unproductive and produce no output (L workers). The two types of workers cannot be distinguished ex ante, and wages cannot be made conditional on production. With some abuse of notation we will call " H firms" firms whose current employee is an H worker, and " L firms" firms whose current employee is of type L .

Young workers, who are not yet employed, can establish a connection to an older employed worker at no cost. Employed workers' types are not observable outside the firm, but following Montgomery and building on sociologists' concept of "in-breeding", we assume that a young individual will have a higher probability of establishing a link to an older worker of his own type. More precisely, each young individual will be connected to an employed worker of his own type with probability $\alpha > 1/2$, where α is common knowledge. The links are otherwise random. Personal connections can be valuable because firms have the option of hiring their new workers through referrals from their current employees, whose own productivity is known

and who, through α , are more likely than not to have connections to young workers of their own type.

If a firm chooses to hire through referrals, its employee transmits the offer to one of the young workers he is connected to (choosing randomly if he has several connections). If the young worker accepts the offer, the contract is concluded and the worker is hired for the next period. Young workers who either reject the referral offer or do not receive any, will need to find employment in the anonymous market. Before entering the market, however, each young worker has the option of engaging in a costly action that has the potential to announce publicly that he is of type H - for example a worker can attempt to be certified through an exam. The action costs λ and the probability of success is $\beta > 1/2$ if the individual is of type H , and $(1 - \beta) < 1/2$ if he is of type L . We call this option "signaling". Workers can borrow λ at no cost against their future labor earnings.² Failure of certification is not observed, and the market cannot distinguish between workers who are not certified because they never attempted certification and those who tried but failed.

Finally, the markets for certified and non certified workers open, and all young workers who have not been hired through referrals offer their labor. Firms can enter these markets freely, and expected profits from market hiring are brought down to zero. Once the new workers are hired, the old workers retire, and a new generation of young agents is born, not yet working but ready to network.

Our model differs from Montgomery's in three aspects. First, and most important, is the possibility of signaling. The availability of this additional information channel will affect the equilibrium, and we will be able to address our central question on the robustness and relative performance of personal networks when signaling is available. Second, relative to Montgomery's original model, we have reversed the direction of the personal ties: originating from the young workers and randomly connecting each of them to an older worker, rather

²More generally, λ is the amount that will need to be repaid out of future wages if a worker decides to signal. Hence it could include borrowing costs, and a decline in λ could be interpreted as, for example, more generous conditions on loans financing extra schooling.

than the opposite. The result is that each young connected worker will have exactly one link to an older worker. But because the links are random, some older workers will have several, while some will have none. The difference matters because it affects the competition among firms in making referral offers. We have chosen our modeling strategy because it allows us to move naturally to the case where networking too is costly (Casella and Hanaki, 2004), but it has the added advantage of leading to a very clean analysis where, contrary to Montgomery, we can always derive closed-form solutions. Finally, we have stream-lined the original two-period model, occasionally cumbersome, by adopting the simpler overlapping generations set-up that its logic suggests. Again, this is mostly a matter of taste, although it is also true that the possibility of referrals generates a dynamic link across periods: if having hired a H worker increases the probability of hiring another H worker next period, the value of a H worker is higher than his immediate productivity. But because this is true whether the H worker is hired in the market or through referrals, the final results are not very sensitive to this change in assumptions.³

A number of assumptions can be questioned, but plausible alternatives would not change the substance of the analysis. Because links are free, workers could be allowed to establish more than one. But the bias in the direction of the links that distinguishes the two types, summarized by α , would continue to hold and to affect the relative probability of being recommended to firms of either type. Assuming that establishing a link requires time and limiting the number of possible links to 1 thus seems a preferable modeling strategy. The older worker passes on the firm's job offer to one of his connections without reaping any surplus. This is Montgomery's original assumption and is common in the study of networks in labor markets (see, for example, Calvo-Armengol and Jackson, 2004). It is also particularly natural here, where the old worker has a purely passive role and the young worker reaps no surplus, and it simplifies the analysis because it leaves the referral wage independent of the specific number of ties that an old worker has. But dropping it would not affect the substance

³A statement we have verified by solving the two-period model with signaling.

of the model, beyond reducing the value to the firm of hiring a worker who will lead to future referrals - typically the profit attached to hiring a H worker. Assigning some of the surplus to the worker making a referral is logically very similar, in this model, to assigning some bargaining power to the new worker being hired. Because several young workers may be competing for the same referral offer, the model gives all bargaining power to the firm; in our companion paper (Casella and Hanaki, 2004) we have investigated the case where firms and workers hired through referrals share expected profits, but beyond the predictable shift in distribution the logic of the model is unchanged. A more important assumption is the inability of the young workers to direct their links exclusively to desirable - typically H - older workers. This is central to the random nature of the network, and thus to the model, but is also the source of the informational content of the personal connection, together with the “in-breeding bias.” It could be read as lack of transparency of the old worker’s type outside the firm, but can also represent, more realistically, the limited set of social interactions available to the young workers. In this model where personal links are created freely, they are best thought of as natural side-effects of daily social interaction, and the young workers’ propensity to connect with older workers of similar type should be interpreted as short - hand for some measure of social segregation.⁴ Finally, an important question is whether the present model is indeed the appropriate one for the question we want to ask. More precisely, this is a model where referrals affect distribution - distribution of profits between H firms and L firms, between incumbent firms and potential entrants, and distribution of wages between different workers - but do not affect efficiency. All workers are always employed and production always equals the total product of all H workers: there is no efficiency rationale to recommend shifting from referrals to a market-based transmission of information.⁵ On the other hand, it is not clear that real world objections to preferential networks are based

⁴For a thorough recent survey of the evidence on social segmentation and social networks and especially their role in labor markets, see Ioannides and Datcher Loury (2004).

⁵Indeed, strictly speaking, signaling is inferior to referrals because of the lost costs λ . In a full model, costs λ would be paid to an education sector; here we could assume that they are redistributed to all agents, but the step is trivial and we ignore it in what follows.

on efficiency: for the most part they are based on the belief that the network is advantageous but exclusionary, and thus plays essentially an “unfair” redistributive purpose. It is this role that is highlighted by the current model.

The solution of the model is straightforward, once the stochastic properties of the network have been characterized. We begin then by studying the network, and in particular the density of connections at each node that determines the probabilities of contacts between young and old workers of the two types.

3 The Network

Because establishing a personal connection entails no cost and does not prevent the option of signaling later, doing so is a weakly undominated strategy: if the young worker does not receive a referral offer, or if the offer is inferior to the market wage, he can access the market.⁶ Thus we will study scenarios where all young workers establish a personal connection.

As mentioned above, the stochastic nature of the connections implies that some young workers will find themselves linked to an older worker who has several other links, while some older workers will have none. Consider then the probability that a young worker of type i ($i = H, L$) will receive a referral offer if the firm employing the older worker he is connected to chooses to hire through referrals - a probability we call p_i .

With a very large number of workers and firms, the density of connections at each old worker node can be studied independently of the rest of the network. Suppose that the size of each generation of workers is $2N$, which then equals the number of active firms. Any young H worker has probability (α/N) of connecting to any specific old H worker, while the same probability equals $(1 - \alpha)/N$ for any young L worker. For large N , the number of

⁶This eliminates equilibria that seem rather trivial: where no networking takes place, because of pessimistic off-equilibrium beliefs on the part of the firms on the quality of any networking worker, or where young workers randomize over networking with just the probabilities that lead H firms to expect a referral worker to be equivalent to a market worker (thereby offering the market wage, and justifying workers’ indifference).

ties connecting any individual old worker to young workers of either type is described by a Poisson distribution: the probability that an old H worker has x ties to young H workers, for example, is given by $\frac{\alpha^x}{x!}e^{-\alpha}$. It follows that the probability that the old H worker i is connected to has k additional connections, a probability we denote by $\gamma_{k,H}$, can be written as:

$$\gamma_{k,H} = \sum_{j=0}^k \left[\frac{\alpha^{k-j}}{(k-j)!} e^{-\alpha} \frac{(1-\alpha)^j}{j!} e^{-(1-\alpha)} \right] = \sum_{j=0}^k \left[e^{-1} \frac{\alpha^{k-j}(1-\alpha)^j}{(k-j)!j!} \right] = \frac{e^{-1}}{k!} \quad (1)$$

where we have used:⁷

$$\frac{1}{k!} = \sum_{j=0}^k \frac{\alpha^{(k-j)}(1-\alpha)^j}{j!(k-j)!}$$

Therefore:

$$\begin{aligned} p_H &= \lim_{N \rightarrow \infty} \left[1 - \left(\frac{2N-1}{2N} \gamma_{2N-1,H} + \frac{2N-2}{2N-1} \gamma_{2N-2,H} + \dots + \frac{1}{2} \gamma_{1,H} \right) \right] = \\ &= \lim_{N \rightarrow \infty} \left(1 - \sum_{k=1}^{2N-1} \frac{k}{k+1} \gamma_{k,H} \right) = 1 - e^{-1} \left[\lim_{N \rightarrow \infty} \left(\sum_{k=1}^{2N-1} \frac{k}{(k+1)!} \right) \right] \end{aligned}$$

or:

$$p_H = 1 - e^{-1} \quad (2)$$

The details of the derivation are in the Appendix (where in particular we show that the error introduced by evaluating the expressions in the limit, as N approaches infinity, is negligible). As intuition suggests, if all young workers network the probability of receiving a referral, conditional on the firm using referrals, is independent of the parameter α : the value of α affects the composition of the pool of other young workers with which i must compete for a referral, but not their expected number. Thus it is also the case that $p_H = p_L$, and in what follows we will identify both terms by $p \equiv 1 - e^{-1}$. But recall once again that these probabilities are conditional on the firms using referrals and that H and L young workers will expect to be connected to firms of different types, generally making different decisions

⁷Since: $\sum_{j=0}^k \binom{k}{j} \alpha^{(k-j)}(1-\alpha)^j = \sum_{j=0}^k \frac{k!}{j!(k-j)!} \alpha^{(k-j)}(1-\alpha)^j = 1$

about their reliance on referrals. The characterization of the equilibria of the model, below, will make this observation precise.

The stochastic nature of the network determines two further probabilities that will be exploited repeatedly. It is convenient to derive them here. We just observed that some old workers will have no ties to any young worker. Thus, from the point of view of the firm, what is the probability that their current employee of type i is able to recommend at least one worker for possible hiring? In other words, what is the probability that the firm's current employee has at least one connection? Call such a probability ϕ_i where i is the current employee's type. An old H worker is linked to a young H with probability α/N (since there are N old H workers). Thus the probability that he has no connection to any young H is given by $(1 - \alpha/N)^N$, the exponent now reflecting the fact that there are N young H workers. The probability that he has no connection to either a young H or a young L is then $(1 - \alpha/N)^N [1 - (1 - \alpha)/N]^N$ and thus ϕ_H , the probability that he has at least one connection, can be approximated by:

$$\phi_H = \lim_{N \rightarrow \infty} [1 - (1 - \frac{\alpha}{N})^N (1 - \frac{1 - \alpha}{N})^N] = 1 - e^{-1} \quad (3)$$

Similarly $\phi_L = 1 - e^{-1}$ and again we will identify both ϕ_H and ϕ_L by $\phi \equiv 1 - e^{-1}$.⁸

Finally, conditional on having at least one connection, what is the probability that an old H worker making a random referral will choose a young worker of type H ? Suppose that the old H worker has k connections, and call such a probability ζ_{HH}^k . Recall that the probability of having k connections can be approximated by γ_{kH} in equation (1). Hence, for

⁸Notice that there is no reason why p and ϕ should be equal in general, and indeed they would differ if the either group of workers did not network with probability 1. (See Casella and Hanaki, 2004).

very large N , we can write:

$$\begin{aligned}\zeta_{HH}^k &= \left(\frac{1}{\gamma_{kH}}\right) \sum_{j=0}^k \left[\binom{k-j}{k} \frac{\alpha^{k-j}}{(k-j)!} e^{-\alpha} \frac{(1-\alpha)^j}{j!} e^{-(1-\alpha)} \right] \\ &= \sum_{j=0}^k \left[\binom{k-j}{k} \frac{\alpha^{k-j}}{(k-j)!} \frac{(1-\alpha)^j}{j!} \right] k!\end{aligned}$$

Using:

$$\sum_{j=0}^k \left[(k-j) \frac{\alpha^{k-j}}{(k-j)!} \frac{(1-\alpha)^j}{j!} \right] = \frac{\alpha}{(k-1)!}$$

the expression simplifies to:

$$\zeta_{HH}^k = \left(\frac{\alpha}{k(k-1)!} \right) k! = \alpha \quad \forall k \quad (4)$$

If we define ζ_{ij}^k as the probability that an old worker of type i having k connections and making a random referral will choose a young worker of type j , the same procedure allows us to derive immediately that $\zeta_{HH}^k = \zeta_{LL}^k = \alpha$, and $\zeta_{HL}^k = \zeta_{LH}^k = 1 - \alpha$ for all k .

It is the simple characterization of these probabilities that makes the model easy to solve. The network, random but with a bias, combines the tractability of purely random networks with the substantive concerns raised by in-breeding and selectivity.⁹

4 The Equilibria of the Model

Given our focus on equilibria where all workers establish personal connections, the only decision workers have to take is whether to attempt certification if they are not hired through referrals. The firms, on the other hand, have to decide whether or not to attempt to hire through referrals of their current employee, and if so, what wage to offer. Each worker i 's

⁹An interesting related literature studies the economic implications of different network architectures, and thus different paths for the transmission of information. Calvo-Armengol and Jackson (2004) and Tassier and Menczer (2004) are examples focused on labor markets.

strategy is the probability with which he chooses to signal, s_i , while each firm j 's strategy is the probability with which the firm chooses to hire through referrals (conditional on its current employee being connected to at least one young worker) r_j and the referral wage w_{rj} . We focus on symmetrical equilibria where all workers of the same type and all firms employing the same type of workers follow the same strategy. In addition, given the stationarity of our set-up, we restrict attention to stationary strategies that remain unchanged over time.¹⁰ If we use the terminology " $\forall i \in H$ " to indicate all workers of type H , and " $\forall j \in H$ " to indicate all firms employing workers of type H (and similarly for L), then: $s_{Hi} = s_H \forall i \in H$, $s_{Li} = s_L \forall i \in L$, $r_{Hj} = r_H$ and $w_{rHj} = w_{rH} \forall j \in H$, $r_{Lj} = r_L$ and $w_{rLj} = w_{rL} \forall j \in L$. We neglect the time subscript to emphasize that these strategies hold for all times. Call w_C and w_U the wage for certified and uncertified workers in the anonymous market. An equilibrium is a set of strategies $\{\sigma_H, \sigma_L, r_H, r_L, w_{rH}, w_{rL}\}$, a pair of market clearing wages $\{w_C, w_U\}$ and a set of beliefs about the workers' types such that no worker and no firm can strictly gain from choosing a strategy different from that assigned to his or its type, the labor market clears, and all beliefs are rational.

Consider a scenario where firms extend referral offers with probabilities r_H and r_L , and workers who have not been hired through referrals attempt certification with probabilities s_H and s_L . We can describe equilibrium wages and firms' profits for generic values of these probabilities. Given wages and profits, different hiring strategies for firms and signaling strategies for workers can be posited, and the appropriate incentive compatibility constraints identify the range of parameter values for which each equilibrium exists.

Examine the problem first from the perspective of the firms. The worker they hire in any given period is valuable both because of his own productivity and because of his ties to younger workers in the future which will enable the firm to hire through referrals, if advantageous. Call V_H the value of hiring a H worker, and Π_H the firm's expected profits

¹⁰Each worker decides whether or not to signal only once, in the second and last period of their life. Firms on the other hand are infinitely-lived and must decide whether or not to hire through referrals every period. By restricting attention to stationary strategies, we reduce the set of strategies for a firm of each type to a single probability, ignoring time.

from referrals from a current H employee (and similarly for V_L and Π_L). Then:

$$V_H = 1 + \max\{0, \delta\Pi_H\} \tag{5}$$

$$V_L = \max\{0, \delta\Pi_L\}$$

where δ is the rate with which expected profits in the next hiring cycle are discounted. Keeping in mind that profits from hiring in the market must be zero, expected profits from referrals must equal the probability of hiring a worker whose value, combining productivity and future referrals, is larger than the referrals wage. If we call h_{LH} the probability of hiring a L worker through referrals from a current H employee (and similarly for the other types), then expected profits from referrals are:

$$\Pi_H = h_{HH}(V_H - w_{rH}) + h_{LH}(V_L - w_{rH}) \tag{6}$$

$$\Pi_L = h_{HL}(V_H - w_{rL}) + h_{LL}(V_L - w_{rL})$$

where the results of the previous section imply:

$$h_{HH} = h_{LL} = \alpha\phi = \alpha(1 - e^{-1}) \tag{7}$$

$$h_{LH} = h_{HL} = (1 - \alpha)\phi = (1 - \alpha)(1 - e^{-1})$$

Any firm which attempts to hire through referrals offers a wage that must be weakly smaller than the expected value of the referral. The wage must be acceptable to a H worker; indeed, because our model gives firms all bargaining power, it must be the lowest wage

acceptable to a H worker and it must be identical for H and L firms: $w_{rH} = w_{rL} \equiv w_r$.¹¹ When some of the workers attempt certification, two different markets exist, a market for certified workers which clears at wage w_C , and a market for uncertified workers, which clears at wage w_U . The extent to which the referral wage reflects the wage for uncertified or certified workers (net of certification costs) depends on the strategy followed by H workers left in the market. Since a H worker attempting certification is successful with probability β , the lowest referral wage he would accept must be:

$$w_r = \begin{cases} \beta w_c + (1 - \beta)w_U - \lambda & \text{if } s_H = 1 \\ w_U & \text{otherwise} \end{cases} \quad (8)$$

The market wages reflect the probabilities and the values of hiring workers of either type. Defining h_{HU} as the probability of hiring a H worker in the market for uncertified workers (and similarly h_{LU}), and h_{HC} and h_{LC} as the corresponding probabilities in the market for certified workers, and keeping in mind that expected profits when hiring in the market are zero:

$$w_U = h_{HU}V_H + h_{LU}V_L = h_{HU}V_H + (1 - h_{HU})V_L = h_{HU}(V_H - V_L) + V_L$$

$$w_C = h_{HC}V_H + h_{LC}V_L = h_{HC}V_H + (1 - h_{HC})V_L = h_{HC}(V_H - V_L) + V_L$$

These probabilities are given by the relative frequencies of workers of either type. For example, if we define $prob(C|H)$ ($prob(C|L)$) as the probability of being in the market for certified workers conditional on being a H type (a L type), then:

¹¹Even when L firms choose to use referrals, and thus $V_L > 0$, they must be driven by the goal of hiring a H worker since L workers are not productive. If workers shared in the surplus generated by referral hiring, the wage offered by H and L firms would both be higher than the minimum acceptable wage for a H worker but they would differ, reflecting the different probabilities of hiring H workers and thus the different expected surplus.

$$h_{HC} = \frac{\text{prob}(C|H)\text{prob}(H)}{\text{prob}(C|H)\text{prob}(H) + \text{prob}(C|L)\text{prob}(L)}$$

Note that $\text{prob}(C|H)$ is the joint probability of not having been hired through referrals and being certified, conditional on being a H worker (and correspondingly for $\text{prob}(C|L)$). Thus:

$$\begin{aligned}\text{prob}(C|H) &= [1 - r_H\alpha p - r_L(1 - \alpha)p](s_H\beta) \\ \text{prob}(C|L) &= [1 - r_H(1 - \alpha)p - r_L\alpha p]s_L(1 - \beta)\end{aligned}$$

Therefore:

$$w_C = \frac{[1 - r_H\alpha p - r_L(1 - \alpha)p](s_H\beta)(V_H - V_L)}{[1 - r_H\alpha p - r_L(1 - \alpha)p](s_H\beta) + [1 - r_H(1 - \alpha)p - r_L\alpha p]s_L(1 - \beta)} + V_L \quad (9)$$

Similarly:

$$h_{HU} = \frac{\text{prob}(U|H)\text{prob}(H)}{\text{prob}(U|H)\text{prob}(H) + \text{prob}(U|L)\text{prob}(L)}$$

and:

$$\begin{aligned}\text{prob}(U|H) &= [1 - r_H\alpha p - r_L(1 - \alpha)p](1 - s_H\beta) \\ \text{prob}(U|L) &= [1 - r_H(1 - \alpha)p - r_L\alpha p][1 - s_L(1 - \beta)]\end{aligned}$$

Therefore:

$$w_U = \frac{[1 - r_H\alpha p - r_L(1 - \alpha)p](1 - s_H\beta)(V_H - V_L)}{[1 - r_H\alpha p - r_L(1 - \alpha)p](1 - s_H\beta) + [1 - r_H(1 - \alpha)p - r_L\alpha p][1 - s_L(1 - \beta)]} + V_L \quad (10)$$

(Recall that, by equation (2), $p = (1 - e^{-1})$).

We can now write the incentive compatibility constraints for firms and workers. Firms

will use referrals only if it profitable to do so, or, taking (6) and (7) into account:

$$r_H > 0 \Leftrightarrow \Pi_H = (1 - e^{-1})[\alpha V_H + (1 - \alpha)V_L - w_r] \geq 0 \tag{11}$$

$$r_L > 0 \Leftrightarrow \Pi_L = (1 - e^{-1})[(1 - \alpha)V_H + \alpha V_L - w_r] \geq 0$$

Workers attempt certification if the cost of doing so is compensated by the difference in the wages, or, given the different probabilities of success for H and L workers:

$$s_H > 0 \Leftrightarrow \beta w_C + (1 - \beta)w_U - \lambda \geq w_U \tag{12}$$

$$s_L > 0 \Leftrightarrow (1 - \beta)w_C + \beta w_U - \lambda \geq w_U$$

The characterization of the economy is complete: the three different wages are given by (8), (9) and (10); the firms' profits from referrals by equations (6); the value to the firm of hiring a worker of either type by (5) and finally the incentive compatibility constraints by (11) and (12). If all incentive compatibility constraints hold with strict inequality, the equilibrium is in pure strategies, and the probabilities $\{r_H, r_L, s_H, s_L\}$ assume only 0 or 1 values; otherwise mixed strategies are possible.

As described earlier, once a candidate set of equilibrium strategies is posited, the incentive compatibility constraints, evaluated at the correct wages, identify the range of parameter values for which the strategies are indeed an equilibrium, if one such range exists. Different equilibria can exist for different parameter values, or indeed multiple equilibria can occur over the same range of parameters. The number of candidate equilibrium regimes is large,¹² but some combinations of strategies can be ruled out ex ante. We can state:

¹²Without imposing any constraint, there are 3^4 combinations of candidate equilibrium strategies. Of these, 2^4 correspond to pure strategy equilibria and the remainder have at least one set of agents randomizing.

Lemma 1. (i) If $s_H = s_L = 0$, then $r_H = 1$ and $r_L = 0$; (ii) If $r_L > 0$, then $r_H = 1$; (iii) If $s_L > 0$, then $s_H = 1$; (iv) if $s_H \in (0, 1)$, then $r_H = 1$.

The lemma is proved in the Appendix, but the logic behind the four observations is not difficult to see. The first point states that in the absence of signaling H firms strictly benefit from hiring through referrals, while L firms do not. The reason is that, absent signaling, H firms have a higher probability of hiring a productive worker through referrals than in the market, while the opposite is true for L firms.¹³ The second point follows immediately from the fact that it is always better to hire a H worker than a L worker: since the probability of doing so through referrals is always higher for H firms, the incentive to use referrals must always be strictly higher for H firms. Similarly, if any worker incurs the positive costs of attempting certification, the market wage for certified workers must always be strictly higher than the wage for uncertified workers, and since the probability of success, upon attempting certification, is always higher for H workers, the incentive to signal must be strictly higher for H workers. Finally, we know from (i) that H firms always rely on referrals in the absence of signaling. If $s_H \in (0, 1)$, then $s_L = 0$ (by (iii)), and firms can offer as referral wage the market wage for uncertified workers. Because some H workers, and only some H workers, exit the uncertified workers pool, the referral wage is lower than in the case of no signaling, while the expected productivity of a referral hire for H firms remains constant at α . If referrals were profitable in the absence of signaling, they must be profitable when $s_H \in (0, 1)$.

It is possible to analyze systematically each candidate equilibrium and the range of parameter values that support it, but given the equations derived above the procedure is mechanical and rather tedious. We limit ourselves to two examples.

¹³The hiring decisions of H firms are strategic complements. Given that other H firms hire through referrals, and L firms do not, $h_{HU} < 1/2 < \alpha$. Thus a H firm benefits from using referrals. For L firms, it is not difficult to verify that in this scenario $h_{LU} > (1 - \alpha)$ (see the Appendix). Thus it is preferable to hire in the market.

4.1 Example 1. Equilibrium with referrals and no signaling.

The workers' choice not to signal can be supported in equilibrium for all parameter values: given $\lambda > 0$, off-equilibrium beliefs on the part of the firms according to which anybody deviating must be an L type are sufficient to induce rational workers not to signal, independently of their type. Lemma 1 states that in such a scenario if an equilibrium exists it must be such that H firms use referrals while L firms do not. The question then is the identification of the range of parameter values for which these latter strategies are an equilibrium. We can state:

Lemma 2. *For all $\alpha > 1/2$, $\lambda > 0$, and $\delta \in [0, 1]$, there exists an equilibrium where $s_H = s_L = 0$, $r_H = 1$ and $r_L = 0$.*

Proof. In principle, a firm can envision any deviating path, extending into the future: a once-for-all deviation where the firm takes as given its own future strategy, a permanent deviation where the firm envisions changing its strategy forever, or indeed any repeated deviation over any subset of future periods, and this for either of the firm's future types. In our stationary environment, however - where all other agents repeat the same strategy and a single deviating firm is negligible - the gain from repeated deviations is only the appropriately discounted sum of the gain from a once-for-all deviation. Ruling out the latter is thus sufficient to rule out any other pattern of deviation.¹⁴

Consider first the scope for deviation by a H firm - the gain from foregoing referrals. The firm will deviate if current expected profits from referrals are negative, taking as given its future strategy. Along the candidate equilibrium path $V_L = 0$ and the individual firm's deviation has no effect on the market wage, and thus on the referral wage. Deviation is profitable if $\Pi_H = (1 - e^{-1})(\alpha V_H - w_r) < 0$, or substituting $s_H = s_L = r_L = 0$, $r_H = 1$ and

¹⁴Although the intuition seems clear, the question arises because a firm's profits from deviation depend on the firm's own future expected strategies - the value of making referrals, which affect today's profit from referrals, depends on the firm's future strategies. This leads to questioning whether a permanent deviation, for example, could be more advantageous than a once-for-all deviation. It is possible to show, however, that this can occur only if the permanent deviation per se is not profitable. Since in addition deviation for a fixed number of periods implies a once-for-all deviation at the end of the planned horizon, the conclusion in the text holds: ruling out once-for-all deviations is sufficient to rule out any other pattern of deviation.

$p = 1 - e^{-1}$ in (10), if:

$$(1 - e^{-1}) \left(\alpha - \frac{e - \alpha(e - 1)}{e + 1} \right) V_H < 0$$

But $V_H \geq 1$ and the second parenthesis is positive for all $\alpha > 1/2$. Deviation cannot be profitable.

Consider now the gain from deviation for a L firm - the gain from switching to using referrals. Again, given $V_L = 0$ along the candidate equilibrium path, deviation is profitable if:

$$(1 - e^{-1}) \left((1 - \alpha) - \frac{e - \alpha(e - 1)}{e + 1} \right) V_H > 0$$

a condition that is violated for all $\alpha > 1/2$. Deviation by either type of firm is then ruled out. \square

This is the equilibrium discussed by Montgomery in his original paper. In the absence of signaling, it is the unique equilibrium of the model (as implied by Lemma 1): H firms always attempt to hire through referrals and L firms never do. Expected profits are zero for L firms, who hire on the open market, but are positive for H firms and equal to the expected profits from referral hiring. From equation (6):

$$\Pi_H = \frac{(e - 1)(2\alpha - 1)}{(1 + e) - \delta(e - 1)(2\alpha - 1)}$$

The value of hiring a H worker is given by:

$$V_H = \frac{1 + e}{(1 + e) - \delta(e - 1)(2\alpha - 1)}$$

and the wage by:

$$w_U = w_r = \frac{e - \alpha(e - 1)}{(1 + e) - \delta(e - 1)(2\alpha - 1)}$$

As expected, the value of a H worker is higher than his personal productivity ($V_H > 1$) for all $\alpha > 1/2$ because employing a H worker leads to a higher than random chance of hiring a H worker in the following period. This effect is more important the higher is α - the higher the probability that connected agents are of the same type - and the higher is δ - the less the future is discounted. The profit from referral hiring accrues entirely to the firm and is given by Π_H , an expression increasing in α and δ , like V_H and for the same reasons. The wage, on the other hand, is declining in α : it would equal $1/2$ if α equalled $1/2$ because referral hiring by H firms would then not affect the average productivity of the market pool, but its value falls monotonically at higher α values reflecting the increased selection of young H workers out of the market. Because the wage reflects not only the probability but also the value of hiring a H worker in the market, it is increasing in δ - it is higher the less the future is discounted. Note that the expected wage is identical for H and L workers, a consequence of our granting all bargaining power to the firm when hiring through referrals and a conclusion that would be easily reversed in favor of a referral premium if referred workers shared in the surplus.¹⁵ With the only noticeable difference that the direction of the network links we have posited strengthens the bargaining position of the firms, this equilibrium essentially replicates Montgomery's results.

4.2 Example 2. Equilibrium with signaling and no referrals.

Can signaling support an equilibrium where referrals are not advantageous? Lemma 3 provides the answer:

Lemma 3. *For all $\alpha > 1/2$, $\delta \in [0, 1]$, there exists an equilibrium where $s_H = 1$, $s_L = 0$, $r_H = 0$ and $r_L = 0$ if $\beta \geq 2\alpha/(1 + \alpha)$ and $(1 - \beta)/(2 - \beta) \leq \lambda \leq \beta/(2 - \beta)$.*

In this scenario, all certified workers must necessarily be H types and firms can, if they

¹⁵If workers hired through referrals had more bargaining power than our model grants them, equilibrium strategies would be unchanged but their own wage would be higher than the market wage. The market wage would be lower, reflecting the lower value to the firm of hiring a H worker, but would again depend negatively on α .

so choose, guarantee themselves a new H worker.¹⁶ To verify that it is an equilibrium, notice first that since no profits are available to firms through referral hirings, $V_H = 1$ and $V_L = 0$. The wages for certified and uncertified workers are given by (9) and (10) above: because all certified workers are of type H , their value is fully reflected in the market wage, $w_C = 1$, while $w_U = (1 - \beta)/(2 - \beta)$. The incentive compatibility constraints for the workers (12) impose a first set of constraints on parameters:

$$s_H = 1 \Rightarrow \frac{\beta}{2 - \beta} \geq \lambda \tag{13}$$

$$s_L = 0 \Rightarrow \frac{1 - \beta}{2 - \beta} \leq \lambda$$

With $\beta > 1/2$, there is a non-empty range of λ values for which the two constraints can both be satisfied.

Consider the potential for deviation by the firms. Any firm willing to hire through referrals would need to offer a wage acceptable to H workers, who prefer to attempt certification. Hence, from (8), $w_r = \beta + (1 - \beta)^2/(2 - \beta) - \lambda$. Because the incentive to use referrals is always larger for H firms (see Lemma 1), ruling out deviation by a H firm is sufficient to rule out deviation by a L firm. As earlier, it is sufficient to focus on once-for-all deviations. A H firm will switch to using referrals if $\Pi_H = (1 - e^{-1})[\alpha - w_r] > 0$. Thus equilibrium requires:

$$r_H = 0 \Rightarrow \lambda \leq \beta + \frac{(1 - \beta)^2}{2 - \beta} - \alpha = \frac{1 - 2\alpha + \beta\alpha}{2 - \beta} \tag{14}$$

Because (13) and (14) must both be satisfied, this equilibrium exists if $(1 - \beta) \leq (1 - 2\alpha + \beta\alpha)$, or $\beta \geq 2\alpha/(1 + \alpha)$. \square

For a suitable range of parameter values, the candidate equilibrium indeed exists: signal-

¹⁶The only other candidate equilibrium where all certified workers are guaranteed to be of H type has strategies $s_H \in (0, 1)$ and $s_L = 0$. But then we know by Lemma 1 that $r_H = 1$: if an equilibrium exists, referrals must take place.

ing provides separation of the workers' types, in the limited sense that all certified workers must be of type H , and firms refrain from using referrals and prefer to hire in the market, an option they would not take in the absence of signaling. Signaling provides information and supplants the use of personal referrals. Notice that hiring in either market, for certified or uncertified workers, leads to zero firm profits, and thus firms are indifferent between paying the premium attached to certification, and guaranteeing themselves a H worker, or hiring a cheaper uncertified worker with a lower but positive probability of being a H type. But hiring an uncertified worker in this equilibrium is not equivalent to hiring an uncertified worker when no signaling takes place: the more precise information reflected in the wage makes this option superior to referrals in this equilibrium but inferior when no signaling takes place.

Notice however that the range of parameter values for which the equilibrium exists is surprisingly limited. Since $\alpha > 1/2$, β cannot be smaller than $2/3$, and λ must fall in a correspondingly narrow interval. Interestingly, the tight range of acceptable parameter values is mostly dictated by the incentive compatibility constraints ensuring that firms refrain from making referrals. In their absence, all values of $\beta > 1/2$ could sustain the equilibrium (although the acceptable values of λ would remain quite limited). This suggests two conjectures: first it seems likely that other equilibria exist, for ranges of parameter values that may differ from or overlap the range identified here, where signaling provides separation between the workers' types but firms still choose to make referral offers.¹⁷ Second, notice that the firms' incentive compatibility constraints select values of λ close to the lower bound of the interval satisfying the workers' incentive constraints. A higher λ would induce firms to deviate. This is an interesting point, beginning to suggest the resilience of referrals in our model: when β is not very high, signaling can be informative only if λ is high enough to induce separation of workers' types. But if λ is high, signaling is informative but also expensive: referral hiring can undercut it and be less precise but preferable. We make this

¹⁷The existence of such equilibria does not follow immediately from a violation of the firms' incentive compatibility constraints in the candidate equilibrium studied. The composition of the markets, the wages and thus all constraints would reflect the different firms' strategies.

conjecture more precise in the next section.

5 Reliance on Personal Connections when Signaling is Informative.

Having verified that signaling can come to eliminate the recourse to personal referrals, we now focus on the opposite question. Under what conditions is the availability of a signaling mechanism compatible with continued reliance on referrals? And if reliance on referrals continues to exist, does signaling affect referrals indirectly, by influencing the quality of referral hiring, i.e. the percentage of referrals falling on workers of different type?

Some scenarios are trivial: if the cost of signaling λ is very low, and the probability of success β not very different across types (β close to $1/2$), then all workers may choose to signal, but certification is uninformative and H firms continue to prefer hiring through referrals (and the more so the higher is α). The question becomes interesting if we restrict attention to equilibria where signaling is informative, where we use the strict criterion that only H workers attempt to signal ($s_H > 0$, $s_L = 0$) because in these equilibria signaling is informationally superior to referrals.

The first result is summarized in the following proposition:

Proposition 1. *For all $\alpha \in (1/2, 1)$, there exist equilibria where signaling is perfectly informative and firms strictly prefer to hire through referrals.*

The proof, in the Appendix, amounts to showing the existence of one such equilibrium. In particular, we focus on the case $\beta = \alpha$ and on strategies $\{s_H = 1, s_L = 0, r_H = 1, r_L = 1\}$ - H workers in the market prefer to signal, L workers do not, and all firms prefer to hire through referrals - and show that for all $\alpha \in (1/2, 1)$ there exists a non-empty range of λ values for which such strategies are indeed equilibrium strategies. The case $\beta = \alpha$ is chosen primarily because it simplifies the algebra and the presentation of the results, but is also a natural reference point: the exogenous precision of the personal connections equals the exogenous precision of the signal. The assumption does not imply that personal connections

and signaling are constrained to be equally informative because the signaling mechanism has one additional element, the cost λ , which leads to self-selection in the decision to engage in signaling - hence the possibility that signaling be perfectly informative even for β very close to $1/2$, as in the equilibrium described here. Because we are evaluating equilibria over the whole range of possible λ value, the restriction $\beta = \alpha$ is compatible with a large number of scenarios, while leaving the model ex ante unbiased. We will use it repeatedly as our reference case.

Although the proof selects one particular example, in fact there are several equilibrium regimes where signaling is informative and firms prefer to use referrals - equilibria where only H firms use referrals, or where a share of them do so while L firms hire in the market, or where all H firms and a share of L use referrals, or equilibria where only a share of H workers signal, while L workers do not. The range of parameter values for which referral hiring takes place and is imprecise, while firms could guarantee themselves H workers is far from limited or special. Figure 1 shows equilibrium strategies in $\lambda - \alpha$ space in the case $\beta = \alpha$ and $\delta = 0.90$. The model is obviously very stylized, but we can read parameter values keeping in mind that the unit of time is the hiring cycle, or more precisely the length of employment of a worker at a single firm. The difference in productivity between a productive and unproductive worker over that cycle is normalized to 1. Thus if we think of the time horizon as about five years, $\delta = 0.90$ corresponds to a yearly discount rate of 2 percent.¹⁸ The parameter λ , the fixed cost of certification, can be thought of as the cost of further education, for example college, and should be read relative to 1: $\lambda = 1$ in our model represents the case where the cost of college education equals the total difference in productivity between a productive and a non-productive worker over five years. As we saw, in the presence of referrals the value of a worker to the firm includes the value of future referral hiring, and thus the premium that firms may be willing to pay to college educated workers may be well above the one-cycle difference in productivity, implying in turn that acceptable values of λ in our model may

¹⁸Our qualitative results are effectively insensitive to the specific value we assign to δ , for all $\delta \in [0, 1]$.

well be above 1.

Figure 1a depicts workers' strategies, and figure 1b firms' strategies. As mentioned earlier, there is always an equilibrium without signaling, supported by firms' negative off-equilibrium beliefs. In Figure 1a, we have allowed signaling to take place whenever it can be supported in equilibrium, with rational beliefs.¹⁹

The figures show that there is a large area of the parameter space for which signaling takes place and is fully informative. Workers signal when the cost λ is not too large; if the precision of the signal (β , which in the figure equals α) is high, only H workers signal, and they do so for a large range of λ values; if on the contrary β is low, then signaling can occur only if λ is low, and for most of these values signaling is not informative because the incentives to signal are very similar for H and L workers.²⁰ Unless β is high, informative signaling requires intermediate values for λ , low enough to be affordable by H workers, but high enough to discourage L workers. As for referrals, the immediate observation from Figure 1b is that there is no equilibrium where firms do not use referrals: over the entire parameters range, referrals never cease to be profitable for firms, whether signaling is informative or not, whether λ is high or low, whether α and β are high or low. The figure relies on $\alpha = \beta$, and thus, as made clear by the equilibrium with no referrals characterized in the previous section, the result is not general. But given our emphasis on the $\alpha = \beta$ case as plausible unbiased reference, we emphasize this conclusion in a separate proposition, proved in the Appendix:

Proposition 2. *Suppose $\alpha = \beta$. Then there exist equilibria where signaling is perfectly informative, but there are no equilibria where referrals are not used.*

Upon a moment of reflection, the reason is obvious: unless β is high, when signaling is informative it is also rather expensive (λ is high), expensive enough to allow H workers to

¹⁹No signaling is the unique equilibrium in the area left white: a worker of either type would not want to attempt certification even if firms, off-equilibrium, expected any certified worker to be of type H . A second equilibrium, with $s_H \in (0, 1)$ and $s_L = 0$, exists in the region bordering the upward sloping frontier between the white and gray areas in Figure 1a. The figure omits it for ease of reading.

²⁰When β is close to $1/2$, the probability of success upon signaling are very similar for H and L workers, but the wage premium for certified workers is small. At high β , the premium is high but the probability of success for a L worker is low. The incentive to signal for L workers is maximal for intermediate values of β .

differentiate themselves. Market wages for certified workers compensate them for the cost of certification, and thus tend to be high. Firms may well prefer the less informative but cheaper reliance on referrals. In the trade-off between information and cost, cost becomes the deciding factor. The conclusion always holds when $\alpha = \beta$ because informative signaling can be cheap only when its precision is high, but if the precision of referral hirings is also correspondingly high, then the cost advantage, small as it may be, remains the dominant consideration.

The firms' equilibrium strategies are particularly interesting when β (and α) are low. There is then a range of parameter values where, if signaling occurs in equilibrium, *all* firms hire through referrals (the black area in figure 1b), including L firms, which never use referrals in the absence of signaling because referrals give them a more than even chance of hiring an unproductive worker. As stated in the following proposition (proved in the Appendix):

Proposition 3. *Signaling, including informative signaling, may induce L firms to hire through referrals.*

Once again, the reason is the market premium for certified workers. Indeed, Figure 1b makes clear that such an equilibrium occurs when, for each α and β , λ approaches its highest acceptable value. Because certified workers must be compensated for the cost of signaling, the areas where L firms use referrals correspond to those ranges of parameter values where the certification premium is highest. When $\alpha = \beta$, L firms' incentive to use referrals is maximal when α is close to $1/2$: the bias inherent in referral hiring is not too strong, while referrals allow firms to avoid the premium for certified workers and still hire workers of higher average productivity than in the uncertified market.

What is remarkable about this equilibrium is that the existence of signaling, and in particular of informative signaling, leads to an *increase* in firms' reliance on referrals. In fact, if $\alpha = \beta$ signaling always weakly increases the expected proportion of workers hired through referrals: either referral hiring is used by H firms alone, as in the absence of signaling, or it is used by both H firms and some positive share of L firms (possibly all).

This observation allows us to address a question we raised at the beginning of this section: how does signaling affect the quality of referral hiring? The answer is an immediate corollary to Proposition 3:

Corollary to Proposition 3. *Signaling always weakly lowers the quality of referral hirings.*

Since only H firms recur to referrals in the absence of signaling, any expansion of referral hiring to L firms necessarily lowers the average productivity of workers hired through referrals. Paradoxically then, signaling not only does not eliminate referrals, but in fact may lead to increased reliance on personal connections, and lower expected productivity of referral hires.

We have phrased our discussion mostly in terms of the $\alpha = \beta$ case, but the results generalize predictably when we loosen this constraint. To generate transparent figures, we can specialize the model in a different direction. Figure 2 describes equilibrium strategies for workers (figure 2a) and firms (figure 2b) for arbitrary values of β and λ when we fix α at 0.75 (and δ at 0.90, as earlier).²¹ Figure 2a is very similar to figure 1a: signaling can occur in equilibrium only if the cost λ is not too high, where the highest acceptable λ increases with β ; if λ is low, both types of workers have an incentive to signal.²² The difference is in figure 2b. First, of all, there are now equilibria without referrals, when β is high (higher than α) and λ low - the area left white in the lower right corner of the figure. This is the equilibrium with no referrals and informative signaling discussed in section 4.2, and a second equilibrium with no referrals and all workers signaling when λ is particularly low. The low λ makes the firms' savings from referral hirings negligible, and the high β makes signaling

²¹As in Figure 1a, a second equilibrium, with $s_H \in (0, 1)$ and $s_L = 0$, exists in the region bordering the upward sloping frontier between the white and gray areas in Figure 2a. Again the figure omits it for ease of reading.

²²The sensitivity of the acceptable λ range to β is reduced, relative to the case where $\alpha = \beta$. At low β but constant α (and H firms only using referrals), equilibrium market wages are lower than they would be if α equalled β , keeping certification valuable and raising the highest acceptable λ . At high β , the effect is reversed: with constant α , smaller than β , market wages for uncertified workers are now higher and the incentive to signal is reduced, reducing in turn the highest acceptable λ .

a good channel of information, even in the absence of full separation.²³ It is clear from the figure though that even in the area where $\beta > \alpha$ ($\beta > 0.75$), the absence of referrals remain a rather special case. Second, the equilibrium where both H and L firms rely on referrals now is concentrated mostly in an area of high β and λ values. With $\alpha = 0.75$, L firms are discouraged from using referrals unless the savings from doing so are substantial: a range of high λ and β where signaling still occurs, the certification premium is high, and the composition of the uncertified labor pool worse than when hiring through referrals.

We can now provide a summary answer to our original question: does the availability of signaling lead firms to forego referrals? More precisely, how large is the region of the parameters space where equilibria without referrals can be supported? Figure 3 shows the full three-dimensional picture, for α and β between $1/2$ and 1 , and λ between 0 and 2.5 , with $\delta = 0.90$.²⁴ On the left-hand side, in grey, is the space where referrals do not take place, as function of the three parameters. Notice the two requirements $\beta > \alpha$ and, simultaneously, λ small. For comparison, the right-hand side shows the parameters space where signaling takes place in equilibrium, a much larger fraction of the total space. The darker shade of grey shows, in both cases, regions where signaling is exclusive to H workers: in the overwhelming majority of this space referrals continue to be employed.

6 Discussion

Armed with these results, we can ask other questions. For example, what is the effect of making certification less expensive - reducing λ ? Will personal connections become less important in labor markets? According to our model, the answer is not immediate, because it depends both on the precision of the information inherent in the personal network and

²³When only H workers signal, all certified workers must be H types, but the composition of the uncertified labor pool and the difference in wages still depend on β . Similarly, when all workers signal, some L workers are expected to become certified, but the composition of the two labor pools, and the wages, remain significantly different if β is high enough.

²⁴As mentioned earlier, results show little sensitivity to δ .

on the standards used in certification. Lowering certification costs reduces the self-selection that limits L workers' attempts to signal, and thus, *ceteris paribus*, reduces the information conveyed by being certified. Only when the signal is in itself precise enough, relative to the network, to limit the importance of this effect - when $\beta \gg \alpha$ - does the cheap availability of public information reduce the reliance on personal connections. But the opposite option of making certification *more* expensive - increasing λ - relying then on the information provided by self-selection, never reduces the use of personal referrals. On the contrary, it tends to increase the use of referrals, even when they are known to lead to a less than average probability of hiring productive workers. Similarly, what is the effect of increasing the standards for certification - increasing β ? Again, the answer depends on other factors too. Only when certification is both rigorous *and* cheap does it become a preferred option to personal referrals. We can also interpret the parameter α as correlated to the openness of a society - the more open and diverse, the lower the "in-breeding bias" and the less predictable the "quality" of a personal referral. Not surprisingly, the model tells that at high α , in a predictable and segregated society, it is very difficult to substitute personal referrals with markets - the information transmitted through personal connections is just too cheap and too accurate. But as the society becomes more open, diverse and mixed, that value of social contacts falls. With appropriate institutions - with high β and low λ signaling - markets can emerge.

A more ambitious task is linking the results of our model to the regularities that have emerged from the empirical literature on the use of social contacts in labor markets.²⁵ The least controversial observation is the negative correlation between the use of social ties in finding employment and the workers' education level (for example Staiger, 1990, for the US, and Pellizzari, 2003, for European countries), an observation that fits well the story told in this model: incomplete information prevents the firms' full knowledge of workers'

²⁵Again Ioannides and Datcher Loury (2004) provide a careful survey. Some recent works are Bentolila, Michelacci and Suarez (2004), Pellizzari (2003), Pistaferri (1999), Santamaria-Garcia (2003), Sylos Labini (2004).

characteristics, and referrals and education are two alternative means of partly revealing such characteristics. Referrals and education are substitutes - as they are in our model where workers hired through referrals can forego the step of obtaining a certification. In a particularly detailed data set on Italian college graduates, a more specific finding is the reduced reliance on social ties in professions like engineering and medicine, relative to social sciences or literature.²⁶ According to our model, the difference can be read in terms of β : either because the standards are tougher or because proficiency is more precisely defined, in medicine and engineering certification is a more precise measure of skills - β is higher - than in social sciences or literature. At low λ - at low cost of public education in Italy - the difference has a direct impact on the reliance on social ties.

The empirical finding that has received most attention and has been most disputed is the existence of a systematic premium paid to workers hired through referrals. A positive premium was found by the first US studies (for example Granovetter (1974), Corcoran et al. (1980) and Staiger (1990)), but has since been disputed. Bentolila et al. (2003) suggest a negative premium, while Pellizzari (2003) and Santamaria-Garcia (2003) find no systematic relation, once workers' and jobs' characteristics are controlled for.²⁷ Figure 4 depicts the referral wage and the market wages in our model. The top row (figures 4a) reports the referral wage and the average market wage as function of β , on the left, and as function of λ , on the right; the central row (figures 4b) distinguishes between the two market wages, for certified and for uncertified workers, and the bottom row (figures 4c) compares the referral wage to the average market wage of H workers and L workers separately.²⁸ The discontinuity points correspond to changes in equilibrium strategies, which can be read from Figure 2; at high values of λ multiple equilibria are possible, as shown in all figures on the right-hand side of Figure 4. All the figures support the difficulties found by researchers in identifying a

²⁶Sylos Labini (2004), based on the ISTAT Survey of Italian college graduates, 1998.

²⁷Sylos Labini (2004) makes the interesting point that not all social ties are equivalent: family ties and professional ties, in particular, may transmit quite different information. In his analysis of Italian data on college graduates, the negative premium is limited to jobs found through family ties.

²⁸The figures should be read keeping in mind that the referral premium would be higher if workers hired through referrals shared in the surplus.

systematic bias. The first row of figures suggests that if the referral wage is simply compared to the average market wage (a not unreasonable comparison in our model where there is only one type of job), the results are ambiguous: the direction of the bias depends on parameters. If these parameters plausibly differ across sectors and/or across countries, the conclusion confirms the heterogeneity across sectors and countries found by the literature. Controlling for the workers' characteristics first appears to yield cleaner results: all referral offers are made to uncertified workers and the premium, relative to the market wage for uncertified workers only, is unambiguously positive (figures 4b). But certification in our model is only an imperfect signal of workers' productivity, and the fact that all referrals are made to uncertified workers is an artifact of the timing of the model. A better analysis would try to control for workers' unobservable characteristics - here their productivity. Figures 4c show that the referral wage has a positive premium for L workers for most parameter values - i.e. it is higher than the market wage they would expect to receive - but has a discount for H workers. Again, as in the literature, the results are not consistent across different groups of workers, with discounts more probable in the case of more productive hires (as reported by Pellizzari, 2003, for example). Of course we are aware that the model is extremely stylized and these results, although suggestive, should be taken with care.

7 Conclusions

This paper has studied the extent to which firms and workers' reliance on networks of personal connections as channels of information about jobs is weakened by the availability of a signaling mechanism. The signaling mechanism is available to all but is costly, and its outcome is an imperfect signal of the worker's true productivity. The network on the other hand is free and connects a young worker to someone who is currently employed and whose productivity is known by the firm. Because connections are more likely between similar agents, the existence of a tie provides information to the firm about the productivity of

the young worker. We have found that although signaling can transmit information more precisely - because the cost induces workers to self-select - reliance on the network is very robust: only for a very small fraction of the parameters space of the model do referrals disappear.

The analysis was motivated by the desire to compare the network, possibly successful but exclusionary, to a market mechanism, open to all and anonymous. In fact, to the extent that they convey any information at all, both mechanisms must differentiate between different types of workers, a bias summarized in the model by the two parameters α and β . In what sense then is signaling in our model a “market mechanism” while the network is not? There are two main differences. First, the cost involved in the decision to signal plays a central role in the revelation of information - contrary to the case of free personal connections. Second, the information revealed by the network is local, whereas the information transmitted by the signal is global - a sentence that could be rephrased more precisely by plausibly defining the information as “verifiable” in the signaling case, and “non-verifiable” in the network case. In our model, the implication is that in the market firms compete for the surplus from the revelation of information, but they do not in the network.²⁹ It is the firms’ open entry into the market that at the end fundamentally distinguishes the two mechanisms.

Other market-type mechanisms seem possible and interesting. The most obvious one, closest in spirit to the Rauch (2001) and to our knowledge neglected by the formal literature on referrals in labor market, is a profit -driven intermediary: an employment agency. How would such an intermediary function in this model? Could it take over successfully the functions fulfilled by the network? We leave the answer to future research.

²⁹Some competition among firms would result if the direction of the ties were reversed, from old to young workers, as in Montgomery’s original paper. But the effect is only partial.

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A Appendix

Probability that a young worker receives a referral offer, conditional on firms using referrals.

The exact probability that an old worker of type H (of which N exist) has k connections in addition to i 's is given by:

$$\tilde{\gamma}_{k,H} = \sum_{j=0}^k \left[\binom{N-1}{c} \left(\frac{\alpha}{N}\right)^c \left(1 - \frac{\alpha}{N}\right)^{N-1-c} \binom{N}{d} \left(\frac{1-\alpha}{N}\right)^d \left(1 - \frac{1-\alpha}{N}\right)^{N-d} \right] \quad (\text{A1})$$

where

$$c \equiv \min(k - j, N - 1)$$

$$d \equiv \min(j, N)$$

The Poisson approximation $\gamma_{k,H}$

$$\gamma_{k,H} = \sum_{j=0}^k \left[\frac{\alpha^{k-j}}{(k-j)!} e^{-\alpha} \frac{(1-\alpha)^j}{j!} e^{-(1-\alpha)} \right] = \sum_{j=0}^k \left[e^{-1} \frac{\alpha^{k-j} (1-\alpha)^j}{(k-j)! j!} \right] = \frac{e^{-1}}{k!} \quad (\text{A2})$$

is the limit of (A1) as N tend to infinity and has well established bounds of error. For example, it can be shown (Feller, 1957, ch. 6) that

$$e^{-\alpha} \frac{\alpha^c}{c!} e^{-\frac{c^2}{N-c} - \frac{\alpha^2}{N-\alpha}} < \binom{N}{c} \left(\frac{\alpha}{N}\right)^c \left(1 - \frac{\alpha}{N}\right)^{N-c} < e^{-\alpha} \frac{\alpha^c}{c!} e^{c \frac{\alpha}{N}}.$$

implying that:

$$\lim_{N \rightarrow \infty} \tilde{\gamma}_{k,H} = \lim_{N \rightarrow \infty} \gamma_{k,H}$$

and therefore:

$$\lim_{N \rightarrow \infty} \left(1 - \sum_{k=1}^{2N-1} \frac{k}{k+1} \tilde{\gamma}_{k,H} \right) = \lim_{N \rightarrow \infty} \left(1 - \sum_{k=1}^{2N-1} \frac{k}{k+1} \gamma_{k,H} \right)$$

- i.e. the error introduced by the approximation does not distort the sum.

The last part of the derivation in the text states without proof that:

$$\lim_{N \rightarrow \infty} \left(\sum_{k=1}^{2N-1} \frac{k}{(k+1)!} \right) = 1$$

To see this, begin by expanding e^x :³⁰

$$\begin{aligned} e^x &= \sum_{k=0}^{\infty} \frac{x^k}{k!}, \\ &= 1 + x + \sum_{k=2}^{\infty} \frac{x^k}{k!}, \\ &= 1 + x + x \sum_{k=1}^{\infty} \frac{x^k}{(k+1)!}. \end{aligned}$$

Differentiating both sides with respect to x :

$$(e^x)' = e^x = 1 + \sum_{k=1}^{\infty} \frac{x^k}{(k+1)!} + x \sum_{k=1}^{\infty} \frac{kx^k}{(k+1)!},$$

or:

$$e^x = 1 + (e^x - x - 1)/x + x \sum_{k=1}^{\infty} \frac{kx^k}{(k+1)!}.$$

Setting $x = 1$:

$$e = 1 + (e - 1 - 1)/1 + \sum_{k=1}^{\infty} \frac{k}{(k+1)!},$$

³⁰We thank Peter S. Dodds for this proof.

or:

$$\sum_{k=1}^{\infty} \frac{k}{(k+1)!} = 1$$

□

Proof of Lemma 1. (i) When $s_H = s_L = 0$, we can write:

$$\Pi_H = \phi(V_H - V_L)(\alpha - h_{HU}) \tag{A3}$$

$$\Pi_L = \phi(V_H - V_L)(1 - \alpha - h_{HU})$$

and

$$h_{HU} = \frac{1 - r_H \alpha p - r_L (1 - \alpha) p}{2 - r_H p - r_L p} \tag{A4}$$

We proceed in two stages. First we show that $(V_H - V_L) > 0$ always. Then we show that $\Pi_H > 0$ and $\Pi_L < 0$ always. (1) If $r_L < 1$, $V_L = 0$ and $V_H \geq 1$, hence $(V_H - V_L) > 0$. If $r_L = 1$, there are two possibilities: (a) if $r_H < 1$, then $\Pi_H = 0$ and $V_H = 1$. In this case, $V_L = \delta \phi(1 - \alpha - h_{HU}) / (1 - \delta \alpha) < 1$ for all $\delta \leq 1$. Hence $(V_H - V_L) > 0$. (b) If $r_H = 1$ and $\Pi_H > 0$, then, by (5) and (A3) above, $(V_H - V_L) = 1 + \delta \phi(V_H - V_L)(2\alpha - 1) > 0$. Thus we can conclude that in all cases, $(V_H - V_L) > 0$. (2) From (A4), $\partial h_{HU} / \partial r_H < 0$, and $\partial h_{HU} / \partial r_L > 0$. Thus h_{HU} is maximal at $\{r_H = 0, r_L = 1\}$ and minimal at $\{r_H = 1, r_L = 0\}$: $h_{HU} \in [\underline{h}_{HU}, \overline{h}_{HU}]$, where $\underline{h}_{HU} \equiv (1 - \alpha p) / (2 - p)$ and $\overline{h}_{HU} \equiv [1 - (1 - \alpha)p] / (2 - p)$. But $\alpha > \overline{h}_{HU}$ and $(1 - \alpha) < \underline{h}_{HU}$ for all $\alpha > 1/2$. Since $(V_H - V_L) > 0$, we can then conclude that $\Pi_H > 0$ and $\Pi_L < 0$ always. If an equilibrium exists, it must have $r_H = 1$ and $r_L = 0$.

(ii). Suppose $r_L \in (0, 1)$ and $\Pi_L = 0$. Then, by (6), $V_L = 0$; but since $V_H \geq 1$, $V_H > V_L$. By (6) then $\Pi_H > 0$ and $r_H = 1$. Suppose $r_L = 1$ and $\Pi_L > 0$. Could it be that $\Pi_H \leq 0$? If so, $V_H = 1$ and $V_L = \delta(1 - e^{-1})(1 - \alpha + aV_L - w_r)$, or $V_L = \delta(1 - e^{-1})(1 - \alpha - w_r) / (1 - \delta \alpha) < 1$ for all $\delta \leq 1$ and $w_r \geq 0$. But if $V_H > V_L$ it must be that $\Pi_H > \Pi_L$ by (6), a contradiction. Hence if $r_L = 1$ and $\Pi_L > 0$, $\Pi_H > 0$ and $r_H = 1$.

(iii) By (12), signaling by either type of workers requires $w_C > w_U$ for all $\lambda > 0$. But then, since $\beta > 1/2$, the incentive to signal is always strictly higher for a H worker than a L worker, and the conclusion follows.

(iv) If $s_H \in (0, 1)$, then $w_r = w_U = h_{HU}(V_H - V_L) + V_L$ and $\Pi_H = \phi(V_H - V_L)(\alpha - h_{HU})$. By result (iii) in the Lemma, if $s_H \in (0, 1)$, then $s_L = 0$, hence

$$h_{HU} = \frac{(1 - r_H\alpha p - r_L(1 - \alpha)p)(1 - s_H\beta)}{(1 - r_H\alpha p - r_L(1 - \alpha)p)(1 - s_H\beta) + (1 - r_H(1 - \alpha)p - r_L\alpha p)} \quad (\text{A5})$$

It is then easy to verify that $\partial h_{HU}/\partial s_H < 0$, and since $\alpha > h_{HU}(s_H = 0)$, a fortiori $\alpha > h_{HU}(s_H > 0)$, $\Pi_H > 0$ and $r_H = 1$. \square

Proof of Proposition 1. To prove the proposition, it is sufficient to show the existence of some such equilibrium. Consider the candidate scenario $\{s_H = 1, s_L = 0, r_H = 1, r_L = 1\}$, where H workers in the market always signal but all firms always prefer hiring through referrals. Suppose $\beta = \alpha$. Equations (5) (6) (8) (9) and (10) yield $V_H, V_L, \Pi_H, \Pi_L, w_r, w_U$, and w_C . The incentive compatibility constraints (11) and (12) allow us to conclude that such scenario is an equilibrium if and only if $\lambda \in [\underline{\lambda}, \bar{\lambda}]$ where:

$$\underline{\lambda} = \max\left\{\frac{(1 - \alpha)(1 - h_{UH})}{1 - \delta\phi(2\alpha - 1)}, \frac{2\alpha - 1 + (1 - \alpha)h_{UH}}{1 - \delta\phi(2\alpha - 1)}\right\}$$

$$\bar{\lambda} = \frac{\alpha(1 - h_{UH})}{1 - \delta\phi(2\alpha - 1)}$$

and, by (A5):

$$h_{UH} = \frac{1 - \alpha}{2 - \alpha}$$

The unique upper bound is given by the requirement that λ should be low enough for H workers to be willing to signal; and the lower bounds by the incentive compatibility constraints on the L workers and the L firms (λ should be high enough for L workers not to

signal and L firms to prefer referrals)³¹ It is not difficult to verify that for all $\alpha \in (1/2, 1)$, $\bar{\lambda}$ is larger than either of the two lower bounds (the relevant lower bound is the first for $\alpha \leq 2 - \sqrt{2}$ and the second for higher α). The incentive compatibility constraints are satisfied and the scenario is an equilibrium for all $\alpha \in (1/2, 1)$. \square

Proof of Proposition 2. The existence of equilibria where signaling is perfectly informative has been established in Proposition 1. Consider now possible equilibria where referrals are not used. By Lemma 1, if $s_H = s_L = 0$, then $r_H = 1$; if $s_H \in (0, 1)$, then $r_H = 1$, and if $s_L > 0$, then $s_H = 1$. Thus the only workers' strategies compatible with the absence of referrals are: $\{s_H = 1, s_L = 0\}$, $\{s_H = 1, s_L \in (0, 1)\}$, and $\{s_H = 1, s_L = 1\}$. The first case is the only one of the three possibilities where signaling is perfectly informative and referrals do not take place. It was studied in detail in the text, and we showed there that the equilibrium requires $\beta \geq 2\alpha/(1 + \alpha) > \alpha \forall \alpha \in (1/2, 1)$, and thus is ruled out if $\alpha = \beta$. Proving that the latter two candidate scenarios cannot be equilibria amounts once again to showing that the incentive compatibility constraints must be violated. Deriving such constraints requires working through the appropriate wage and profits equations for each scenario, but given equations (5), (6), (8), (9) and (10) the derivation of the constraints is trivial, and we leave the details to the reader. In the second scenario, $\{s_H = 1, s_L \in (0, 1), r_H = r_L = 0\}$, the two binding constraints are that L workers must be indifferent about signaling, while H firms must prefer not to use referrals, or:

$$\lambda = \frac{(1 - \beta)(h_{HC} - h_{HU})}{1 - \delta(1 - e^{-1})[\alpha - (2\beta - 1)h_{HC} - 2(1 - \beta)h_{UC}]} \quad (\text{A6})$$

$$\lambda < \beta(h_{HC} - h_{HU}) + h_{HU} - \alpha \equiv \bar{\lambda} \quad (\text{A7})$$

³¹If the incentive compatibility constraint ensuring that the L firms' strategy is a best response is satisfied, the equivalent constraint on H firms is satisfied automatically.

where:

$$h_{HC} = \frac{\beta}{\beta + (1 - \beta)s_L}$$

$$h_{HU} = \frac{1 - \beta}{1 + (1 - \beta)(1 - s_L)}$$

For any given λ , (A6) identifies the equilibrium s_L , as long as (A7) is satisfied. Substituting $\alpha = \beta$ and (A7) in (A6), we can write:

$$\lambda = \frac{(1 - \beta)(h_{HC} - h_{HU})}{1 + \delta(1 - e^{-1})[(1 - \beta)(h_{HC} - h_{HU}) - \bar{\lambda}]}$$

or:

$$\bar{\lambda} > \frac{(1 - \beta)(h_{HC} - h_{HU})}{1 + \delta(1 - e^{-1})[(1 - \beta)(h_{HC} - h_{HU}) - \bar{\lambda}]} \quad (\text{A8})$$

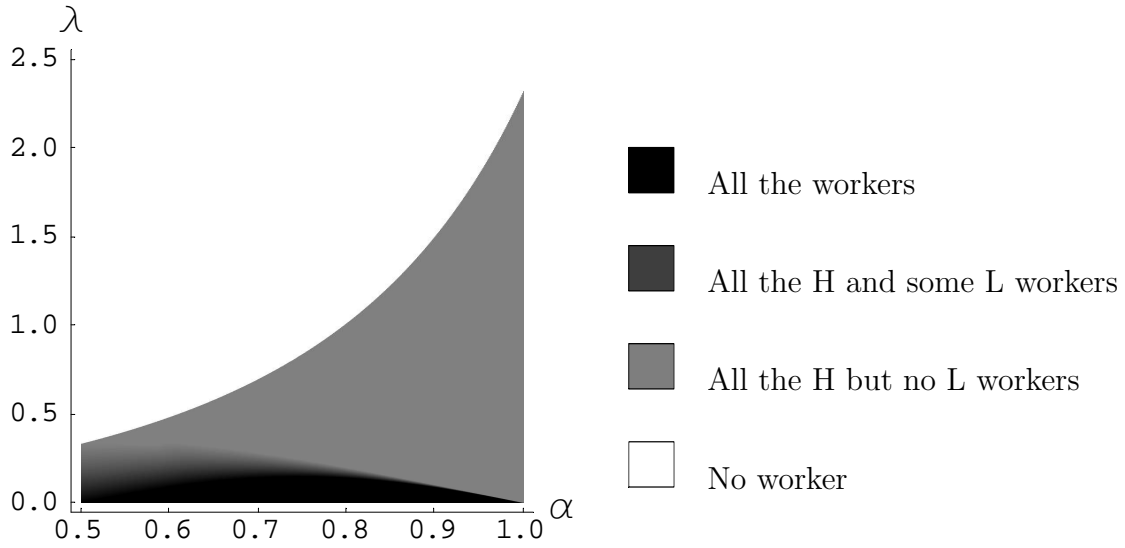
It is not difficult to verify that for all $s_L \in (0, 1)$, $(1 - \beta)(h_{HC} - h_{HU}) > \bar{\lambda}$. Hence (A8) implies

$$\delta(1 - e^{-1})[(1 - \beta)(h_{HC} - h_{HU}) - \bar{\lambda}]\bar{\lambda} > [(1 - \beta)(h_{HC} - h_{HU}) - \bar{\lambda}]$$

a condition that can only be satisfied for $\bar{\lambda} > 1$. But for all $s_L \in (0, 1)$, $h_{HC} > h_{HU}$, implying $\bar{\lambda} < h_{HC} - \beta < 1$. The scenario cannot be an equilibrium when $\alpha = \beta$. In the third scenario, $\{s_H = 1, s_L = 1, r_H = r_L = 0\}$, if H firms do not use referrals it must be that: $\lambda < \beta(2\beta - 1) + 1 - \beta - \alpha$. If $\alpha = \beta$ the constraint becomes $\lambda < (\beta - 1)(2\beta - 1) < 0$, which is violated for all $\lambda > 0$, $\beta \in (1/2, 1)$.

Proof of Proposition 3. The same argument used to prove Proposition 1 proves Proposition 3. \square

(a) Equilibrium Signalling



(b) Equilibrium Referral

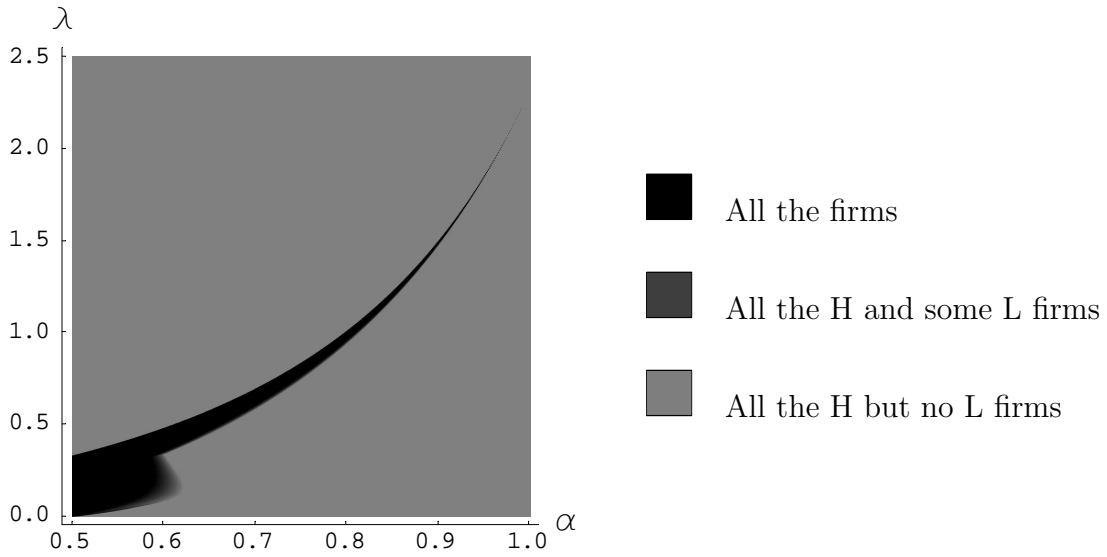
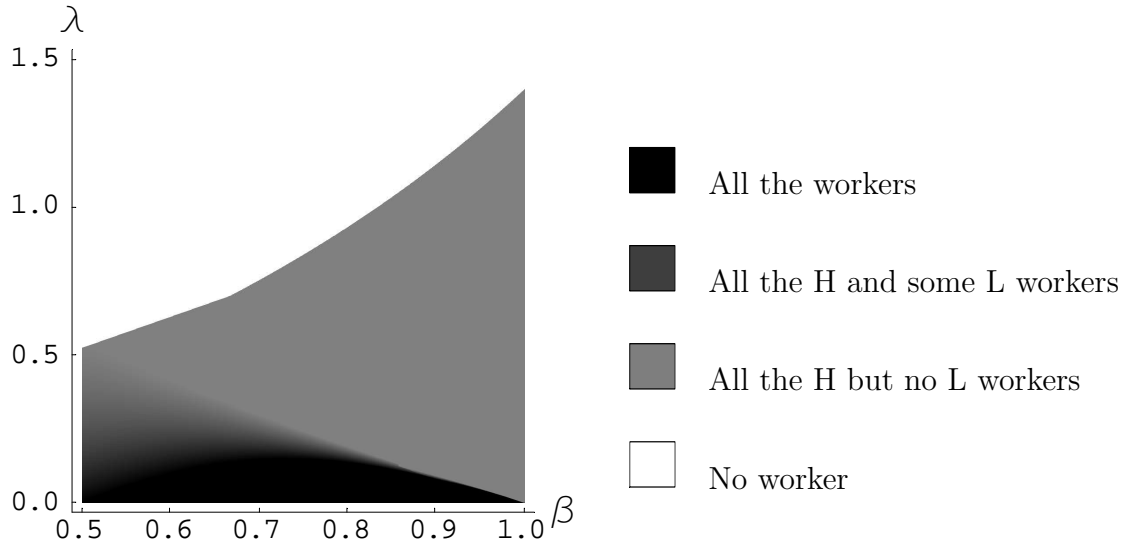


Figure 1: (a) Equilibrium signaling and (b) referral in $\alpha - \lambda$ space for $\alpha = \beta$ and $\delta = 0.90$.

(a) Equilibrium Signalling



(b) Equilibrium Referral

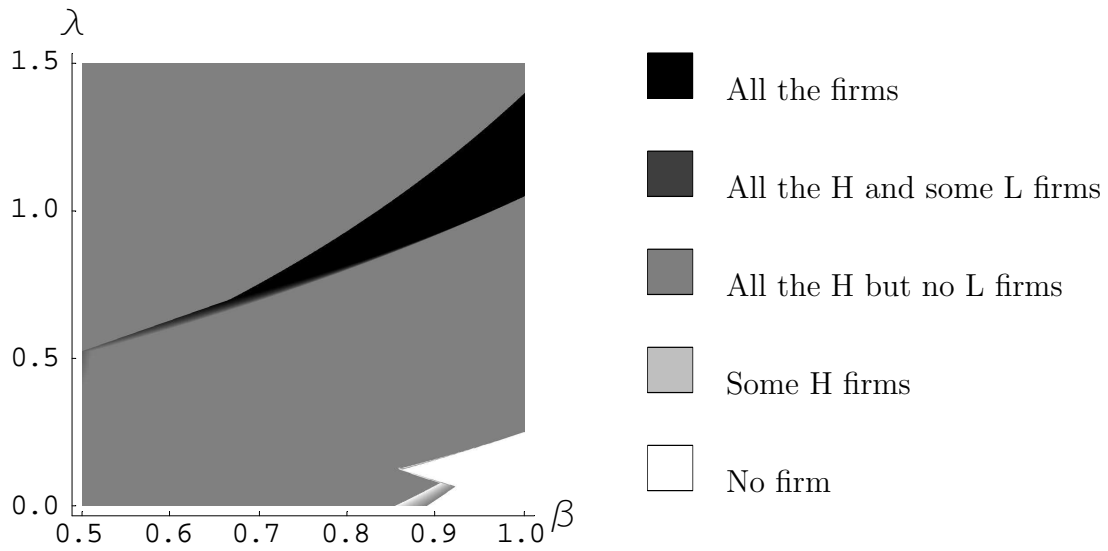


Figure 2: (a) Equilibrium signaling and (b) referral in β - λ space for $\alpha = 0.75$ and $\delta = 0.90$.

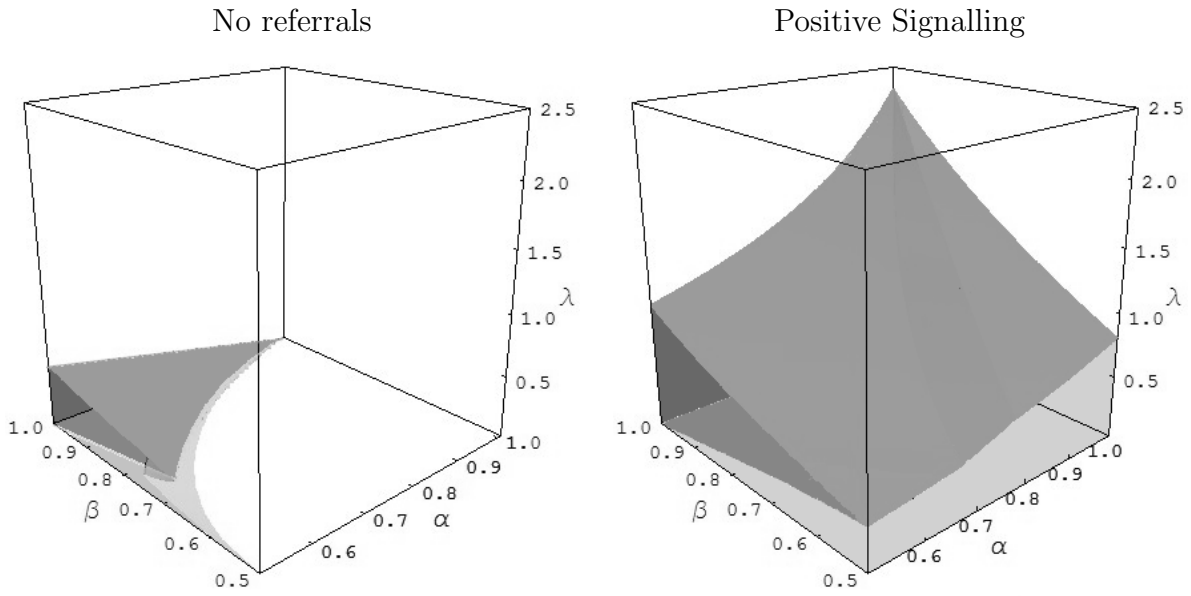
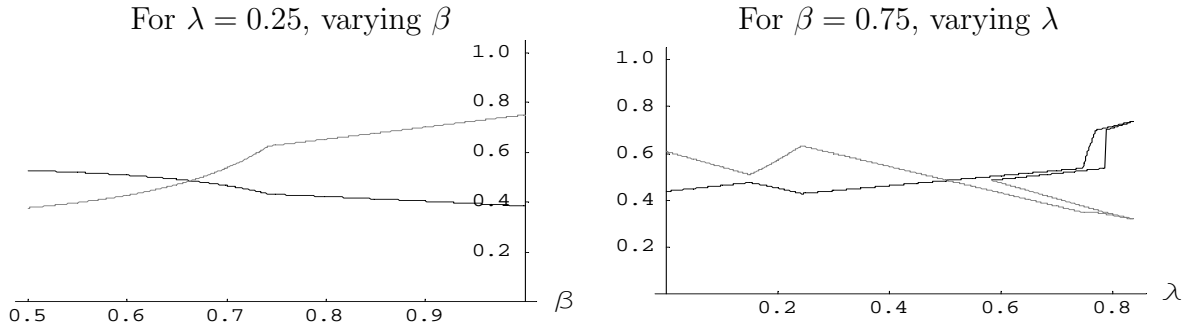
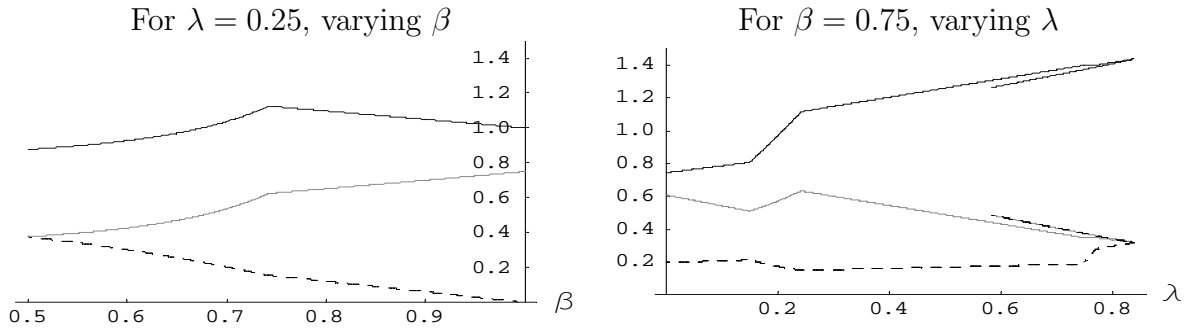


Figure 3: The space of parameters where equilibria without referrals exist (left) and where equilibria with signaling exist (right). Darker grey correspond to informative signaling ($s_L = 0$). $\delta = 0.90$

(a) Average market wage and referral wage



(b) Market wage for certified and uncertified workers and referral wage



(c) Average market wage for H and L workers and referral wage

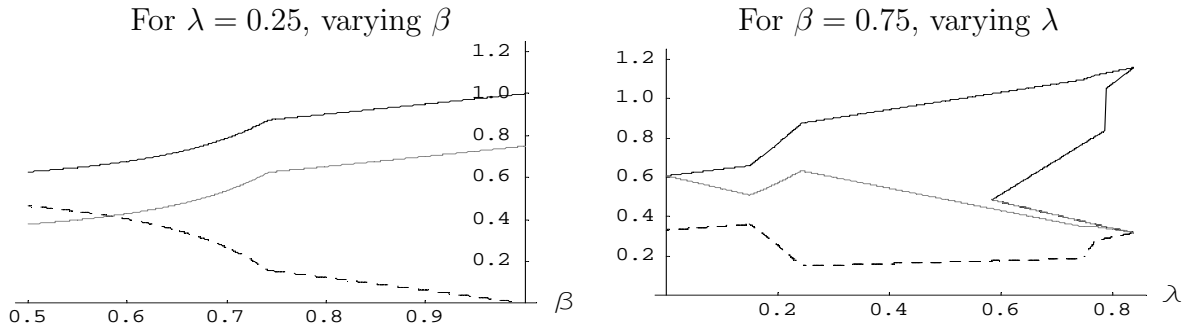


Figure 4: (a) Average market wage (black) and referral wage (gray). (b) Market wage for certified workers (black, solid), market wage for uncertified workers (black, dashed), and referral wage (gray). (c) Average market wage for H workers (black, solid), average market wage for L workers (black, dashed), and referral wage (gray). Notice the multiple equilibria in the $\beta = 0.75$ figures at high values of λ . For all figures $\alpha = 0.75$ and $\delta = 0.90$

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(lxv) This paper was presented at the EuroConference on “Auctions and Market Design: Theory, Evidence and Applications” organised by Fondazione Eni Enrico Mattei and sponsored by the EU, Milan, September 25-27, 2003

(lxvi) This paper has been presented at the 4th BioEcon Workshop on “Economic Analysis of Policies for Biodiversity Conservation” organised on behalf of the BIOECON Network by Fondazione Eni Enrico Mattei, Venice International University (VIU) and University College London (UCL), Venice, August 28-29, 2003

(lxvii) This paper has been presented at the international conference on “Tourism and Sustainable Economic Development – Macro and Micro Economic Issues” jointly organised by CRENoS (Università di Cagliari e Sassari, Italy) and Fondazione Eni Enrico Mattei, and supported by the World Bank, Sardinia, September 19-20, 2003

(lxviii) This paper was presented at the ENGIME Workshop on “Governance and Policies in Multicultural Cities”, Rome, June 5-6, 2003

(lxix) This paper was presented at the Fourth EEP Plenary Workshop and EEP Conference “The Future of Climate Policy”, Cagliari, Italy, 27-28 March 2003

(lxx) This paper was presented at the 9th Coalition Theory Workshop on "Collective Decisions and Institutional Design" organised by the Universitat Autònoma de Barcelona and held in Barcelona, Spain, January 30-31, 2004

(lxxi) This paper was presented at the EuroConference on “Auctions and Market Design: Theory, Evidence and Applications”, organised by Fondazione Eni Enrico Mattei and Consip and sponsored by the EU, Rome, September 23-25, 2004

(lxxii) This paper was presented at the 10th Coalition Theory Network Workshop held in Paris, France on 28-29 January 2005 and organised by EUREQua.

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