

Contracting with Externalities and Outside Options

Francis Bloch and Armando Gomes

NOTA DI LAVORO 78.2004

MAY 2004

CTN – Coalition Theory Network

Francis Bloch, *Ecole Supérieure de Mécanique de Marseille and GREQAM*
Armando Gomes, *Department of Finance, the Wharton School, University of Pennsylvania*

This paper can be downloaded without charge at:

The Fondazione Eni Enrico Mattei Note di Lavoro Series Index:
<http://www.feem.it/Feem/Pub/Publications/WPapers/default.htm>

Social Science Research Network Electronic Paper Collection:
<http://ssrn.com/abstract=XXXXXX>

The opinions expressed in this paper do not necessarily reflect the position of
Fondazione Eni Enrico Mattei

Contracting with Externalities and Outside Options

Summary

This paper proposes a model of multilateral contracting where players are engaged in two parallel interactions: they dynamically form coalitions and play a repeated normal form game with temporary and permanent decisions. This formulation encompasses many economic models with externalities and outside options. We show that when outside options are pure (i.e. independent of the actions of other players), there exists a Markov Perfect equilibrium resulting in efficient outcomes when players become perfectly patient. If outside options are not pure, all Markov perfect equilibria may be inefficient. The distribution of coalitional gains and the dynamics of coalition formation are characterized in four illustrative applications.

Keywords: Outside options, Externalities, Coalitional bargaining

JEL Classification: C71, C72, C78, D62

We are grateful to seminar participants at Cal Tech, Toulouse, the Roy seminar in Paris and ESEM 2003 in Stockholm for helpful comments.

This paper was presented at the 9th Coalition Theory Workshop on "Collective Decisions and Institutional Design" held in Barcelona, Spain, on 30-31 January 2004 and organised by the Universitat Autònoma de Barcelona.

Address for correspondence:

Francis Bloch
Ecole supérieure de mécanique de Marseille and GREQAM
2 rue de la Charité
13002 Marseille
France
Email: bloch@ehess.cnrs-mrs.fr

1 Introduction

Multilateral contracting often involves strategic negotiations. The recent examples of the Kyoto protocol to reduce the emission of greenhouse gases, and of the Doha round to eliminate tariffs in international trade show that countries adopt a number of strategies (such as forming groups, delaying decisions, leaving the negotiations table) to affect the outcome of negotiations. Given the importance of the decisions taken through multilateral negotiations, it is a worthwhile task for economists to try and understand what leads parties to sometimes reach inefficient, partial contracts instead of forming global agreements.

In order to model multilateral negotiations, we resort to an extension of Rubinstein (1982)'s bargaining model to more than two players (see discussion of literature below), in which we allow for coalition formation and strategic action choices. We construct a model where players are engaged in two parallel interactions: they propose to form coalitions in order to extract gains from cooperation; and coalitions participate in a repeated normal form game, where they choose actions that may either be temporary or permanent (exiting or opting out). The model thus encompasses a wide variety of situations involving externalities and endogenous exit decisions. We argue that the combination of strategic action choices and coalition formation is not merely a technical nicety but also provides novel insights into multilateral contracting that have economic applications.

Our analysis centers around three questions: When is the outcome of multilateral contracting efficient? Are coalitions formed immediately or gradually? What is the distribution of gains from cooperation in the equilibrium contract? We provide an answer to the first question in the most general context. We address the dynamics of coalition formation and the distribution of gains from cooperation in selected illustrative applications.

In classical models of two player bargaining, when a player chooses her outside option, negotiations end and the other player is left with a fixed payoff. In the context of multilateral negotiations, when a player opts out and

chooses to enforce a permanent action, the other players continue to bargain over the formation of coalitions and continue to choose actions which may affect the payoff of the exiting player. We point out that there is a crucial distinction between situations where outside option values are independent of the action of other players (a case we label *pure outside options*) and situations where players' outside option values are affected by the actions of remaining players.

The key result of our paper is that *there always exist an efficient equilibrium outcome in games with pure outside options*. To understand this result, notice first that, because players make simultaneous action choices, coordination failures may arise, and we cannot rule out inefficient equilibria where all players simultaneously exit. In order to select equilibria which are immune to coordination failures, we introduce a refinement of equilibrium in which at every choice of actions, players remain in the game with a probability greater than $\varepsilon > 0$. In games with pure outside options, we show that as players become perfectly patient, equilibria without coordination failure exist and are efficient— the probability of exit converges to zero, and all players eventually reach an efficient global contract. The intuition underlying these results is easily grasped. Early exit results in an aggregate efficiency loss. In a game with pure outside options, players are able to capture this inefficiency loss and will never choose to leave before the grand coalition is formed. By staying in the game one more period, a player is guaranteed to obtain her outside option (which remains available because outside options are pure), and is able to capture the inefficiency loss by proposing to form the grand coalition when she is recognized to make an offer. Hence, early exit will never occur in equilibrium.

The previous result depends crucially on the fact that outside options are independent of the actions of the other players. We provide an example to show that, in games where outside options are not pure, *all equilibrium outcomes may lead to the inefficient formation of partial coalitions*. The three-player example we construct displays the following features: (i) once a two-player coalition has formed, players obtain a large payoff when they

are the only ones exiting the game, and the unique equilibrium of the simultaneous action game is completely mixed, so that exit occurs with a positive probability, and (ii) at the initial stage where all players are singletons, players have an incentive to form a two-player coalition, as a partial agreement results in a large asymmetry between the two-player coalition and the remaining singleton. When both features are present (incentives to exit alone and large payoff to partial agreements), in all equilibria, players initially choose to form a two-player coalition, and to exit the game with a positive probability. These equilibria are obviously inefficient, as players exit before extracting all gains from cooperation.

In order to analyze in more detail the equilibria of the game, we consider four illustrative applications of the model. The first two applications deal with games with pure outside options, which as we already know admit efficient equilibria when there are no coordination failures. We focus our attention on the distribution of gains and the dynamics of contracting. The first application is an extension of two-player games with outside options to a multilateral context. We show that the equilibrium (without coordination failures) of the multilateral game reflects the “outside option principle”: either outside options are binding and the player with the largest outside option receives her outside option, or they are not binding and the outcome of bargaining is unaffected by outside options. However, when outside options are binding, the equilibrium exhibits a novel property: the equilibrium payoff of all players depend on the *entire vector of outside options* (and is an increasing function of players’ own outside options). The main reason for the surprising result is that the player with the largest outside option randomizes between exiting and staying after a rejection, so that even values of small outside options matter because they can credibly occur off the equilibrium path.

In our second application, we analyze the principal-agent models with externalities proposed by Segal (1999), where a single principal contracts with several agents, and the contract imposes externalities on non-trading agents. We focus on the dynamics of coalition formation in a model with

symmetric agents, and show that when trading between the principal and agents induces positive externalities on other agents, the principal and agents contracts to form the grand coalition in one step. When trading induces negative externalities, the grand coalition is formed in two steps. The principal first chooses to contract with a subset of agents in order to reduce the outside opportunities of the remaining agents.

The last two applications consider games where the payoff of exiting players depends on the actions chosen by remaining players. We first consider a three-player pure public good game, similar to the game studied by Ray and Vohra (2001). Countries negotiate over the reduction of pollution levels, and partial contracts result in positive externalities on the other countries. We show that the grand coalition does form in equilibrium. Depending on the value of partial agreements, a global agreement is either reached immediately or in two steps. Finally, we discuss a model of market entry with synergies, where firms may merge –and benefit from synergies – before entering the market. In this model, the merger of two firms induces negative externalities on the remaining firms. Assuming that the market can only support one firm, we exhibit a range of parameter values for which the game results in the inefficient formation of a partial agreement.

The rest of the paper is organized as follows. Section 2 presents the model and Section 3 contains preliminary results on characterization and existence of equilibria. In Section 4, we discuss efficiency of the bargaining outcomes, and establish our main results. Section 5 discusses our four illustrative applications, and Section 6 concludes. We start with a review of the existing literature on coalition formation.

Literature Review

The model we propose belongs to a family of extensive form games extending Rubinstein (1982)'s model to more than two players. In order to situate our contribution with respect to the existing literature, we summarize in the table below earlier work on related models of coalitional bargaining.¹

¹We did not include in the table models where multiple offers can be made at any point

	immediate exit	continuous renegotiations	endogenous exit
<u>no externalities</u>			
fixed order	Chatterjee et al. (1993)	Seidmann Winter (SW)(1998)	SW(1998)
random order	Okada (1996)	Gul (1989)	
<u>externalities</u>			
fixed order	Bloch (1996) Ray Vohra (1999)		
random order	Montero (1999)	Gomes (2001)	THIS PAPER

In the first column, we list models where coalitions are forced to exit after they form. It is well-known that this assumption may result in inefficient outcomes, even in the absence of externalities.² Clearly, this inefficiency is still present in the larger class of games with externalities.

By contrast, the second column lists models where players never leave the game, and extract a flow payoff every period. In these games with continuous renegotiations, the grand coalition is ultimately formed, as players will continue negotiating until all gains from cooperation are exhausted. Seidmann and Winter (1998) focus their attention on conditions under which the grand coalition is formed immediately or gradually; Gomes (2001) shows that delays in the formation of the grand coalition arise in games with negative externalities, and that the grand coalition forms immediately in games with positive externalities..

To the best of our knowledge, the only precursor to our study, allowing coalitions to endogenously choose when to exit, is one of the models proposed by Seidmann and Winter (1998). Our model differs from theirs in various aspects. First, they consider a fixed order whereas we allow for random choice in the identity of the proposer. Second, and more importantly,

in time. Perry and Reny (1994) and Maskin (2003) propose models where coalitions can bid for new members by making simultaneous offers. We also did not include models based on effectivity functions such as Gomes and Jehiel (2002) and Konishi and Ray (2003).

²Consider the following example, inspired by Chatterjee et al. (1993). Let $n = 3$ and the gains from cooperation be represented by a coalitional function $v(S) = 0$ if $|S| = 1$, $v(S) = 3$ if $|S| = 2$ and $v(S) = 4$ when $|S| = 3$. As δ converges to 1, the outcome of the bargaining procedure where the grand coalition forms should result in equal sharing of the coalitional surplus among the symmetric players ($\frac{4}{3}$ for every player). But clearly, players then have an incentive to deviate forming an inefficient coalition of size 2, inducing a payoff of $\frac{3}{2}$ for each coalitional member. If this coalition must leave the negotiation after its formation, the additional surplus of 1 is lost.

the underlying gains from cooperation in their model are represented by a coalitional function (with no externalities), whereas payoffs in our model are based on strategic interaction at the action phase. These differences preclude a direct comparison of our results, and in particular the distinction between games with pure outside options or general outside options is irrelevant in the context of Seidmann and Winter (1998).

2 The Model

We model the formation of coalitions and bargaining as an infinite horizon game, with two distinct phases at every period. Any period starts with a *contracting phase*, where a player is chosen at random to propose a coalition, and a payment to all other coalition members. All prospective members respond in turn to the offer, and the coalition is formed only if all its members agree to the contract. If a coalition is formed, the proposer acquires control rights over the resources of coalition members. We then identify the player with the coalition formed. In the *action phase*, all active players choose an action, which may be a permanent action (in which case the player exits the game) or a temporary action. The action profile determines a flow payoff for all the players, representing the underlying economic opportunities.³ The interplay between the contracting and action phases enables us to consider simultaneously issues of coalition formation, externalities and endogenous exit decisions.

Formally, let N be a set of agents, indexed by $i = 1, 2, \dots, n$. A coalition S is a non-empty subset of agents, and a coalition structure is a partition of the set N into disjoint coalitions, $\{S_1, \dots, S_j, \dots, S_J\}$. Time is discrete and runs as $t = 1, 2, \dots, \infty$ and every period t is decomposed into two subperiods: a contracting phase and an action phase. Subgames are described by a state variable s composed of the set of active players, the set of players that have

³This contrasts with all other models of coalitional bargaining, where underlying benefits from cooperation are either represented by games in coalitional function form (Chatterjee et al. (1993), Seidmann and Winter (1998)) or by games in partition function form (Ray and Vohra (1999), Gomes (2001)).

exited, and their exit decisions.

Contracting phase: Let $\mathcal{N}(s)$ be the set of active players at state s . One of the players in $\mathcal{N}(s)$ is chosen at random to make an offer. The probability with which player S is chosen to make an offer, $q_S(s)$, is exogenously given and may depend on the state. An offer is a pair $c = (\mathcal{S}, t)$, where \mathcal{S} is a subset of players in $\mathcal{N}(s)$ and t a vector of transfers satisfying $\sum_{S \in \mathcal{S}} t_S = 0$. We interpret the transfer t_T as the net present value of a flow of payments, by which player S obtains control over the resources of player T . When player S has obtained control over the resources of all the players in \mathcal{S} , we identify the player with the coalition.⁴ A fixed protocol determines the order in which players in $\mathcal{S} \setminus S$ respond to the offer c . If all of them accept the offer, the coalition is formed, and a new state is obtained, with a set of active players $(\mathcal{N}(s) \setminus \mathcal{S}) \cup \{\cup_{T \in \mathcal{S}} T\}$. If one of the prospective members of \mathcal{S} rejects the offer, no trade takes place and the state stays at s .

Action phase: At the action phase in state s , all active players in $\mathcal{N}(s)$ simultaneously choose an action. As noted above, a player in $\mathcal{N}(s)$ may have acquired control over the resources of a coalition S . In that case, her action set is given by a set A_S which may be different from $A_S = \times_{j \in S} A_j$.⁵ The action set A_S is decomposed into a set of permanent (or *exit*) actions E_S and a set of temporary (or *reversible*) actions R_S . In many applications, the two sets only consist of one element: a single action $r \in R_S$ interpreted as “remaining in the game”, and a single action, $e \in E_S$, interpreted as “exiting the game”. By choosing a permanent action $e_S \in E_S$, a player simultaneously commits to play the same action ad infinitum and to leave the negotiations (the set of players who have exited at state s is denoted by $\mathcal{E}(s)$). Hence, we interpret a permanent action as an irreversible investment made by the player, which is not subject to renegotiation.

⁴As active players are identified with the coalitions they control, we do not keep track of the identity of the agents who control coalitions.

⁵In some applications, it may be natural to suppose that a player who has acquired a coalition S has access to an action set $A_S = \times_{i \in S} A_i$. This is only one of the possible interpretations of our model, and we prefer to define generally action sets for all the coalitions.

At the end of the action phase, flow payoffs are collected by all the players. If the *action profile* is $a = (r_{T,T \in \mathcal{N}(s)}; e_{T,T \in \mathcal{E}(s)})$ flow payoffs accrue to all players in $\mathcal{N}(s) \cup \mathcal{E}(s)$ according to utility functions $v_S(a)$. The payoff flow (or single-period payoff) is $(1 - \delta) v_S(a)$ with present value $v_S(a)$, where $\delta \in (0, 1)$ is the common discount rate of all players. Note that the payoff functions $v_S(a)$ are defined, for every coalition S and every coalition structure containing S , and the actions taken by all coalitions in the coalition structure.⁶ When the grand coalition forms, we let V denote the total payoff of the grand coalition, and assume that the grand coalition is efficient, i.e.

$$V > \sum_{S \in \mathcal{N}(s) \cup \mathcal{E}(s)} v_S(a) \text{ for any state } s \text{ and action profile } a.$$

Formally, a state of the game s is described by three elements: the active players in the game, $\mathcal{N}(s)$, the set of players who have exited, $\mathcal{E}(s)$, and the permanent actions they have chosen, $e(s) = (e_{T,T \in \mathcal{E}(s)})$. We restrict our attention to *Markovian* strategies. Hence, at the contracting phase, a proposer's strategy only depends on the current state s , a respondent's strategy only depends on the current state s and the current offer she receives t_T . At the action phase, strategies only depend on the current state s . A *Markov perfect equilibrium* (MPE) is a Markovian strategy profile, where every player acts optimally at every contracting phase of the game, and all players play a Nash equilibrium at every action phase.

For a given Markovian strategy, let $\phi_S^1(s)$ denote the continuation value of the game for player S at the contracting phase at state s (before the choice of proposer), and $\phi_S^2(s)$ denote the continuation value of player S at the action phase of state s . Finally, we denote by Φ_i the value of the game for player i at the initial contracting stage, when no coalition has formed.

⁶Again, we note that in some applications, it is natural to assume $v_S(a) = \sum_{i \in S} v_i(a)$, but this is only one of the possible interpretations of our model.

3 Characterization and Existence

We now provide a complete characterization of equilibrium. At any state s , we first compute the mixed strategy equilibria at the action phase, taking continuation values $\phi_S^1(\cdot)$ as given.

The action stage at state s can be represented by a standard game in strategic form, $\Gamma(s) = (\mathcal{N}(s), \{A_S, u_S(s, \cdot)\}_{S \in \mathcal{N}(s)})$, where players are the active players at state s , A_S the action set of player S and payoffs $u_S(s, \cdot)$ are defined as follows. For any action profile a , let $\mathcal{P}(a)$ be the set of active players who have chosen permanent (exit) actions, and e denote those permanent actions. Define $h(s, a)$ to be the new state reached after the choice of actions a , i.e. $h(s, a) = \{\mathcal{N}(s) \setminus \mathcal{P}(a), \mathcal{E}(s) \cup \mathcal{P}(a), (e(s), e)\}$. In words, the state $h(s, a)$ is the state reached from state s , when players in $\mathcal{P}(a)$ have chosen the permanent actions e . The payoff function $u_S(s, \cdot)$ corresponds to the continuation value of the game at the action phase. Players receive a flow payoff of $(1 - \delta)v_S(a, e(s))$ in the current period, and the game moves to the contracting phase of state $h(s, a)$ in the next period, so that

$$u_S(s, a) = \delta\phi_S^1(h(s, a)) + (1 - \delta)v_S(a, e(s)).$$

In a Markov perfect equilibrium, the strategy profile $\sigma^2(s)$ of active players at the action phase of state s must be a Nash equilibrium of game $\Gamma(s)$.

We now suppose that the continuation values at the action phases $\phi_S^2(\cdot)$ are fixed, and compute the optimal behavior of proposers and respondents at the contracting stage of state s . If any player T rejects the contract offered, the game moves to the action phase of state s and player T receives a payoff $\phi_T^2(s)$. The minimal offer that player T accepts is $\phi_T^2(s)$, and thus any proposer optimally offers $t_T = \phi_T^2(s)$. Given a contract $c = (\mathcal{S}, t)$, define the state obtained when the offer is accepted at state s by $g(c, s) = \{(\mathcal{N}(s) \setminus \mathcal{S}) \cup \{\cup_{T \in \mathcal{S}} T\}, \mathcal{E}(s), e(s)\}$ — i.e. all coalitions belonging to \mathcal{S} cease to exist and a new larger coalition, $\cup_{T \in \mathcal{S}} T$, is formed. If player S proposes a contract c and the contract is accepted, the game moves to the action phase of state $g(c, s)$. The surplus of the proposer is thus given

by $\phi_{\cup_{T \in \mathcal{S}} T}^2(g(c, s)) - \sum_{T \in \mathcal{S}} \phi_T^2(s)$. The proposer thus selects the coalition formed, \mathcal{S} , in order to solve:

$$\max_{\mathcal{T} \subset \mathcal{N}(s), \mathcal{S} \in \mathcal{T}} \phi_{\cup_{T \in \mathcal{T}} T}^2(g(c, s)) - \sum_{T \in \mathcal{T}} \phi_T^2(s).$$

If different coalitions result in the same maximal payoff, player S may randomize across the coalitions formed, and we let $\sigma^1(s)$ denote the probability distribution over all subsets $\mathcal{S} \subset \mathcal{N}(s)$, $S \in \mathcal{S}$ that player S may form at state s . We have now completely characterized the Markov perfect equilibrium of the game at state s for fixed continuation values $\phi_S^1(\cdot)$ and $\phi_S^2(\cdot)$. To summarize:

Lemma 1 *A strategy profile σ is a Markov perfect equilibrium if and only if there exists payoffs $\phi_S^1(s), \phi_S^2(s)$ such that:*

- (i) *at the action stage, $\sigma^2(s)$ is a Nash equilibrium of the game $\Gamma(s) = (\mathcal{N}(s), \{A_S, u_S(s)\}_{S \in \mathcal{N}(s)})$ where $u_S(s, a) = \delta \phi_S^1(h(s, a)) + (1 - \delta)v_S(a, e(s))$, and $\phi_S^2(s)$ is the equilibrium payoff of coalition S at this equilibrium;*
- (ii) *at the contracting stage, for all contracts $c = (\mathcal{S}, t)$ in the support of $\sigma^1(s)$:*

$$\begin{aligned} t_T &= \phi_T^2(s) \text{ for all } T \in \mathcal{S}, \text{ and} \\ \mathcal{S} &\in \arg \max_{\mathcal{T} \subset \mathcal{N}(s), \mathcal{S} \in \mathcal{T}} \phi_{\cup_{T \in \mathcal{T}} T}^2(g(c, s)) - \sum_{T \in \mathcal{T}} \phi_T^2(s) \end{aligned}$$

The continuation value at the contracting stage is given by

$$\begin{aligned} \phi_S^1(s) &= q_S(s) \sum_{\mathcal{S}} \sigma_S^1(s) (\mathcal{S}) (\phi_{\cup_{T \in \mathcal{S}} T}^2(g(c, s)) - \sum_{T \in \mathcal{S}} \phi_T^2(s)) \\ &\quad + \sum_{T \in \mathcal{N}(s), T \neq S} q_T(s) \sum_T \sigma_T^1(s) (T) (\mathbf{1}_{S \in T} \phi_S^2(s) + \mathbf{1}_{S \notin T} \phi_S^2(g(c, s))) \end{aligned}$$

where $q_S(s)$ is the probability that coalition S makes an offer at state s and $\mathbf{1}$ is the indicator function.

The Lemma gives a complete characterization of equilibrium, and enables us to compute the continuation values of the game at the contracting and

action stages. At the action stage, the continuation value is obtained as the equilibrium payoff of a strategic game played by the active players. At the contracting stage, the continuation value is obtained as an expected value, considering three possible situations. With probability $q_S(s)$, player S is called to make an offer, and proposes to form any optimal coalition \mathcal{S} , obtaining a surplus $(\phi_{\cup_{T \in \mathcal{S}} T}^2(g(c, s)) - \sum_{T \in \mathcal{S}} \phi_T^2(s))$. With probability $q_T(s)$, another player T is recognized to make an offer, and proposes a coalition \mathcal{T} . Either player S belongs to coalition \mathcal{T} , and receives the offer $\phi_S^2(s)$, or player S does not belong to the coalition, and receives her continuation value $\phi_S^2(g(c, s))$ at the action phase of state.

We now prove the existence of continuation values $\phi_S^1(s)$ and $\phi_S^2(s)$ satisfying the conditions of the above Lemma, and show that the coalitional bargaining game always has a Markov perfect equilibrium.

Proposition 1 *The coalitional bargaining game admits a Markov perfect equilibrium.*

The characterization results of this section will be used to construct Markov perfect equilibria in the examples and applications of the next sections.

4 Efficiency

We start the efficiency analysis of coalitional bargaining game by considering games with *pure outside options*, where a player's payoff after exit is independent of the actions of the other players. Formally:

Definition 1 *The underlying game v is a game with pure outside options if and only if for all players S choosing $e_S \in E_S$, $v_S(a_{-S}, e_S) = v_S(a'_{-S}, e_S)$, $\forall a_{-S}, a'_{-S} \in A_{-S}$.*

The condition above clearly applies to the games without externalities studied by Seidmann and Winter (1999). But it also applies to games with externalities like the principal agent problems considered by Segal (1999).

Moreover, the condition does not rule out the possibility that players' actions affect the interim payoffs of other players, which may have an important influence on the coalitions ultimately formed and the distribution of gains from cooperation.

We show that games with pure outside options always admit Markov perfect equilibria where contracting results in an approximately Pareto efficient outcome. Formally, we show that for any $\xi > 0$, $\sum \Phi_i > V - \xi$ for all $\delta \geq \delta(\xi)$, where we recall that Φ_i is player i value at the beginning of the game. We also show that when externalities on players' exit payoffs are negligible, the coalitional bargaining procedure results in approximately efficient contracting outcomes.

Conversely, in games where players' outside options depend on the behavior of other players, *all Markov perfect equilibria may be inefficient* (i.e., there exists a $\xi > 0$ such that $\sum \Phi_i < V - \xi$ in all equilibria and for all $\delta \geq \delta(\xi)$). We exhibit a three-player game where, in all equilibria, there exists an action stage where the probability of players exiting is bounded away from zero and, at the initial contracting stage, players have an incentive to reach the action stage where exit occurs with positive probability.

Efficiency in Games with Pure Outside Options

Inefficient outcomes arise in the bargaining game when players exit before the formation of the grand coalition.⁷ At the action phase, as players' exit choices are simultaneous, coordination failures may lead to inefficient equilibria. Consider the following simple two-player example.

Example 1 *There are two symmetric players. Each player has access to two actions: exiting (e) and remaining (r). The payoff matrix at the initial*

stage is:

	r	e	
r	$(0, 0)$	$(0, a)$	
e	$(a, 0)$	(a, a)	

and the total value of the coalition $\{1, 2\}$ is $V > 2a$

⁷As we consider situations where players' discount factors converge to 1, inefficiencies due to delay in the formation of the grand coalition become negligible.

Let ϕ^1 denote the common continuation value (at a symmetric equilibrium) of both players at the initial state. In the action phase, the game Γ played by the two players has a payoff matrix given by:

	r	e
r	$(\delta\phi^1, \delta\phi^1)$	$(\delta a, a)$
e	$(a, \delta a)$	(a, a)

It is easy to see that this game admits an inefficient pure strategy equilibrium where both players simultaneously exit. Notice that this is not the only equilibrium of the game for high values of the discount factor δ . If $\delta > 2a/V$, the game also admits an efficient symmetric pure strategic equilibrium where both players remain, and $\phi^1 = V/2$.

Example 1 illustrates in the simplest way the fact that coordination failures are unavoidable in a model where exit decisions are simultaneous. However, when the discount factor δ is high enough, the game also admits efficient equilibria where both players remain in the game with positive probability. Coordination failures at the action phase can easily result in inefficient equilibria at the contracting phase as well.⁸

Hence, in our search for efficient outcomes, we focus on equilibria without coordination failures at the action phase. We define an ε -R strategy profile as one where all players put a probability at least equal to ε of remaining in the game at every action stage. Formally, we define:

Definition 2 *For any $\varepsilon \in (0, 1)$, an ε -R strategy profile is a strategy profile where all players play a temporary action with probability at least equal to ε at any action phase, i.e. $\sum_{r_S \in R_S} \sigma_S^2(s)(r_S) \geq \varepsilon$ for any state s and any player $S \in \mathcal{N}(s)$. An ε -R Markov perfect equilibrium is an MPE in ε -R strategies.*

⁸To see this, add a third player to the game of example 1, and suppose that a coalition of two players obtains a payoff W when it exits, with $W > 3a, V > W + a$ and $W > 3V/4$. In this game, for $\delta \geq \max\{3a/W, 3(V - W)/W\}$, there exists an equilibrium where (i) players initially contract to form a two player coalition, (ii) after a two player coalition is formed, all players simultaneously exit, and (iii) at the initial action phase when all three players are present, all players remain in the game. This equilibrium results in the formation of the inefficient two-player coalition.

The class of ε -R equilibria defines a refinement of Markov perfect equilibria. This refinement is of interest because we show in Proposition 2 that when the discount factor is high enough, ε -R equilibria always exist in games with pure outside options. Moreover, in Proposition 3 we establish that all ε -R equilibria are Pareto efficient in games with pure outside options.⁹ Thus ε -R equilibria defines a non-empty class of efficient equilibria which is immune to coordination failures.¹⁰

Proposition 2 *For any underlying game v with pure outside options and any $1 > \varepsilon > 0$, there exists $\delta(\varepsilon)$ such that for all $\delta \geq \delta(\varepsilon)$, the bargaining game admits an ε -R Markov perfect equilibrium.*

Proposition 2 is a key result of our analysis. The intuition underlying the result follows. Consider the constrained coalitional bargaining game where all players are required to play ε -R strategies. By standard arguments, this game admits a Markov perfect equilibrium. We show that any equilibrium of the ε -constrained game is also an equilibrium of the original (unconstrained) coalitional bargaining game. Suppose by contradiction that the constraint were binding for one player. Exiting would then be a strict best response at some action phase, and the game would end up with early exit with probability at least $1 - \varepsilon > 0$. This results in an aggregate inefficiency for all the players. However, if the exiting player had instead chosen to stay, her short-term losses would be negligible (as δ is close to one), and her payoff in the next period would be strictly greater than her outside option. This last statement is true for two reasons. On the one hand, if the player were not chosen to propose next period, she would always be able to get her outside option (we use here the assumption that outside options are pure, so a player cannot be prevented from getting the same outside option next period.). On

⁹There may not be ε -R equilibria, even for pure outside option games, for low values of the discount factor. For example, the game analyzed in Example 1 does not admit any ε -R equilibrium for low values of δ .

¹⁰Preplay communication may be another reason for players avoiding coordination failures. Cooper et al. (1992) find that preplay communication can be quite effective in overcoming coordination failures

the other hand, if the player were to propose in the next contracting phase, she would be able to extract some of the aggregate efficiency loss, making her payoff strictly greater than her outside option. Hence remaining in the game must be a better response than exiting at the action phase, and any equilibrium of the ε -constrained game is also an equilibrium of the original game.

Note that this result depends crucially on the fact that outside options are pure. In games where outside options depend on the actions of the other players, a player may not be able to get the same payoff if she exits later in the game. Hence, as we will see in the example below, Proposition 2 does not extend to games where players' payoff upon exit depends on the behavior of other players.

Interestingly, taking ε converging to 1, Proposition 2 shows that, as δ converges to one, the bargaining game admits a Markov perfect equilibrium where the probability of exit at any action phase converges to zero. In fact, this result can be strengthened, as we can show that, as δ converges to 1, in *all* ε -R equilibria, the probability of exit of all the players at any action phase converges to zero. Furthermore, as the probability of remaining in the negotiations converges to one, the grand coalition will ultimately be formed in equilibrium, and the bargaining procedure results in an efficient outcome.

Proposition 3 *For any game with pure outside options, as δ converges to one, the probability of exit in any ε -R Markov perfect equilibrium converges to zero for all the players at all states, and the equilibrium outcome converges to an efficient outcome (i.e., for any $\xi > 0$ there exists a $\delta(\xi)$ such that $\sum \Phi_i > V - \xi$ for all $\delta \geq \delta(\xi)$).*

Propositions 2 and 3 thus show that, for games with pure outside options, as δ converges to 1, there exists a Markov perfect equilibrium resulting in an efficient outcome. We now show that these results are robust to the introduction of small external effects. When outside options are approximately pure, we can still show that ε -R Markov perfect equilibria exist for high discount factors. For δ close enough to one, this guarantees that the

game admits a Markov perfect equilibrium where players exit at the action phase with a probability close to zero, and the outcome of the bargaining procedure is approximately efficient. Formally:

Proposition 4 *Let $\max_{S, e_S, a_{-S}, a'_{-S}} |v(a_{-S}, e_S) - v(a'_{-S}, e_S)| = \eta(v)$. For any $1 > \varepsilon > 0$ there exists $\eta(\varepsilon) > 0$ and $\delta(\varepsilon)$ such that for all $\delta \geq \delta(\varepsilon)$, and all games satisfying $\eta(v) \leq \eta(\varepsilon)$, an ε -R Markov perfect equilibrium exists. Furthermore, for any $\xi > 0$ there exists $\eta(\varepsilon, \xi) > 0$ and $\delta(\varepsilon, \xi)$ such that all ε -R Markov perfect equilibria result in an outcome which is approximately Pareto efficient, i.e. $\sum \Phi_i \geq V - \xi$ for all $\delta \geq \delta(\varepsilon, \xi)$ and all games satisfying $\eta(v) \leq \eta(\varepsilon, \xi)$.*

Inefficiencies in Games without Pure Outside Options

We now provide an example to show that when players' outside options depend on the behavior of other players *all Markov perfect equilibria may be inefficient*. As all two-player games are efficient at the contracting stage,¹¹ this example involves three players.

Example 2 *There are three symmetric players with two actions r and e . At the initial stage (state s_1), when the players are singletons, payoff matrices are given by:*

	r	e	
r	$(0, 0, 0)$	$(0, 2, 0)$	
e	$(2, 0, 0)$	$(-1, -1, 0)$	
	r	e	

	r	e
r	$(0, 0, 2)$	$(0, -1, -1)$
e	$(-1, 0, -1)$	$(-1, -1, -1)$
	r	e

where player 1 chooses rows, player 2 chooses columns, and player 3 chooses matrices. If two players form a coalition (state s_2), the payoff matrices are given by

	r	e
r	$(0, 0)$	$(0, 9)$
e	$(2, 0)$	$(-1, -1)$

¹¹In two-player games, the sum of continuation values at the action stage is $\phi_1^2 + \phi_2^2 < V$. Thus, at the contracting phase, a proposer i always offer ϕ_{-i}^2 to form the grand coalition since its payoff is $V - \phi_{-i}^2 > \phi_i^2$, and the responder accepts the offer.

where player 1 (row) is the singleton player and player 2 (column) the two-player coalition. If the grand coalition forms, the total payoff is $V = 10$. All players have equal proposer probabilities and they are very patient (δ close to one).

In this example, after the exit decision of any player, the dominant strategy of remaining players is to play r and they have no incentives to form any further coalitions. Hence, as soon as one player has exited, equilibrium behavior is easily characterized, and we focus on those states where all players are still present in the game. Our goal is to show that there are no efficient equilibria. We prove this result in two steps, first analyzing the subgame in which a two-player coalition has formed (state s_2) and then the initial contracting stage of the three-player game (state s_1).

(i) Consider state s_2 where a two-player coalition has formed. The action stage admits a unique, inefficient, equilibrium where both players employ mixed strategies.¹² The equilibrium utilities and offers are given by the solution to the nonlinear system of equations:

$$\begin{aligned}\phi_1^1 &= \frac{10 - \phi_2^2 + \phi_1^2}{2}, \\ \phi_2^1 &= \frac{10 - \phi_1^2 + \phi_2^2}{2}, \\ \phi_1^2 &= \delta\sigma_2\phi_1^1 = 2\sigma_2 - (1 - \sigma_2), \\ \phi_2^2 &= \delta\sigma_1\phi_2^1 = 9\sigma_1 - (1 - \sigma_1)\end{aligned}$$

This system of equations admits a unique solution (continuous in δ) which converges to $\phi_1^2 = 0.54$ and $\phi_2^2 = 8.42$, $\sigma_1 = 0.94$, and $\sigma_2 = 0.51$, as δ

¹²Clearly simultaneous exit cannot be a Nash equilibrium of the game, and there cannot be equilibria where one player exits and the other one randomizes between staying and exiting. If both players choose to remain, their continuation value will be $\delta\phi_i^1$ and as $\phi_1^1 + \phi_2^1 \leq 10$, one of the players has an incentive to take her outside option. The strategy profiles (e, r) and (r, e) cannot be equilibria either. For example, if player 1 exits and player 2 remains, $\phi_1^2 = 2$ and $\phi_2^2 = 0$. Player 1 then has an incentive to remain, as she would obtain either her outside option (if the other player proposes next period) or the entire surplus V (if she proposes next period.) A similar argument shows that there is no equilibrium where one player remains and the other one randomizes between staying and exiting.

converges to 1. Note that the value of the two-player coalition is $\phi_2^2 > 8$ and that there is an efficiency loss as $\sum_{i=1}^2 \phi_i^2 < 9 < V = 10$.

(ii) Now consider state s_1 . We first establish that one of the players must have a continuation value at the action stage satisfying $\phi_i^2(s_1) > 2$. Suppose by contradiction that $\phi_i^2(s_1) \leq 2$ for all players i . At the contracting stage, by proposing to form a two-player coalition, a player will be able to obtain a payoff $\phi_2^2(s_2) - \phi_i^2(s_1) > 8 - 2 = 6$. Since every player is recognized to make an offer with probability $1/3$, we conclude that the continuation value at the contracting stage of state s_1 , $\phi_i^1(s_1)$ is bounded below by $1/3(\phi_2^2(s_2) - \phi_i^2(s_1)) > 2$. But this implies that, as δ converges to 1, in equilibrium, all players remain at the action stage of state s . If at least one of the other players exits, remaining is clearly a dominant strategy. If the two other players remain, remaining must be a best response, because for δ close enough to 1, $\delta\phi_i^1(s_1) > 2$ and the outside option has value 2. As all players remain at the action stage, we thus have $\phi_i^2(s_1) = \delta\phi_i^1(s_1)$ for all players. This last statement results in a contradiction because we assumed $\phi_i^2(s_1) \leq 2$ and we showed $\phi_i^1(s_1) > 2$.

Now, let i be a player with continuation value $\phi_i^2(s_1) > 2$. Then, in any equilibrium, players j and k must propose to form the two-player coalition $\{j, k\}$ at the contracting stage of state s_1 . This statement results from the fact that the marginal benefit of including player i in the contract ($V - \phi_2^2(s_2)$) is smaller than the minimal transfer that player i will accept to join the coalition, $\phi_i^2(s_1)$. Hence, at least in two thirds of the cases (when players j or k are chosen to make the initial offer), the equilibrium of the game results in the inefficient formation of a two-player coalition. This clearly implies that the initial values of the game satisfy $\sum \Phi_i < V$.

Example 2 is clearly robust to small perturbations in the payoff matrices. Furthermore, in the next Section, we provide an economic application (market entry with synergies) giving rise to a payoff structure which is equivalent to the payoff structure of Example 2. In the absence of a complete characterization of games resulting in inefficient outcomes, we note that the

example displays two crucial properties:

- (i) there exists an action stage where in equilibrium, the probability of exit of all players is bounded away from zero (for all $\delta \geq \bar{\delta}$);
- (ii) at the initial contracting stage, players have an incentive to reach the action stage where exit occurs with positive probability.

Property (i) highlights the difference between the case of pure outside options (where there always exist an equilibrium with all players remaining for δ close to 1) and general games. In our example, the outside option of a player crucially depends on the behavior of the other player. By exiting alone, both players obtain positive payoffs (of 2 or 9), but the outside options become negative when both players exit simultaneously. Hence, a player may choose to exit today, because by waiting one period, she might be unable to retain the same outside option. In games with two players and two actions, it can be checked that the structure of our example (a "game of chicken" where (e, e) gives lower payoffs than (r, r) , and the sum of the maximal outside options of the two players is greater than V) is the only structure for which all equilibria are inefficient.

Property (ii) can only be satisfied if the payoff of a two-player coalition is large with respect to the value of the grand coalition. A rapid look at the equations defining equilibrium at the action stage shows that the most favorable condition for ϕ_2^2 to be high is when the outside option of the two-player coalition is high and the outside option of the singleton is low. (In our example, the outside option of the two player coalition (9) is much higher than the outside option of the singleton player (2)). In other words, the formation of a two-player coalition must result in a large increase in the value of the outside option.

5 Applications

In this Section, we develop four applications of the model to economic problems. We study the Markov perfect equilibria of the bargaining game, and

we analyze the distribution of the surplus induced by the equilibria and the dynamics of coalition formation.

5.1 Multilateral Bargaining with Outside Options

Bilateral bargaining with outside options is a problem that has been widely studied (e.g., Shaked and Sutton (1984) and Sutton (1986)) and has been applied to a variety of economic problems (labor negotiations, marriage, contract theory, etc.). Yet little is known about its natural extension to an arbitrary number of players. We develop this extension in this section and show that the equilibrium exhibits some novel properties.

In the multilateral bargaining game with outside options there are n players who can collectively achieve a surplus V when the grand coalition forms. Each player is characterized by an outside option v_i . At the action stage each player can choose between remaining or exiting. If a player S exits, her outside option is given by $\sum_{i \in S} v_i$. In the Appendix, we obtain the following closed form solution for the ε -R Markov perfect equilibrium as δ converges to one.

Proposition 5 *The multilateral bargaining with outside options has the following Markov perfect equilibrium outcome:*

(i) *If $\bar{v} \geq \frac{1}{n}v$, where $\bar{v} = \max_{i=1, \dots, n} v_i$ is the largest outside option, the equilibrium payoffs converge to:*

$$\phi_i = v_i + \frac{(\bar{v} - v_i)}{\sum_{j=1}^n (\bar{v} - v_j)} \left(V - \sum_{j=1}^n v_j \right),$$

for all $i \in N$ and only the player with largest outside option opts out; the opt-out probability σ satisfies

$$\lim_{\delta \rightarrow 1} \frac{\sigma}{(1 - \delta)} = \frac{n\bar{v} - V}{V - \sum_{j=1}^n v_j},$$

(ii) *If $\bar{v} < \frac{1}{n}v$ the equilibrium payoffs converge to $\phi_i = \frac{1}{n}v$, for all $i \in N$ and no player opts out at the action stage.*

This equilibrium is a generalization of the equilibrium of Example 1, when players remain in the game with positive probability. It reflects the “outside options principle”: either outside options are binding and the player with the largest outside option receives her outside option, or they are not binding and the outcome of bargaining is unaffected by the outside options (see Sutton (1986)).

However, the equilibrium exhibits a novel property. The equilibrium payoff of all the players depend on the *entire* vector of outside options, including the smallest outside options. This result can easily be interpreted. In equilibrium, the player with the largest outside option randomizes between exiting and staying. Hence, if a player rejects the offer at the contracting stage, every player will obtain her outside option with positive probability. The equilibrium offer to any player i is thus a function of the entire vector of outside options, and is increasing in v_i .

The model puts forward testable empirical predictions that could be explored in experimental studies. The model has other comparative statics implications (besides the one that player’s payoff are increasing on their outside option). It also predicts that an increase in the highest outside option increases the sensitivity of a player’s payoff with respect to her own outside option, $\frac{\partial^2 \phi_i}{\partial \bar{v} \partial v_i} \geq 0$. Increasing the largest outside option \bar{v} , increases the probability of opting out, and the bargaining outcome becomes more sensitive to the outside options of all the players.

5.2 Contracting with Externalities

Segal (1999) analyzes a contracting model with externalities, in which a principal contracts with several agents. Players’ utilities depend on the trades (actions) chosen by the principal and the agents he has contracted with, so that agents excluded from the contract may suffer (or benefit from) externalities. Segal (1999) shows that this general structure encompasses a number of specific models, ranging from models in industrial organization (vertical contracting, exclusive dealing, network externalities, mergers to monopoly), to models in finance (debt restructuring, takeovers) or public

economics (the provision of public goods and bads). Our goal here is to analyze this principal-agent problem in a dynamic setting (Segal's (1999) model is static) and explore the role of outside options, or irreversibility of trades, in the allocation of gains and the efficiency of the outcome.

Specifically, trade among the principal and agent i is described by the action $a_i \in [0, \bar{a}]$, where $i = 1, \dots, n$. Externalities among agent's actions are captured by the following utility structure. Any agent i trading with the principal receives a payoff $a_i\alpha(A) + \beta(A)$, where A denotes aggregate trade, $A = \sum_{i=1}^n a_i$. If an agent does not trade with the principal, she chooses the no-trade action $a_i = 0$, and obtains a payoff $\beta(A)$. The principal's payoff is given by $F(A)$.¹³ Without loss of generality, all players no-trade payoffs are normalized to zero (i.e., $F(0) = \beta(0) = 0$).

Principal agent models can be divided into two broad categories, according to the sign of the externalities that traders impose on nontraders.

Definition 3 *Externalities on nontraders are positive (negative) if their payoff $\beta(A)$ is increasing (decreasing) in the aggregate trade $A = \sum a_i$.*

A dynamic version of the principal agent problem can be recast in the framework of this paper as follows. In any period of the game, at the contracting stage, the principal contracts with a coalition of agents S (like Segal (1999), we assume that agents cannot contract among themselves and that the principal has all the bargaining power). At the action stage, the principal and the agents who have already contracted, say S , may choose not to trade (a reversible action) or to trade (a permanent action). When coalition S trades (or exits) it chooses the trade A_S that maximizes its payoff, i.e. $v(S) = \max_A F(A) + A\alpha(A) + |S|\beta(A)$; the payoff received by agents outside coalition S when there is exit is thus $v_i(S) = \beta(A_S)$.

Interestingly, despite the existence of externalities, the underlying game is a pure outside option game because the aggregate payoff of principal and

¹³When agents are identical, this utility specification is equivalent to the linearity condition (condition L) proposed by Segal (1999, p. 341). Segal (1999) shows that this condition is satisfied in a variety of economic models.

agents who are contracting, $v(S)$, does not depend on actions of other non-trading agents. We now characterize a Markov perfect equilibrium for δ converging to one. When externalities on nontraders are positive, it is easy to see that the multilateral bargaining procedure immediately reaches an efficient agreement. By offering to form the grand coalition, and offering to each agent his minimal payoff (the no-trade value), the principal can extract the entire surplus. As the principal has all the bargaining power and agents' outside options are minimized with no trade, these offers constitute a subgame perfect equilibrium.¹⁴

When externalities on nontraders are negative, the structure of equilibrium is more complex. First notice that for all coalitions $S \subset T$,

$$\begin{aligned} v(S) &= F(A_S) + A_S\alpha(A_S) + |S|\beta(A_S) \\ &\geq F(A_T) + A_N\alpha(A_T) + |S|\beta(A_T) \\ &\geq F(A_T) + A_T\alpha(A_T) + |T|\beta(A_T) = v(T) \end{aligned}$$

where the first inequality is due to the fact that A_S is the optimal trade of a coalition S , and the second inequality is due to the fact that externalities are negative (because $\beta(0) = 0$, $\beta(A_T) \leq 0$).¹⁵ Hence, when externalities are negative, the principal obtains a higher payoff in a subcoalition S than in the grand coalition and her exit option $v(S)$ is greater than the total surplus V .

Therefore, after a coalition S is formed, it will require a positive transfer from all remaining agents to form the grand coalition. The coalition receives a transfer $\frac{v(S)-V}{|N|-|S|}$ per agent.¹⁶ Note that this transfer is an average of what the remaining agents get if the coalition trades, $v_i(S)$, and what they get if the coalition does not trade, 0 (the weights depend on the probabilities that the coalition chooses to exit or stay at the action stage).

¹⁴Segal (1999, p. 368) also notes that in games with positive externalities, efficient outcomes can easily be reached by having the principal make an offer conditional on unanimous acceptance.

¹⁵The normalization, $\beta(0) = 0$, implies that in games with positive (negative) externalities $\beta(A) > 0$ ($\beta(A) < 0$), whenever $A > 0$.

¹⁶The transfer made by each agent is the solution of $v(S) + x(|N| - |S|) = V$.

The coalition that forms in the first step is the one that can extract the highest transfer from agents after formed,

$$v^* = \max_S \frac{v(S) - V}{|N| - |S|}.$$

In the Appendix, we construct a Markov perfect equilibrium where the principal is able to extract a transfer v^* from all agents, and the grand coalition is formed in two steps. Summarizing our findings we have:

Proposition 6 *The principal agent problem has the following efficient Markov perfect equilibrium outcome:*

(i) *Positive externalities: the principal offers to form the grand coalition offering to each agent his minimal payoff (the no-trade value); all agents get the no-trade value and the principal extracts the entire surplus;*

(ii) *Negative externalities: the principal proposes to form a random coalition that maximizes $\frac{v(S)-V}{|N|-|S|}$, asking v^* for each agent receiving the offer. Then, the principal forms the grand coalition with the remaining agents, also asking v^* per agent, and when at the action stage exits the game with a positive probability, converging to 0 as δ converges to one.*

Hence, when externalities are negative, the principal has an incentive to contract with the agents in two steps. In the first step, the principal forms a coalition which generates maximum negative external effects on the remaining players. In the second step, the principal uses his credible outside option to extract high transfers from the agents (see also Genicot and Ray (2003)).¹⁷ On the other hand, in the positive externality case, contracting takes place in only one step.

5.3 Public Good Provision (Ray and Vohra, 2001)

Ray and Vohra (2001) analyze the formation of coalitions providing a pure public good. The leading illustration of their model is the formation of

¹⁷Genicot and Ray (2003) also consider the contracting problem among the principal and several agents (the negative externality case) using a different dynamic framework than ours. They also find that contracting will occur in several steps.

groups of countries deciding on abatement levels in international negotiations over transboundary pollution. They assume that each agent has a utility given by $v = Z - c(z)$, where Z is the total amount of public goods provided and z the quantity produced by the agent, with $c(\cdot)$ strictly increasing, strictly convex and $c'(0) = 0$. When a coalition S exits, it chooses its level of public good Z_S in order to maximize

$$Z_S - c\left(\frac{Z_S}{|S|}\right).$$

We restrict our analysis to a symmetric three-player game. Suppose that every player only has access to two strategies: remaining (r), resulting in a zero contribution to the public good, and exiting (e) where she contributes her optimal level of public good. As $c'(0) = 0$, every coalition will ultimately choose to exit and provide the public good. Hence, as δ converges to 1, the only relevant payoffs are the payoffs obtained by the three players when they exit as singletons (denoted a), the payoffs obtained when a two-player coalition and a singleton exit (denoted b for the two-player coalition and c for the singleton), and the total payoff V obtained by the grand coalition when it exits. Furthermore, as the optimal level of public good for coalition S is independent of the choices of the other players, and the cost function c is strictly convex, the game is strictly superadditive, i.e. $b > 2a$ and $V > b + c$.

It is easy to check that the ε -R equilibria of this game result in the formation of the grand coalition. Once a two-player coalition has formed, the game becomes equivalent to an asymmetric version of Example 1, and in an ε -R equilibrium either both players remain in the game (and obtain $V/2$ each), or the large player randomizes between exiting and staying, and obtains her outside option b (when $b \geq V/2$). Hence, either the grand coalition is formed immediately, or a two-player coalition forms, and negotiates with the remaining player to form the grand coalition. One can check that it is optimal to form the grand coalition immediately when the outside value of a partial coalition b is not too high; if this outside option is high, the grand coalition is formed in two steps, and members of the two-player coalition ob-

tain their outside option b . Formally, we obtain the following Proposition:

Proposition 7 *In the three player public good application, there exists a unique ε -R Markov perfect equilibrium, as δ converges to 1. This equilibrium give rise to the formation of the grand coalition. If $b \leq 2V/3$, the grand coalition is formed immediately; if $b > 2V/3$, the grand coalition is formed in two steps.*

It is instructive to contrast the result of Proposition 7 with the analysis of Ray and Vohra (2001), who use a different model of coalitional bargaining. In Ray and Vohra (2001)'s model, players make offers to form coalitions according to a fixed protocol. As coalitions exit the game immediately after they are formed, exit decisions are taken sequentially. In this model, it is easy to see that the procedure may end up in an inefficient equilibrium, where some players decide to leave early, in order to free-ride on the coalition formed by subsequent players. (More precisely, the first player may choose to exit, anticipating that the next two players form a coalition; this early exit decision is optimal whenever $c > V/3$). In our model, by contrast, exit decisions are taken simultaneously. If a player makes an unacceptable offer at the initial stage (or rejects the offer), all players simultaneously choose whether to exit at the action phase, resulting in a value less than $V/3$. Hence, players cannot commit to exit and free-ride on the coalitions formed by other players, and the equilibrium outcome is efficient. Finally, the dynamics of coalition formation reported in Proposition 7 is reminiscent of Seidmann and Winter (1998)'s results in games without externalities. Seidmann and Winter (1998) show that non-emptiness of the core is a necessary condition for the grand coalition to form immediately. If we interpret b as the value of a two-player coalition, non-emptiness of the core is equivalent to $b \leq 2V/3$. Hence, as in Seidmann and Winter (1998), but within a different model of coalitional bargaining, we observe that the grand coalition forms immediately when the worth of intermediate coalitions is small, and form gradually when the worth of intermediate coalitions becomes large.

5.4 Market Entry with Synergies

Suppose that three symmetric firms contemplate entering a market with fixed entry costs. By making a prior agreement, firms can benefit from synergies which will reduce their entry cost. Individual firms face an entry cost F , a coalition of two firms faces an entry cost G , with $G < F$ and the entry cost of the coalition of three firms is normalized to zero. If a single firm enters the market, it obtains a gross monopoly profit $1 > F$; if two or three firms enter the market simultaneously, price competition drives profits down to zero for all the firms which have entered the market. Obviously, the Pareto efficient outcome is for the grand coalition to form and enter the market.

We analyze this model by assuming that coalitions choose between two strategies remaining in the game (r) and exiting and entering the market (e). Clearly, once one firm has entered the market, the other firms should abstain from entering. Hence, as δ converges to 1, the payoff matrices of the game Γ played at the action phases converge to:

$$\begin{array}{c}
 \begin{array}{cc}
 & \begin{array}{c} r \\ e \end{array} \\
 \begin{array}{c} r \\ e \end{array} & \begin{array}{|c|c|}
 \hline
 (\phi, \phi, \phi) & (0, 1 - F, 0) \\
 \hline
 (1 - F, 0, 0) & (-F, -F, 0) \\
 \hline
 \end{array} \\
 & \begin{array}{c} r \\ e \end{array}
 \end{array}
 \quad
 \begin{array}{c}
 \begin{array}{cc}
 & \begin{array}{c} r \\ e \end{array} \\
 \begin{array}{c} r \\ e \end{array} & \begin{array}{|c|c|}
 \hline
 (0, 0, 1 - F) & (0, -F, -F) \\
 \hline
 (-F, 0, -F) & (-F, -F, -F) \\
 \hline
 \end{array} \\
 & \begin{array}{c} r \\ e \end{array}
 \end{array}
 \end{array}$$

where player 1 chooses rows, player 2 chooses columns, and player 3 chooses matrices, and ϕ denotes the continuation value of the game at the initial contracting phase.

If two players form a coalition, the payoff matrices are given by

$$\begin{array}{c}
 \begin{array}{cc}
 & \begin{array}{c} r \\ e \end{array} \\
 \begin{array}{c} r \\ e \end{array} & \begin{array}{|c|c|}
 \hline
 (\phi_1, \phi_2) & (0, 1 - G) \\
 \hline
 (1 - F, 0) & (-F, -G) \\
 \hline
 \end{array} \\
 & \begin{array}{c} r \\ e \end{array}
 \end{array}$$

where player 1 is the singleton player and player 2 the two-player coalition and ϕ_1 and ϕ_2 denote the continuation value at the contracting phase of the two players.

As long as $1 > F + G$, it is easy to see that the two-player game played after a two-player coalition has formed is equivalent to the two-player game of Example 2, and the only equilibrium at the action phase involves both players employing completely mixed strategies. Now assume that there is a large difference between the fixed costs of single firms and of coalitions of two firms ($F > 4/5$ and $G < 1/5$). In that case, the three-player symmetric game becomes equivalent to the game of Example 2. In the Appendix, we show that the Markov perfect equilibrium of the game results in the inefficient formation of a two-player coalition, which exits the game with positive probability at the action phase.

Proposition 8 *In the three-player model of market entry with synergies, as δ converges to 1, the Markov perfect equilibria of the game lead to the formation of a two-player coalition in the initial contracting stage, and firms inefficiently exit the game with positive probability at the action phase.*

Proposition 8 shows that inefficient outcomes arise not only in numerical examples, but also in significant economic models. Inefficiencies may also obtain in a larger class of models in Industrial Organization where firms decide whether to invest in a project and benefit from synergies by forming coalitions. A typical example of those situations are research joint ventures (RJV) which have been analyzed, among others, by Kamien et al. (1992) and d'Aspremont and Jacquemin (1988). If spillovers in R&D are low, R&D decisions are strategic substitutes and partial RJVs create significant value because they impose negative externalities on non-participants. Our results suggest that these two ingredients combined may lead to the formation of inefficient partial RJVs. On the other hand, if there are significant R&D spillovers then R&D decisions are strategic complements, and we expect the formation of a comprehensive RJV.

6 Conclusion

This paper proposes a coalitional bargaining model in which coalitions strategically interact and endogenously choose whether or not to exit. This formulation is general enough to study the formation of coalitions and the distribution of gains from cooperation in a wide variety of economic models with externalities and outside options. We show that when outside options are independent of the actions of other players, there exists Markov perfect equilibria (the class of MPE without coordination failures) which converge to efficient outcomes when the players become perfectly patient. On the other hand, in games with general outside options, all equilibria may be inefficient.

These results highlight the difference between our model and previous models of coalitional bargaining. In a setting with externalities, Ray and Vohra (1999) show that when players cannot renegotiate, the outcome of coalition formation is typically inefficient, as players have an incentive to leave the game before extracting all the surplus. On the contrary, Gomes (2001) establishes that when renegotiation occurs and players cannot choose to exit, the outcome is always efficient. Our study identifies a new type of friction – externalities on players’ endogenous outside options – that may lead to bargaining inefficiencies.

Appendix: Proofs

Proof of Proposition 1: We define a correspondence $F : \Phi \times \Phi \times \Sigma^1 \times \Sigma^2 \rightarrow \Phi \times \Phi \times \Sigma^1 \times \Sigma^2$ whose fixed points are the MPE. Φ is the set of continuation values $\phi = (\phi_S(s))$, which are bounded below by

$$\min\{v_S(a) : \text{for all states } s \text{ s.t. } S \in \mathcal{C}(s) \text{ and } a \in (A_T)_{T \in \mathcal{C}(s)}\},$$

where $\mathcal{C}(s) = \mathcal{N}(s) \cup \mathcal{E}(s)$. Furthermore, the sum $\sum_{S \in \mathcal{C}(s)} \phi_S(s)$ is bounded above

by V so Φ is a closed, convex interval of a finite-dimensional Euclidean space. Let Σ^1 be the set of proposers' strategies σ^1 at the contracting stage. Omitting the transfers (which are defined as the value of the coalition at the next action phase), $\sigma_S^1(s)$ is a probability distribution over the finite set $\{\mathcal{S} \subset \mathcal{N}(s) : S \in \mathcal{S}\}$. Let Σ^2 be the set of strategies σ^2 at the action stage. For any state s and any coalition $S \in \mathcal{N}(s)$, $\sigma_S^2(s)$ is a probability distribution over the finite set A_S . Both Σ^1 and Σ^2 are thus convex and compact subsets of a finite-dimensional Euclidean space.

The correspondence F is defined as follows. $(\varphi^1, \varphi^2, \mu^1, \mu^2) \in F(\phi^1, \phi^2, \sigma^1, \sigma^2)$ if and only if, for all states s and coalitions $S \in \mathcal{C}(s)$:

$$\begin{aligned} \varphi_S^1(s) &= q_S(s) \left(\sum_{\mathcal{S} \in \mathcal{S}} \sigma_S^1(s)(\mathcal{S}) (\phi_{\cup_{T \in \mathcal{S}} T}^2(g(c, s)) - \sum_{T \in \mathcal{S}} \phi_T^2(s)) \right) \\ &\quad + \sum_{T \in \mathcal{N}(s)} q_T(s) \sum_{\mathcal{S}} \sigma_T^1(s)(\mathcal{S}) (\mathbf{1}_{S \in \mathcal{S}} \phi_S^2(s) + \mathbf{1}_{S \notin \mathcal{S}} \phi_S^2(g(c, s))), \\ \varphi_S^2(s) &= u_S(s, \sigma^2)(\phi^1, \phi^2, \sigma^1, \sigma^2), \\ \text{supp}(\mu_S^1(s)) &\subset \arg \max_{\mathcal{S} \subset \mathcal{N}(s) \text{ s.t. } S \in \mathcal{S}} \left\{ (\phi_{\cup_{T \in \mathcal{S}} T}^2(g(c, s)) - \sum_{T \in \mathcal{S}} \phi_T^2(s)) \right\}, \\ \text{supp}(\mu_S^2(s)) &\subset \arg \max_{a_S \in A_S} \{u_S(s, a_S, \sigma_{-S}^2)(\phi^1)\}, \end{aligned}$$

where supp denotes the support of a probability distribution, and where, for any $\mu^2 \in \Sigma^2$,

$$u_S(s, \mu^2)(\phi^1) = \sum_{a=(a_T)_{T \in \mathcal{N}(s)}} \left(\prod_{T \in \mathcal{N}(s)} \mu_T^2(s)(a_T) \right) (\delta \phi_S^1(h(s, a)) + (1 - \delta) v_S(a, e(s))).$$

According to Proposition 1, the fixed points of F are MPE. To show that F has a fixed point we apply the Kakutani fixed point theorem. We have already noted that $Z = \Phi \times \Phi \times \Sigma^1 \times \Sigma^2$ is a compact and convex subset of a finite-dimensional Euclidean space, and $F(Z) \subset Z$. Furthermore, standard arguments show that $F(z)$ is a convex (and non-empty) set for all $z \in Z$, and that F has a closed graph. Thus the Kakutani fixed point theorem applies. Q.E.D.

Proof of Proposition 2: Suppose by contradiction that there exists an MPE of the constrained game, σ^k , with payoffs ϕ^k , and a sequence δ^k converging to one, such that σ^k is not an MPE of the original, game. Let s be a state where no coalitions have opted out and $S \in \mathcal{N}(s)$ a coalition for which the constraint is binding,

$$v_S := \max_{a_S \in E_S} v_S(a_S, \sigma_{-S}^2) > u_S^k(s, a_S, \sigma_{-S}^2) \text{ for all } a_S \in R_S, \quad (1)$$

so that $\sum_{a_S \in R_S} \sigma_S^2(s)(a_S) = \varepsilon$. Let K be the minimum aggregate efficiency loss when one coalition opts out. By assumption, $K > 0$. Since coalition S opts out with probability $(1 - \varepsilon)$, and, once S opts out, the aggregate payoff is $v_N(a^k) \leq V - K$, for all future action profiles a^k , $\phi_N^{2,k}(s) \leq V - (1 - \varepsilon)K$. (We denote the sum $\sum_{S \in \mathcal{C}(s)} v_S(a)$ by $v_N(a)$).

We now estimate the lowest payoff that coalition S can obtain in the ε -constrained game. She can guarantee for herself at least v_S by opting out, but in the ε -constrained game she can only opt with probability at most equal to $1 - \varepsilon$. The strategy of opting out of the game with probability $1 - \varepsilon$, and choosing x_S such that $\underline{v}_S = \min_{x_S \in R_S} \min_{x_{-S} \in X_{-S}} v_S(x_S, x_{-S})$ with probability ε at every action stage, and of not making any offers and rejecting any offers made at every contracting stage, yields coalition S at least

$$\underline{\phi}_S = \frac{\underline{v}_S(1 - \delta) + \delta(1 - \varepsilon)v_S}{1 - \delta\varepsilon},$$

which converges to v_S when δ converges to 1. (This formula comes from the evaluation of $E[\sum_{t=0}^{\infty} \delta^t(1 - \delta)v_S(a^t)]$). Thus $\phi_S^{i,k}(s) \geq \underline{\phi}_S$, for $i = 1, 2$.

In addition,

$$\begin{aligned} \phi_S^{1,k}(s) &\geq (1 - q_S(s))\underline{\phi}_S + q_S(s) \left(V - \sum_{T \in \mathcal{N}(s) \setminus S} \phi_T^{2,k}(s) \right) = \\ &= (1 - q_S(s))\underline{\phi}_S + q_S(s)\phi_S^{2,k}(s) + q_S(s) \left(V - \sum_{T \in \mathcal{N}(s)} \phi_T^{2,k}(s) \right), \end{aligned} \quad (2)$$

which implies $\phi_S^{1,k}(s) \geq \underline{\phi}_S + q_S(s)(1 - \varepsilon)K$. But coalition S 's payoff $u_S^k(s, a_S, \sigma_{-S}^2)$, for any $a_S \in R_S$, is at least equal to

$$\lambda \left(\delta \phi_S^{1,k}(s) + (1 - \delta)\underline{v}_S \right) + (1 - \lambda) \left(\delta \underline{\phi}_S + (1 - \delta)v_S \right), \quad (3)$$

where $\lambda \geq \varepsilon^{\mathcal{N}(s)-1}$ is the probability that all remaining $\mathcal{N}(s) \setminus S$ coalitions choose reversible actions. Combining our findings so far, we get

$$\begin{aligned} \liminf_{k \rightarrow \infty} u_S^k(s, a_S, \sigma_{-S}^2) &\geq \lambda(v_S + q_S(s)(1 - \varepsilon)K) + (1 - \lambda)v_S \\ &= v_S + \lambda \cdot q_S(s)(1 - \varepsilon)K > v_S \end{aligned}$$

which is in contradiction with inequality (1).

Q.E.D.

Proof of Proposition 3: We prove that as δ converges to one, all ε -R MPE converge to a Pareto efficient outcome. Assume by contradiction that there is a state s for which the statement is false. (In case there are multiple states for which the statement is false, choose one with the smallest number of active players). Then there is a subsequence δ_k converging to one satisfying $\phi_N^{2,k}(s) \leq V - K$, where $K > 0$. The payoff of any player $S \in \mathcal{N}(s)$ also satisfies inequality (2) thus $\phi_S^{1,k}(s) \geq v_S + q_S(s)K > v_S$. Since player S 's payoff from remaining in the game is greater than expression (3), for k large enough, it is greater than $v_S + \lambda \cdot q_S(s)K > v_S$. Thus in equilibrium no player opts out, and $\phi_S^{1,k}(s) = \phi_S^{2,k}(s)$.

Consider the players' strategies at the contracting stage of state s . Forming the grand coalition yields a strictly positive gain $V - \phi_N^{2,k}(s) \geq K > 0$. But then in all states $g(c, s)$, there are fewer active players than in state s , and thus by our initial assumption, $\phi_N^{2,k}(g(c, s)) \rightarrow V$. In addition, the aggregate payoff is equal to

$$\phi_N^{1,k}(s) = \sum_{C \in \mathcal{N}(s)} q_C(s) \left(\sum_S \sigma_C^1(s) \phi_N^{2,k}(g(c, s)) \right),$$

which implies that $\phi_N^{1,k}(s) = \phi_N^{2,k}(s) \rightarrow V$, resulting in a contradiction. It is clear that if the probability of early exit did not converge to zero, then the MPE could not converge to the Pareto efficient outcome. Moreover, since the probability of early exit converges to zero, then the equilibrium payoffs at both stages converge to the same value. Q.E.D.

Proof of Proposition 4: The structure of the proof is similar to the structure of the proofs of Proposition 2 and Proposition 3 and we only outline the steps that are different.

For all S , there exist v_S such that $\max_{e_S, a_{-S}} |v_S(e_S, a_{-S}) - v_S| \leq \eta/2$. Inequality (1) changes to

$$v_S + \eta/2 > \max_{a_S \in E_S} v_S(a_S, \sigma_{-S}^2) > u_S^k(s, a_S, \sigma_{-S}^2) \text{ for all } a_S \in R_S. \quad (4)$$

The same argument as in the proof of Proposition 2 shows that $\underline{\phi}_S \geq v_S - \eta/2$,

$$\liminf_{k \rightarrow \infty} \phi_S^{1,k}(s) \geq v_S - \eta/2 + q_S(s) (1 - \varepsilon) K,$$

and coalition S 's payoff $u_S^k(s, a_S, \sigma_{-S}^2)$, is at least equal to

$$\lambda (v_S - \eta/2 + q_S(s) (1 - \varepsilon) K) + (1 - \lambda) (v_S - \eta/2).$$

Combining the results, we get

$$\liminf_{k \rightarrow \infty} u_S^k(s, a_S, \sigma_{-S}^2) \geq v_S - \eta/2 + \lambda \cdot q_S(s) (1 - \varepsilon) K,$$

which is greater than $v_S + \eta/2$ for η small enough, resulting in a contradiction.

To show that the equilibrium is approximately efficient, an adaptation of the proof of Proposition 3 shows that equilibrium payoffs satisfy $\phi_S^{1,k}(s) \geq v_S - \frac{1}{2}\eta + q_S(s)K > v_S + \frac{1}{2}\eta$ for k large enough and η small enough. Hence, at the action phase, no player wants to opt out, and at the contracting phase, all players want to form some coalition. This implies that the equilibrium is approximately efficient. Q.E.D.

Proof of Proposition 5: We construct the equilibrium. At any state s where some players have opted out, the equilibrium strategy is for all active players to opt out. At any state s where no player has opted out, let S_1, \dots, S_m be the m active coalitions (indexed by j), and let S_1 be the coalition with the highest outside option (and suppose that there is a single coalition with the highest outside option).

We propose the following strategies. At the contracting stage, every player proposes to form the grand coalition, and to offer x_j to other coalitions, resulting in expected equilibrium payoffs ϕ_j . At the action stage, player S_1 opts out of the game with probability σ and the other players continue to negotiate. Let $v_N = \sum_i v_i$. The variables $\sigma(s)$, $x_i(s)$ and $\phi_i(s)$ are defined by the following equations :

If $v_1 \geq \frac{1}{m}V$ then

$$\begin{aligned} \sigma(s) &= (1 - \delta) \frac{mv_1 - \delta V}{\delta(\delta V - \delta v_N - v_1(1 - \delta))}, \\ \phi_j(s) &= \frac{v_1 + \frac{\sigma}{(1-\delta)}\delta^2 v_j}{\delta \left(1 + \delta \frac{\sigma}{(1-\delta)}\right)} \text{ and } x_j(s) = \phi_j(s) - \frac{(1 - \delta)v_1}{\delta} \text{ for } j = 2, \dots, m, \\ \phi_1(s) &= \frac{v_1}{\delta} \text{ and } x_1(s) = v_1, \end{aligned} \tag{5}$$

If $v_1 < \frac{1}{m}V$ then

$$\begin{aligned} \sigma(s) &= 0, \\ \phi_i(s) &= \frac{1}{m}V \text{ and } x_i(s) = \frac{1}{m}\delta V \text{ for } i = 1, \dots, m. \end{aligned} \tag{6}$$

We now show that this strategy profile forms a Markov perfect equilibrium. Consider any state where all players are active. If $v_1 \geq \frac{1}{m}V$, at the action stage, player 1 is indifferent between opting out and continuing, as $v_1 = \delta\phi_1$. For players $j = 2, \dots, m$,

$$\delta\phi_j - v_j = \frac{v_1 - v_j - \frac{\sigma}{(1-\delta)}\delta(1 - \delta)v_j}{\left(1 + \delta \frac{\sigma}{(1-\delta)}\right)}.$$

For δ close enough to 1, $\delta\phi_j - v_j > 0$, so no player wants to opt out. If now $v_1 < \frac{1}{m}V$, for all players $j = 1, 2, \dots, m$, $\delta\phi_j - v_j = \frac{\delta V}{m} - v_j > 0$ for δ large enough. So no player wants to opt out either.

Consider now the contracting stage. First suppose that $v_1 \geq \frac{1}{m}V$. If the grand coalition is formed, the offers must satisfy

$$\begin{aligned} x_j &= (1 - \sigma)\delta\phi_j + \sigma\delta v_j \text{ for } j = 2, \dots, n, \\ \phi_i &= \frac{1}{m}(V - x_N) + x_i, \\ x_1 &= v_1 = \delta\phi_1, \end{aligned} \tag{7}$$

Combining the last two equations,

$$\phi_1 - x_1 = \frac{(1 - \delta)v_1}{\delta} = \frac{1}{m}(V - x_N),$$

so

$$x_i = \phi_i - \frac{(1 - \delta)v_1}{\delta} \text{ for } i = 1, \dots, m,$$

Replacing the value of x_i in the first equation yields

$$\phi_j - \frac{(1 - \delta)v_1}{\delta} = (1 - \sigma)\delta\phi_j + \sigma\delta v_j,$$

whose unique solution is the ϕ_j given in the proposed strategy profile. Adding all equations for $j = 2, \dots, n$ results in

$$x_N - x_1 = (1 - \sigma)(\delta\phi_N - \delta\phi_1) + \sigma\delta(v_N - v_1),$$

and since $\phi_N = V$, $x_N = \phi_N - m\frac{(1-\delta)v_1}{\delta}$, $\delta\phi_1 = v_1$, and $x_1 = v_1$ we can solve for σ ,

$$\sigma = (1 - \delta) \frac{mv_1 - \delta V}{\delta(\delta V - \delta v_N - v_1(1 - \delta))},$$

as claimed. Notice that $\sigma \geq 0$ if and only if $\delta \geq \delta_0$ where $\delta_0 = \frac{v_1}{V - v_N + v_1} < 1$ because $V - v_N > 0$, and for δ close enough to 1, $\sigma \leq 1$.

Now suppose that $v_1 < \frac{1}{m}V$. If the grand coalition is formed,

$$\begin{aligned} x_i &= \delta\phi_i \text{ for all } i \\ \phi_i &= \frac{1}{m}(V - x_N) + x_i \end{aligned} \tag{8}$$

and it is straightforward to verify that the unique solution of the system of equations is given by the formula in the description of the strategy profile.

It remains to verify that no player wants to deviate by forming a subcoalition at the contracting stage. Consider a deviation by which some of the active players form a subcoalition $S \subset N$, and let ϕ'_j be the continuation value of players following the deviation. If $v_S \geq v_1$ then the payoff of coalition S converges to $\phi'_S = v_S$ for δ large enough. Now $v_S < \phi_S$ since $\phi_i \geq v_i$ with strict inequality for at least one $i \in S$. Hence, the deviation is not profitable. Similarly, if $v_S < v_1$, all players

$j \notin S \cup \{1\}$ benefit from the deviation, since their new payoff ϕ'_j is obtained by replacing m by $m - |S| + 1$ in the formula for equilibrium payoffs, and thus satisfy $\phi'_j > \phi_j$. Now, as $\sum_{j \in N} \phi'_j = \sum_{j \in N} \phi_j = V$ and $\phi'_1 = \phi_1$, players in S are better off not deviating.

Our analysis only deals with the case where there is a unique player with the highest outside value at any state. The result can be generalized to situations with multiple players with highest values as follows. Suppose that there are m players, $j = 1, \dots, m$, such that $v_j = \max_{i \in N} v_i$. Perturb the payoffs, by adding a random vector ε to all the payoffs, and construct the equilibrium for the perturbed game, where all values are different. As ε goes to zero, because equilibrium payoffs and strategies are upper hemi continuous in the parameters of the game, one can obtain limit equilibrium payoffs and strategies for the original game. Q.E.D.

Proof of Proposition 6: We give an explicit construction of the Markov perfect equilibrium. Consider any state s where the principal has contracted with a set S of agents. Due to the symmetry of the problem we associate to each coalition S its cardinal, $\#S = m$, and define $v(m)$, $v_i(m)$, $\phi^k(m)$ and $\phi_i^k(m)$. Let $x^*(m)$ be the unique solution of

$$x^*(m) = \arg \min_{m' \geq m} \left\{ \frac{v(n) - v(m')}{n - m'} \right\}$$

and

$$v_i^*(m) = \min_{m' \geq m} \left\{ \frac{v(n) - v(m')}{n - m'} \right\}$$

Consider the following strategies. At a subgame m where $x^*(m) = m$, the principal offers $\phi_i^2(m)$ to all the remaining agents, and the agents accept any offer greater than or equal to $\phi_i^2(m)$. At the action stage, the principal exits with a positive probability σ . The values σ and $\phi_i^2(m)$ are computed as solutions to the equations:

$$\begin{aligned} \phi^1(m) &= v(n) - (n - m) \phi_i^2(m) \\ \phi_i^1(m) &= \phi_i^2(m) \\ \phi^2(m) &= \delta \phi^1(m) = v(m) \\ \phi_i^2(m) &= (1 - \sigma) \delta \phi_i^1(m) + \sigma v_i(m) \end{aligned}$$

At a subgame m where $x^*(m) > m$, the principal offers to contract with $x^*(m) - m$ of the $n - m$ remaining agents (all agents are chosen with equal probability). She offers $\phi_i^2(m)$ to all the agents, and agents accept any offer greater than or equal to $\phi_i^2(m)$. At the action stage, the principal never exits. The value $\phi_i^2(m)$ is computed

as a solution to the equations:

$$\begin{aligned}
\phi^1(m) &= \phi^2(x^*(m)) - (x^*(m) - m) \phi_i^2(m) \\
\phi_i^1(m) &= \frac{(x^*(m) - m)}{n - m} \phi_i^2(m) + \frac{(n - x^*(m))}{n - m} \phi_i^2(x^*(m)) \\
\phi^2(m) &= \delta \phi^1(m) \\
\phi_i^2(m) &= \delta \phi_i^1(m)
\end{aligned}$$

Note that, as δ converges to 1, the equilibrium offers $\phi_i^2(m)$ converge to $\frac{v(n) - v(x^*(m))}{n - x^*(m)} = v_i^*(m)$ and $\frac{\sigma}{(1 - \delta)}$ converges to the positive value $\frac{v(m) - v(n)}{v(n) - v(m) - (n - m)v_i(m)}$.

To show that this strategy profile forms a subgame perfect equilibrium, we first consider subgames satisfying $x^*(m) = m$. By construction, the principal's exit decision at the action stage and the agents' responses at the contracting stage are optimal. It remains to check that the principal's offer at the contracting stage is optimal. Suppose by contradiction that the principal makes an acceptable offer to $m' < n$ agents. She would then receive a payoff $\phi^2(m') - (m' - m) \phi_i^2(m)$ instead of $v(n) - (n - m) \phi_i^2(m)$. Two cases must be distinguished. If $x^*(m') = m'$, then $\phi^2(m') = v(m')$. But because $x^*(m) = m$,

$$\phi_i^2(m) < \frac{v(n) - v(m')}{n - m'},$$

and hence

$$v(m') < v(n) - (n - m') \phi_i^2(m),$$

establishing that the deviation is unprofitable. If now $x^*(m') > m'$, in the continuation game, the principal proposes to form a coalition of size $x^*(m')$ and then moves to the grand coalition. Overall, she thus offers $v_i^*(m')$ to the remaining $(n - m')$ agents and $\phi^2(m') = v(n) - (n - m') v_i^*(m')$. But because $x^*(m) = m$, $v_i^*(m') > v_i^*(m)$ and hence,

$$v(n) - (n - m') v_i^*(m') - (m' - m) v_i^*(m) < v(n) - (n - m) v_i^*(m),$$

establishing that the deviation is unprofitable.

Consider now a subgame satisfying $x^*(m) > m$. We first show that, at the action stage, staying in the game is the optimal action of the principal. By exiting, the principal obtains a payoff of $v(m)$ and by staying a payoff of $\phi(m) = v(n) - (n - m) v_i^*(m)$. As $x^*(m) \neq m$,

$$v_i^*(m) < \frac{v(n) - v(m)}{n - m},$$

so that the optimal strategy is to choose a temporary action. At the contracting stage, the agents' response is optimal by construction, and by an argument similar to the argument in the case $x^*(m) = m$, the principal has no incentive to offer to

form a coalition of size $m' \neq x^*(m)$.

Q.E.D.

Proof of Proposition 7: We construct the payoff matrices of the game Γ played at the action phases when δ converges to 1. It is easy to check that, once a player has exited the game, the optimal choice of the two remaining players is to exit as a two-player coalition, and the expected payoff of each of the remaining players is equal to $b/2$. Hence, the payoff matrices are given by:

$$\begin{array}{c}
 \begin{array}{cc}
 & r & e \\
 r & \boxed{(\phi, \phi, \phi)} & \boxed{(b/2, c, b/2)} \\
 e & \boxed{(c, b/2, b/2)} & \boxed{(a, a, a)}
 \end{array}
 &
 \begin{array}{cc}
 & r & e \\
 r & \boxed{(b/2, b/2, c)} & \boxed{(a, a, a)} \\
 e & \boxed{(a, a, a)} & \boxed{(a, a, a)}
 \end{array}
 \end{array}$$

where ϕ denotes the continuation value of the game at the initial contracting phase.

If two players form a coalition, the payoff matrices are given by

$$\begin{array}{cc}
 & r & e \\
 r & \boxed{(\phi_1, \phi_2)} & \boxed{(c, b)} \\
 e & \boxed{(c, b)} & \boxed{(c, b)}
 \end{array}$$

where player 1 is the singleton player and player 2 the two-player coalition and ϕ_1 and ϕ_2 denote the continuation value at the contracting phase of the two players.

Once the two-player coalition has formed, the two-player game corresponds to an asymmetric version of Example 1, and as $V > c+b$, we can easily characterize the ε -R equilibria for δ converging to 1. If $V/2 > \max\{c, b\}$, the game admits a unique ε -R equilibrium where both players remain and $\phi_1 = \phi_2 = V/2$. If $V/2 \leq \max\{c, b\}$, the game admits a unique ε -R equilibrium where the player with the largest option randomizes between staying and exiting, and the player with the lowest outside option remains in the game. The probability that the player with the largest option remains in the game converges to 1 as δ converges to 1. Supposing (without loss of generality) that $c \geq b$, the payoffs converge to $\phi_1 = c, \phi_2 = V - c > b$.

We now consider the symmetric ε -R equilibria of the game at the initial phase, where the three players are singletons. Consider first the action stage. If $V/3 > c$, there exists an equilibrium where all players remain and $\phi = V/3$. If $V/3 < c$, the symmetric ε -R equilibrium involves all players choosing a common probability σ of remaining in the game, where σ satisfies:

$$\sigma^2 V/3 + \sigma(1 - \sigma)b = \sigma^2 c + 2\sigma(1 - \sigma)a.$$

Notice that, in both cases, the continuation value of players at the action stage satisfy $\phi^2 \leq V/3$.

Now, consider the initial contracting stage. Suppose first that $b \leq 2V/3$. In that case, we claim that the grand coalition is formed immediately. By forming a two player coalition, the proposer gets at most: $b - \phi^2$ whereas she would get $V - 2\phi^2$ if she proposed to form the grand coalition immediately. As $b \leq 2V/3$

and $\phi^2 \leq V/3, b - x \leq V - 2x$. If now $b > 2V/3$, we claim that the coalition is formed in two steps. As $b > 2V/3, c < V/3$ and hence $\phi^2 = V/3$. But then, $V - 2\phi^2 = V/3 < b - \phi^2$, and at the initial contracting stage, the proposer has an incentive to form a two-player coalition. Q.E.D.

Proof of Proposition 8: Consider the action stage after two players have formed a coalition. The only equilibrium of the game is a completely mixed strategy profile (σ_1, σ_2) satisfying the following equations (the notations are similar to those of Example 2),

$$\begin{aligned} x_1 &= (1 - \sigma_2)\phi_1 = (1 - \sigma_2) - F, \\ x_2 &= (1 - \sigma_1)\phi_2 = (1 - \sigma_1) - G, \\ \phi_1 &= \frac{1}{2}(1 - x_2 + x_1), \\ \phi_2 &= \frac{1}{2}(1 - x_1 + x_2). \end{aligned}$$

Solving these equations we obtain:

$$\begin{aligned} \phi_1 &= 1 - t, & \phi_2 &= t \\ \sigma_1 &= \frac{(t-F)(1-t)}{t^2}, & \sigma_2 &= \frac{t-F}{t} \\ x_1 &= \frac{F(1-t)}{t}, & x_2 &= t - \frac{(t-F)(1-t)}{t} \end{aligned} \quad (9)$$

where t is a solution of $f(t) = 2t^3 + (-3 - F + G)t^2 + (2F + 1)t - F = 0$. Note that because $F + G < 1$,

$$f(F) = -F^2(1 - G - F) < 0 \text{ and } f(1 - G) = G^2(1 - G - F) > 0,$$

so that a solution $t \in (F, 1 - G)$ exists.

Now consider the initial stage where no coalition has been formed. We will show that it is a weakly dominant strategy for every firm to stay. By staying, a firm obtains either $\delta\phi$ if no other firm exits, or 0 if another firm exits. By exiting, the firm either gets $1 - F$ if no other firm enters the market, or 0 otherwise. We want to show:

$$\delta\phi \geq 1 - F. \quad (10)$$

We consider only symmetric equilibria. If players propose to form the grand coalition at the contracting stage, $\phi = 1/3$ and, as δ converges to 1 and $F > 4/5$, $\delta\phi \geq 1 - F$. If players propose to form a two-player coalition with equal probability of choosing any of the two other firms, and with x the continuation value at the action stage of the initial state,

$$\phi = \frac{1}{3}(x_2 - x) + \frac{1}{3}x + \frac{1}{3}x_1 = \frac{x_2 + x_1}{3} \quad (11)$$

The solution (9) implies that inequality (10) is equivalent to

$$h(t) = 2F + Ft + 2t^2 - 4t \geq 0.$$

This inequality holds for all $F \geq 4/5$ because the quadratic expression $h(\cdot)$ satisfies $h(F) = F(3F - 2) > 0$ and $h'(F) = 5F - 4 \geq 0$.

Finally, we check that it is an optimal strategy for a firm to form a coalition with one of the two other firms at the initial contracting stage. By forming the grand coalition, each firm obtains a payoff $1 - 2\delta\phi$. By forming a coalition of size 2 it obtains $x_2 - \delta\phi$. Hence, we need to establish that

$$x_2 + \phi \geq 1,$$

which is equivalent to $g(t) = 8t^2 - (5F + 7)t + 5F \geq 0$. This inequality holds for all $F \in (2/3, 1)$ because the quadratic expression $g(\cdot)$ satisfies $g(F) = F(3F - 2) > 0$ and $g'(F) = F(16 - 5F) > 0$. Q.E.D.

References

- Bloch, F. (1996) "Sequential Formation of Coalitions in Games with Externalities and Fixed Payoff Division," *Games and Economics Behavior* **14**, 90-123.
- Chatterjee, K. , B. Dutta, D. Ray and K. Sengupta (1993) "A Noncooperative Theory of Coalitional Bargaining," *Review of Economic Studies* **60**, 463-477.
- Cooper, R., D. DeJong, R. Forsythe and T. Ross (1992) "Communication in Coordination Games," *Quarterly Journal of Economics*, **107**, 739-71.
- D'Aspremont, C. and A. Jacquemin (1988) "Cooperative and Noncooperative R&D in Duopoly with Spillovers," *American Economic Review* **78**, 1133-1137.
- Genicot, G. and D. Ray (2003) "Contracts and Externalities: How Things Fall Apart," mimeo, New York University.
- Gomes, A. (2001) "Multilateral Contracting with Externalities," mimeo, The Wharton School, University of Pennsylvania.
- Gomes, A. and P. Jehiel (2002) "Dynamic Processes of Social and Economic Interactions: On the Persistency of Inefficiencies," mimeo, The Wharton School, University of Pennsylvania.
- Gul, F. (1989) "Bargaining Foundations of Shapley Value," *Econometrica*, **57**, 81-95.
- Kamien, M., E. Muller, and I. Zang (1992) "Research Joint Ventures and R&D Cartels," *American Economic Review* **82**, 1293-1306.
- Konishi, H., and D. Ray (2003), "Coalition Formation as a Dynamic Process," *Journal of Economic Theory*.**110**, 1-41.
- Maskin, E., (2003), "Bargaining, Coalitions, and Externalities," mimeo, Institute for Advanced Studies.
- Montero, M. (1999) "Coalition Formation in Games with Externalities," *CentER Discussion Paper*, 99121.
- Okada, A. (1996) "A Noncooperative Coalitional Bargaining Game with Random Proposers," *Games and Economic Behavior*, **16**, 97-108.

- Perry, M. and P. Reny (1994) "A Noncooperative View of Coalition Formation and the Core," *Econometrica* **62**, 795-817.
- Ray, D. and R. Vohra (1999) "A Theory of Endogenous Coalition Structures," *Games and Economic Behavior* **26**, 286-336.
- Ray, D. and R. Vohra (2001) "Coalitional Power and Public Goods," *Journal of Political Economy* **109**, 1355-1384.
- Rubinstein, A. (1982) "Perfect Equilibrium in a Bargaining Model," *Econometrica* **50**, 97-108.
- Segal, I. (1999) "Contracting with Externalities," *Quarterly Journal of Economics* **114**, 337-388.
- Seidmann, D. and E. Winter (1998) "A Theory of Gradual Coalition Formation," *Review of Economic Studies* **65**, 793-815.
- Shaked, A. and J. Sutton (1984) "Involuntary Unemployment as a Perfect Equilibrium in a Bargaining Model," *Econometrica* **52**, 1351-1364.
- Sutton, J. (1986) "Noncooperative Bargaining Theory: An Introduction," *Review of Economic Studies* **53**, 709-724.

NOTE DI LAVORO DELLA FONDAZIONE ENI ENRICO MATTEI

Fondazione Eni Enrico Mattei Working Paper Series

Our Note di Lavoro are available on the Internet at the following addresses:

<http://www.feem.it/Feem/Pub/Publications/WPapers/default.html>

<http://www.ssrn.com/link/feem.html>

NOTE DI LAVORO PUBLISHED IN 2003

PRIV	1.2003	<i>Gabriella CHIESA and Giovanna NICODANO</i> : <u>Privatization and Financial Market Development: Theoretical Issues</u>
PRIV	2.2003	<i>Ibolya SCHINDELE</i> : <u>Theory of Privatization in Eastern Europe: Literature Review</u>
PRIV	3.2003	<i>Wietze LISE, Claudia KEMFERT and Richard S.J. TOL</i> : <u>Strategic Action in the Liberalised German Electricity Market</u>
CLIM	4.2003	<i>Laura MARSILIANI and Thomas I. RENSTRÖM</i> : <u>Environmental Policy and Capital Movements: The Role of Government Commitment</u>
KNOW	5.2003	<i>Reyer GERLAGH</i> : <u>Induced Technological Change under Technological Competition</u>
ETA	6.2003	<i>Efrem CASTELNUOVO</i> : <u>Squeezing the Interest Rate Smoothing Weight with a Hybrid Expectations Model</u>
SIEV	7.2003	<i>Anna ALBERINI, Alberto LONGO, Stefania TONIN, Francesco TROMBETTA and Margherita TURVANI</i> : <u>The Role of Liability, Regulation and Economic Incentives in Brownfield Remediation and Redevelopment: Evidence from Surveys of Developers</u>
NRM	8.2003	<i>Elissaios POPYRAKIS and Reyner GERLAGH</i> : <u>Natural Resources: A Blessing or a Curse?</u>
CLIM	9.2003	<i>A. CAPARRÓS, J.-C. PEREAU and T. TAZDAÏT</i> : <u>North-South Climate Change Negotiations: a Sequential Game with Asymmetric Information</u>
KNOW	10.2003	<i>Giorgio BRUNELLO and Daniele CHECCHI</i> : <u>School Quality and Family Background in Italy</u>
CLIM	11.2003	<i>Efrem CASTELNUOVO and Marzio GALEOTTI</i> : <u>Learning By Doing vs Learning By Researching in a Model of Climate Change Policy Analysis</u>
KNOW	12.2003	<i>Carole MAIGNAN, Gianmarco OTTAVIANO and Dino PINELLI (eds.)</i> : <u>Economic Growth, Innovation, Cultural Diversity: What are we all talking about? A critical survey of the state-of-the-art</u>
KNOW	13.2003	<i>Carole MAIGNAN, Gianmarco OTTAVIANO, Dino PINELLI and Francesco RULLANI (lix)</i> : <u>Bio-Ecological Diversity vs. Socio-Economic Diversity. A Comparison of Existing Measures</u>
KNOW	14.2003	<i>Maddy JANSSENS and Chris STEYAERT (lix)</i> : <u>Theories of Diversity within Organisation Studies: Debates and Future Trajectories</u>
KNOW	15.2003	<i>Tuzin BAYCAN LEVENT, Enno MASUREL and Peter NIJKAMP (lix)</i> : <u>Diversity in Entrepreneurship: Ethnic and Female Roles in Urban Economic Life</u>
KNOW	16.2003	<i>Alexandra BITUSIKOVA (lix)</i> : <u>Post-Communist City on its Way from Grey to Colourful: The Case Study from Slovakia</u>
KNOW	17.2003	<i>Billy E. VAUGHN and Katarina MLEKOV (lix)</i> : <u>A Stage Model of Developing an Inclusive Community</u>
KNOW	18.2003	<i>Selma van LONDEN and Arie de RUIJTER (lix)</i> : <u>Managing Diversity in a Globalizing World</u>
Coalition		
Theory	19.2003	<i>Sergio CURRARINI</i> : <u>On the Stability of Hierarchies in Games with Externalities</u>
Network		
PRIV	20.2003	<i>Giacomo CALZOLARI and Alessandro PAVAN (lx)</i> : <u>Monopoly with Resale</u>
PRIV	21.2003	<i>Claudio MEZZETTI (lx)</i> : <u>Auction Design with Interdependent Valuations: The Generalized Revelation Principle, Efficiency, Full Surplus Extraction and Information Acquisition</u>
PRIV	22.2003	<i>Marco LiCalzi and Alessandro PAVAN (lx)</i> : <u>Tilting the Supply Schedule to Enhance Competition in Uniform-Price Auctions</u>
PRIV	23.2003	<i>David ETTINGER (lx)</i> : <u>Bidding among Friends and Enemies</u>
PRIV	24.2003	<i>Hannu VARTIAINEN (lx)</i> : <u>Auction Design without Commitment</u>
PRIV	25.2003	<i>Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx)</i> : <u>Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions</u>
PRIV	26.2003	<i>Christine A. PARLOUR and Uday RAJAN (lx)</i> : <u>Rationing in IPOs</u>
PRIV	27.2003	<i>Kjell G. NYBORG and Ilya A. STREBULAIEV (lx)</i> : <u>Multiple Unit Auctions and Short Squeezes</u>
PRIV	28.2003	<i>Anders LUNANDER and Jan-Eric NILSSON (lx)</i> : <u>Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts</u>
PRIV	29.2003	<i>TangaMcDANIEL and Karsten NEUHOFF (lx)</i> : <u>Use of Long-term Auctions for Network Investment</u>
PRIV	30.2003	<i>Emiel MAASLAND and Sander ONDERSTAL (lx)</i> : <u>Auctions with Financial Externalities</u>
ETA	31.2003	<i>Michael FINUS and Bianca RUNDSHAGEN</i> : <u>A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games</u>
KNOW	32.2003	<i>Michele MORETTO</i> : <u>Competition and Irreversible Investments under Uncertainty</u>
PRIV	33.2003	<i>Philippe QUIRION</i> : <u>Relative Quotas: Correct Answer to Uncertainty or Case of Regulatory Capture?</u>
KNOW	34.2003	<i>Giuseppe MEDA, Claudio PIGA and Donald SIEGEL</i> : <u>On the Relationship between R&D and Productivity: A Treatment Effect Analysis</u>
ETA	35.2003	<i>Alessandra DEL BOCA, Marzio GALEOTTI and Paola ROTA</i> : <u>Non-convexities in the Adjustment of Different Capital Inputs: A Firm-level Investigation</u>

GG	36.2003	<i>Matthieu GLACHANT</i> : <u>Voluntary Agreements under Endogenous Legislative Threats</u>
PRIV	37.2003	<i>Narjess BOUBAKRI, Jean-Claude COSSET and Omrane GUEDHAMI</i> : <u>Postprivatization Corporate Governance: the Role of Ownership Structure and Investor Protection</u>
CLIM	38.2003	<i>Rolf GOLOMBEK and Michael HOEL</i> : <u>Climate Policy under Technology Spillovers</u>
KNOW	39.2003	<i>Slim BEN YOUSSEF</i> : <u>Transboundary Pollution, R&D Spillovers and International Trade</u>
CTN	40.2003	<i>Carlo CARRARO and Carmen MARCHIORI</i> : <u>Endogenous Strategic Issue Linkage in International Negotiations</u>
KNOW	41.2003	<i>Sonia OREFFICE</i> : <u>Abortion and Female Power in the Household: Evidence from Labor Supply</u>
KNOW	42.2003	<i>Timo GOESCHL and Timothy SWANSON</i> : <u>On Biology and Technology: The Economics of Managing Biotechnologies</u>
ETA	43.2003	<i>Giorgio Busetti and Matteo MANERA</i> : <u>STAR-GARCH Models for Stock Market Interactions in the Pacific Basin Region, Japan and US</u>
CLIM	44.2003	<i>Katrin MILLOCK and Céline NAUGES</i> : <u>The French Tax on Air Pollution: Some Preliminary Results on its Effectiveness</u>
PRIV	45.2003	<i>Bernardo BORTOLOTTI and Paolo PINOTTI</i> : <u>The Political Economy of Privatization</u>
SIEV	46.2003	<i>Elbert DIJKGRAAF and Herman R.J. VOLLEBERGH</i> : <u>Burn or Bury? A Social Cost Comparison of Final Waste Disposal Methods</u>
ETA	47.2003	<i>Jens HORBACH</i> : <u>Employment and Innovations in the Environmental Sector: Determinants and Econometrical Results for Germany</u>
CLIM	48.2003	<i>Lori SNYDER, Nolan MILLER and Robert STAVINS</i> : <u>The Effects of Environmental Regulation on Technology Diffusion: The Case of Chlorine Manufacturing</u>
CLIM	49.2003	<i>Lori SNYDER, Robert STAVINS and Alexander F. WAGNER</i> : <u>Private Options to Use Public Goods. Exploiting Revealed Preferences to Estimate Environmental Benefits</u>
CTN	50.2003	<i>László Á. KÓCZY and Luc LAUWERS</i> (Ixi): <u>The Minimal Dominant Set is a Non-Empty Core-Extension</u>
CTN	51.2003	<i>Matthew O. JACKSON</i> (Ixi): <u>Allocation Rules for Network Games</u>
CTN	52.2003	<i>Ana MAULEON and Vincent VANNETELBOSCH</i> (Ixi): <u>Farsightedness and Cautiousness in Coalition Formation</u>
CTN	53.2003	<i>Fernando VEGA-REDONDO</i> (Ixi): <u>Building Up Social Capital in a Changing World: a network approach</u>
CTN	54.2003	<i>Matthew HAAG and Roger LAGUNOFF</i> (Ixi): <u>On the Size and Structure of Group Cooperation</u>
CTN	55.2003	<i>Taiji FURUSAWA and Hideo KONISHI</i> (Ixi): <u>Free Trade Networks</u>
CTN	56.2003	<i>Halis Murat YILDIZ</i> (Ixi): <u>National Versus International Mergers and Trade Liberalization</u>
CTN	57.2003	<i>Santiago RUBIO and Alistair ULPH</i> (Ixi): <u>An Infinite-Horizon Model of Dynamic Membership of International Environmental Agreements</u>
KNOW	58.2003	<i>Carole MAIGNAN, Dino PINELLI and Gianmarco I.P. OTTAVIANO</i> : <u>ICT, Clusters and Regional Cohesion: A Summary of Theoretical and Empirical Research</u>
KNOW	59.2003	<i>Giorgio BELLETTINI and Gianmarco I.P. OTTAVIANO</i> : <u>Special Interests and Technological Change</u>
ETA	60.2003	<i>Ronnie SCHÖB</i> : <u>The Double Dividend Hypothesis of Environmental Taxes: A Survey</u>
CLIM	61.2003	<i>Michael FINUS, Ekko van IERLAND and Robert DELLINK</i> : <u>Stability of Climate Coalitions in a Cartel Formation Game</u>
GG	62.2003	<i>Michael FINUS and Bianca RUNDSHAGEN</i> : <u>How the Rules of Coalition Formation Affect Stability of International Environmental Agreements</u>
SIEV	63.2003	<i>Alberto PETRUCCI</i> : <u>Taxing Land Rent in an Open Economy</u>
CLIM	64.2003	<i>Joseph E. ALDY, Scott BARRETT and Robert N. STAVINS</i> : <u>Thirteen Plus One: A Comparison of Global Climate Policy Architectures</u>
SIEV	65.2003	<i>Edi DEFRANCESCO</i> : <u>The Beginning of Organic Fish Farming in Italy</u>
SIEV	66.2003	<i>Klaus CONRAD</i> : <u>Price Competition and Product Differentiation when Consumers Care for the Environment</u>
SIEV	67.2003	<i>Paulo A.L.D. NUNES, Luca ROSSETTO, Arianne DE BLAEIJ</i> : <u>Monetary Value Assessment of Clam Fishing Management Practices in the Venice Lagoon: Results from a Stated Choice Exercise</u>
CLIM	68.2003	<i>ZhongXiang ZHANG</i> : <u>Open Trade with the U.S. Without Compromising Canada's Ability to Comply with its Kyoto Target</u>
KNOW	69.2003	<i>David FRANTZ</i> (Iix): <u>Lorenzo Market between Diversity and Mutation</u>
KNOW	70.2003	<i>Ercole SORI</i> (Iix): <u>Mapping Diversity in Social History</u>
KNOW	71.2003	<i>Ljiljana DERU SIMIC</i> (Ixi): <u>What is Specific about Art/Cultural Projects?</u>
KNOW	72.2003	<i>Natalya V. TARANOVA</i> (Ixi): <u>The Role of the City in Fostering Intergroup Communication in a Multicultural Environment: Saint-Petersburg's Case</u>
KNOW	73.2003	<i>Kristine CRANE</i> (Ixi): <u>The City as an Arena for the Expression of Multiple Identities in the Age of Globalisation and Migration</u>
KNOW	74.2003	<i>Kazuma MATOBA</i> (Ixi): <u>Glocal Dialogue- Transformation through Transcultural Communication</u>
KNOW	75.2003	<i>Catarina REIS OLIVEIRA</i> (Ixi): <u>Immigrants' Entrepreneurial Opportunities: The Case of the Chinese in Portugal</u>
KNOW	76.2003	<i>Sandra WALLMAN</i> (Ixi): <u>The Diversity of Diversity - towards a typology of urban systems</u>
KNOW	77.2003	<i>Richard PEARCE</i> (Ixi): <u>A Biologist's View of Individual Cultural Identity for the Study of Cities</u>
KNOW	78.2003	<i>Vincent MERK</i> (Ixi): <u>Communication Across Cultures: from Cultural Awareness to Reconciliation of the Dilemmas</u>
KNOW	79.2003	<i>Giorgio BELLETTINI, Carlotta BERTI CERONI and Gianmarco I.P. OTTAVIANO</i> : <u>Child Labor and Resistance to Change</u>
ETA	80.2003	<i>Michele MORETTO, Paolo M. PANTEGHINI and Carlo SCARPA</i> : <u>Investment Size and Firm's Value under Profit Sharing Regulation</u>

IEM	81.2003	<i>Alessandro LANZA, Matteo MANERA and Massimo GIOVANNINI: <u>Oil and Product Dynamics in International Petroleum Markets</u></i>
CLIM	82.2003	<i>Y. Hossein FARZIN and Jinhua ZHAO: <u>Pollution Abatement Investment When Firms Lobby Against Environmental Regulation</u></i>
CLIM	83.2003	<i>Giuseppe DI VITA: <u>Is the Discount Rate Relevant in Explaining the Environmental Kuznets Curve?</u></i>
CLIM	84.2003	<i>Reyer GERLAGH and Wietze LISE: <u>Induced Technological Change Under Carbon Taxes</u></i>
NRM	85.2003	<i>Rinaldo BRAU, Alessandro LANZA and Francesco PIGLIARU: <u>How Fast are the Tourism Countries Growing? The cross-country evidence</u></i>
KNOW	86.2003	<i>Elena BELLINI, Gianmarco I.P. OTTAVIANO and Dino PINELLI: <u>The ICT Revolution: opportunities and risks for the Mezzogiorno</u></i>
SIEV	87.2003	<i>Lucas BRETSCGHER and Sjak SMULDERS: <u>Sustainability and Substitution of Exhaustible Natural Resources. How resource prices affect long-term R&D investments</u></i>
CLIM	88.2003	<i>Johan EYCKMANS and Michael FINUS: <u>New Roads to International Environmental Agreements: The Case of Global Warming</u></i>
CLIM	89.2003	<i>Marzio GALEOTTI: <u>Economic Development and Environmental Protection</u></i>
CLIM	90.2003	<i>Marzio GALEOTTI: <u>Environment and Economic Growth: Is Technical Change the Key to Decoupling?</u></i>
CLIM	91.2003	<i>Marzio GALEOTTI and Barbara BUCHNER: <u>Climate Policy and Economic Growth in Developing Countries</u></i>
IEM	92.2003	<i>A. MARKANDYA, A. GOLUB and E. STRUKOVA: <u>The Influence of Climate Change Considerations on Energy Policy: The Case of Russia</u></i>
ETA	93.2003	<i>Andrea BELTRATTI: <u>Socially Responsible Investment in General Equilibrium</u></i>
CTN	94.2003	<i>Parkash CHANDER: <u>The γ-Core and Coalition Formation</u></i>
IEM	95.2003	<i>Matteo MANERA and Angelo MARZULLO: <u>Modelling the Load Curve of Aggregate Electricity Consumption Using Principal Components</u></i>
IEM	96.2003	<i>Alessandro LANZA, Matteo MANERA, Margherita GRASSO and Massimo GIOVANNINI: <u>Long-run Models of Oil Stock Prices</u></i>
CTN	97.2003	<i>Steven J. BRAMS, Michael A. JONES, and D. Marc KILGOUR: <u>Forming Stable Coalitions: The Process Matters</u></i>
KNOW	98.2003	<i>John CROWLEY, Marie-Cecile NAVES (Ixxiii): <u>Anti-Racist Policies in France. From Ideological and Historical Schemes to Socio-Political Realities</u></i>
KNOW	99.2003	<i>Richard THOMPSON FORD (Ixxiii): <u>Cultural Rights and Civic Virtue</u></i>
KNOW	100.2003	<i>Alaknanda PATEL (Ixxiii): <u>Cultural Diversity and Conflict in Multicultural Cities</u></i>
KNOW	101.2003	<i>David MAY (Ixxiii): <u>The Struggle of Becoming Established in a Deprived Inner-City Neighbourhood</u></i>
KNOW	102.2003	<i>Sébastien ARCAND, Danielle JUTEAU, Sirma BILGE, and Francine LEMIRE (Ixxiii) : <u>Municipal Reform on the Island of Montreal: Tensions Between Two Majority Groups in a Multicultural City</u></i>
CLIM	103.2003	<i>Barbara BUCHNER and Carlo CARRARO: <u>China and the Evolution of the Present Climate Regime</u></i>
CLIM	104.2003	<i>Barbara BUCHNER and Carlo CARRARO: <u>Emissions Trading Regimes and Incentives to Participate in International Climate Agreements</u></i>
CLIM	105.2003	<i>Anil MARKANDYA and Dirk T.G. RÜBBELKE: <u>Ancillary Benefits of Climate Policy</u></i>
NRM	106.2003	<i>Anne Sophie CRÉPIN (Ixiv): <u>Management Challenges for Multiple-Species Boreal Forests</u></i>
NRM	107.2003	<i>Anne Sophie CRÉPIN (Ixiv): <u>Threshold Effects in Coral Reef Fisheries</u></i>
SIEV	108.2003	<i>Sara ANIYAR (Ixiv): <u>Estimating the Value of Oil Capital in a Small Open Economy: The Venezuela's Example</u></i>
SIEV	109.2003	<i>Kenneth ARROW, Partha DASGUPTA and Karl-Göran MÄLER(Ixiv): <u>Evaluating Projects and Assessing Sustainable Development in Imperfect Economies</u></i>
NRM	110.2003	<i>Anastasios XEPAPADEAS and Catarina ROSETA-PALMA(Ixiv): <u>Instabilities and Robust Control in Fisheries</u></i>
NRM	111.2003	<i>Charles PERRINGS and Brian WALKER (Ixiv): <u>Conservation and Optimal Use of Rangelands</u></i>
ETA	112.2003	<i>Jack GOODY (Ixiv): <u>Globalisation, Population and Ecology</u></i>
CTN	113.2003	<i>Carlo CARRARO, Carmen MARCHIORI and Sonia OREFFICE: <u>Endogenous Minimum Participation in International Environmental Treaties</u></i>
CTN	114.2003	<i>Guillaume HAERINGER and Myrna WOODERS: <u>Decentralized Job Matching</u></i>
CTN	115.2003	<i>Hideo KONISHI and M. Utku UNVER: <u>Credible Group Stability in Multi-Partner Matching Problems</u></i>
CTN	116.2003	<i>Somdeb LAHIRI: <u>Stable Matchings for the Room-Mates Problem</u></i>
CTN	117.2003	<i>Somdeb LAHIRI: <u>Stable Matchings for a Generalized Marriage Problem</u></i>
CTN	118.2003	<i>Marita LAUKKANEN: <u>Transboundary Fisheries Management under Implementation Uncertainty</u></i>
CTN	119.2003	<i>Edward CARTWRIGHT and Myrna WOODERS: <u>Social Conformity and Bounded Rationality in Arbitrary Games with Incomplete Information: Some First Results</u></i>
CTN	120.2003	<i>Gianluigi VERNASCA: <u>Dynamic Price Competition with Price Adjustment Costs and Product Differentiation</u></i>
CTN	121.2003	<i>Myrna WOODERS, Edward CARTWRIGHT and Reinhard SELTEN: <u>Social Conformity in Games with Many Players</u></i>
CTN	122.2003	<i>Edward CARTWRIGHT and Myrna WOODERS: <u>On Equilibrium in Pure Strategies in Games with Many Players</u></i>
CTN	123.2003	<i>Edward CARTWRIGHT and Myrna WOODERS: <u>Conformity and Bounded Rationality in Games with Many Players</u></i>
	1000	Carlo CARRARO, Alessandro LANZA and Valeria PAPPONETTI: <u>One Thousand Working Papers</u>

NOTE DI LAVORO PUBLISHED IN 2004

IEM	1.2004	<i>Anil MARKANDYA, Suzette PEDROSO and Alexander GOLUB:</i> <u>Empirical Analysis of National Income and So2 Emissions in Selected European Countries</u>
ETA	2.2004	<i>Masahisa FUJITA and Shlomo WEBER:</i> <u>Strategic Immigration Policies and Welfare in Heterogeneous Countries</u>
PRA	3.2004	<i>Adolfo DI CARLUCCIO, Giovanni FERRI, Cecilia FRALE and Ottavio RICCHI:</i> <u>Do Privatizations Boost Household Shareholding? Evidence from Italy</u>
ETA	4.2004	<i>Victor GINSBURGH and Shlomo WEBER:</i> <u>Languages Disenfranchisement in the European Union</u>
ETA	5.2004	<i>Romano PIRAS:</i> <u>Growth, Congestion of Public Goods, and Second-Best Optimal Policy</u>
CCMP	6.2004	<i>Herman R.J. VOLLEBERGH:</i> <u>Lessons from the Polder: Is Dutch CO2-Taxation Optimal</u>
PRA	7.2004	<i>Sandro BRUSCO, Giuseppe LOPOMO and S. VISWANATHAN (lxv):</i> <u>Merger Mechanisms</u>
PRA	8.2004	<i>Wolfgang AUSSENEGG, Pegaret PICHLER and Alex STOMPER (lxv):</i> <u>IPO Pricing with Bookbuilding, and a When-Issued Market</u>
PRA	9.2004	<i>Pegaret PICHLER and Alex STOMPER (lxv):</i> <u>Primary Market Design: Direct Mechanisms and Markets</u>
PRA	10.2004	<i>Florian ENGLMAIER, Pablo GUILLEN, Loreto LLORENTE, Sander ONDERSTAL and Rupert SAUSGRUBER (lxv):</i> <u>The Chopstick Auction: A Study of the Exposure Problem in Multi-Unit Auctions</u>
PRA	11.2004	<i>Bjarne BRENDSTRUP and Harry J. PAARSCH (lxv):</i> <u>Nonparametric Identification and Estimation of Multi-Unit, Sequential, Oral, Ascending-Price Auctions With Asymmetric Bidders</u>
PRA	12.2004	<i>Ohad KADAN (lxv):</i> <u>Equilibrium in the Two Player, k-Double Auction with Affiliated Private Values</u>
PRA	13.2004	<i>Maarten C.W. JANSSEN (lxv):</i> <u>Auctions as Coordination Devices</u>
PRA	14.2004	<i>Gadi FIBICH, Arieh GAVIOUS and Aner SELA (lxv):</i> <u>All-Pay Auctions with Weakly Risk-Averse Buyers</u>
PRA	15.2004	<i>Orly SADE, Charles SCHNITZLEIN and Jaime F. ZENDER (lxv):</i> <u>Competition and Cooperation in Divisible Good Auctions: An Experimental Examination</u>
PRA	16.2004	<i>Marta STRYSZOWSKA (lxv):</i> <u>Late and Multiple Bidding in Competing Second Price Internet Auctions</u>
CCMP	17.2004	<i>Slim Ben YOUSSEF:</i> <u>R&D in Cleaner Technology and International Trade</u>
NRM	18.2004	<i>Angelo ANTOCI, Simone BORGHESI and Paolo RUSSU (lxvi):</i> <u>Biodiversity and Economic Growth: Stabilization Versus Preservation of the Ecological Dynamics</u>
SIEV	19.2004	<i>Anna ALBERINI, Paolo ROSATO, Alberto LONGO and Valentina ZANATTA:</i> <u>Information and Willingness to Pay in a Contingent Valuation Study: The Value of S. Erasmo in the Lagoon of Venice</u>
NRM	20.2004	<i>Guido CANDELA and Roberto CELLINI (lxvii):</i> <u>Investment in Tourism Market: A Dynamic Model of Differentiated Oligopoly</u>
NRM	21.2004	<i>Jacqueline M. HAMILTON (lxvii):</i> <u>Climate and the Destination Choice of German Tourists</u>
NRM	22.2004	<i>Javier Rey-MAQUIEIRA PALMER, Javier LOZANO IBÁÑEZ and Carlos Mario GÓMEZ GÓMEZ (lxvii):</i> <u>Land, Environmental Externalities and Tourism Development</u>
NRM	23.2004	<i>Pius ODUNGA and Henk FOLMER (lxvii):</i> <u>Profiling Tourists for Balanced Utilization of Tourism-Based Resources in Kenya</u>
NRM	24.2004	<i>Jean-Jacques NOWAK, Mondher SAHLI and Pasquale M. SGRO (lxvii):</i> <u>Tourism, Trade and Domestic Welfare</u>
NRM	25.2004	<i>Riaz SHAREEF (lxvii):</i> <u>Country Risk Ratings of Small Island Tourism Economies</u>
NRM	26.2004	<i>Juan Luis EUGENIO-MARTÍN, Noelia MARTÍN MORALES and Riccardo SCARPA (lxvii):</i> <u>Tourism and Economic Growth in Latin American Countries: A Panel Data Approach</u>
NRM	27.2004	<i>Raúl Hernández MARTÍN (lxvii):</i> <u>Impact of Tourism Consumption on GDP. The Role of Imports</u>
CSRM	28.2004	<i>Nicoletta FERRO:</i> <u>Cross-Country Ethical Dilemmas in Business: A Descriptive Framework</u>
NRM	29.2004	<i>Marian WEBER (lxvi):</i> <u>Assessing the Effectiveness of Tradable Landuse Rights for Biodiversity Conservation: an Application to Canada's Boreal Mixedwood Forest</u>
NRM	30.2004	<i>Trond BJORN DAL, Phoebe KOUNDOURI and Sean PASCOE (lxvi):</i> <u>Output Substitution in Multi-Species Trawl Fisheries: Implications for Quota Setting</u>
CCMP	31.2004	<i>Marzio GALEOTTI, Alessandra GORIA, Paolo MOMBRINI and Evi SPANTIDAKI:</i> <u>Weather Impacts on Natural, Social and Economic Systems (WISE) Part I: Sectoral Analysis of Climate Impacts in Italy</u>
CCMP	32.2004	<i>Marzio GALEOTTI, Alessandra GORIA, Paolo MOMBRINI and Evi SPANTIDAKI:</i> <u>Weather Impacts on Natural, Social and Economic Systems (WISE) Part II: Individual Perception of Climate Extremes in Italy</u>
CTN	33.2004	<i>Wilson PEREZ:</i> <u>Divide and Conquer: Noisy Communication in Networks, Power, and Wealth Distribution</u>
KTHC	34.2004	<i>Gianmarco I.P. OTTAVIANO and Giovanni PERI (lxviii):</i> <u>The Economic Value of Cultural Diversity: Evidence from US Cities</u>
KTHC	35.2004	<i>Linda CHAIB (lxviii):</i> <u>Immigration and Local Urban Participatory Democracy: A Boston-Paris Comparison</u>
KTHC	36.2004	<i>Franca ECKERT COEN and Claudio ROSSI (lxviii):</i> <u>Foreigners, Immigrants, Host Cities: The Policies of Multi-Ethnicity in Rome. Reading Governance in a Local Context</u>
KTHC	37.2004	<i>Kristine CRANE (lxviii):</i> <u>Governing Migration: Immigrant Groups' Strategies in Three Italian Cities – Rome, Naples and Bari</u>
KTHC	38.2004	<i>Kiflemariam HAMDE (lxviii):</i> <u>Mind in Africa, Body in Europe: The Struggle for Maintaining and Transforming Cultural Identity - A Note from the Experience of Eritrean Immigrants in Stockholm</u>
ETA	39.2004	<i>Alberto CAVALIERE:</i> <u>Price Competition with Information Disparities in a Vertically Differentiated Duopoly</u>
PRA	40.2004	<i>Andrea BIGANO and Stef PROOST:</i> <u>The Opening of the European Electricity Market and Environmental Policy: Does the Degree of Competition Matter?</u>
CCMP	41.2004	<i>Micheal FINUS (lxix):</i> <u>International Cooperation to Resolve International Pollution Problems</u>

KTHC	42.2004	<i>Francesco CRESPI</i> : <u>Notes on the Determinants of Innovation: A Multi-Perspective Analysis</u>
CTN	43.2004	<i>Sergio CURRARINI and Marco MARINI</i> : <u>Coalition Formation in Games without Synergies</u>
CTN	44.2004	<i>Marc ESCRHUELA-VILLAR</i> : <u>Cartel Sustainability and Cartel Stability</u>
NRM	45.2004	<i>Sebastian BERVOETS and Nicolas GRAVEL</i> (Ixvi): <u>Appraising Diversity with an Ordinal Notion of Similarity: An Axiomatic Approach</u>
NRM	46.2004	<i>Signe ANTHON and Bo JELLESMARK THORSEN</i> (Ixvi): <u>Optimal Afforestation Contracts with Asymmetric Information on Private Environmental Benefits</u>
NRM	47.2004	<i>John MBURU</i> (Ixvi): <u>Wildlife Conservation and Management in Kenya: Towards a Co-management Approach</u>
NRM	48.2004	<i>Ekin BIROL, Ágnes GYOVAI and Melinda SMALE</i> (Ixvi): <u>Using a Choice Experiment to Value Agricultural Biodiversity on Hungarian Small Farms: Agri-Environmental Policies in a Transitional Economy</u>
CCMP	49.2004	<i>Gernot KLEPPER and Sonja PETERSON</i> : <u>The EU Emissions Trading Scheme. Allowance Prices, Trade Flows, Competitiveness Effects</u>
GG	50.2004	<i>Scott BARRETT and Michael HOEL</i> : <u>Optimal Disease Eradication</u>
CTN	51.2004	<i>Dinko DIMITROV, Peter BORM, Ruud HENDRICKX and Shao CHIN SUNG</i> : <u>Simple Priorities and Core Stability in Hedonic Games</u>
SIEV	52.2004	<i>Francesco RICCI</i> : <u>Channels of Transmission of Environmental Policy to Economic Growth: A Survey of the Theory</u>
SIEV	53.2004	<i>Anna ALBERINI, Maureen CROPPER, Alan KRUPNICK and Nathalie B. SIMON</i> : <u>Willingness to Pay for Mortality Risk Reductions: Does Latency Matter?</u>
NRM	54.2004	<i>Ingo BRÄUER and Rainer MARGGRAF</i> (Ixvi): <u>Valuation of Ecosystem Services Provided by Biodiversity Conservation: An Integrated Hydrological and Economic Model to Value the Enhanced Nitrogen Retention in Renaturated Streams</u>
NRM	55.2004	<i>Timo GOESCHL and Tun LIN</i> (Ixvi): <u>Biodiversity Conservation on Private Lands: Information Problems and Regulatory Choices</u>
NRM	56.2004	<i>Tom DEDEURWAERDERE</i> (Ixvi): <u>Bioprospection: From the Economics of Contracts to Reflexive Governance</u>
CCMP	57.2004	<i>Katrin REHDANZ and David MADDISON</i> : <u>The Amenity Value of Climate to German Households</u>
CCMP	58.2004	<i>Koen SMEKENS and Bob VAN DER ZWAAN</i> : <u>Environmental Externalities of Geological Carbon Sequestration Effects on Energy Scenarios</u>
NRM	59.2004	<i>Valentina BOSETTI, Mariaester CASSINELLI and Alessandro LANZA</i> (Ixvii): <u>Using Data Envelopment Analysis to Evaluate Environmentally Conscious Tourism Management</u>
NRM	60.2004	<i>Timo GOESCHL and Danilo CAMARGO IGLIORI</i> (Ixvi): <u>Property Rights Conservation and Development: An Analysis of Extractive Reserves in the Brazilian Amazon</u>
CCMP	61.2004	<i>Barbara BUCHNER and Carlo CARRARO</i> : <u>Economic and Environmental Effectiveness of a Technology-based Climate Protocol</u>
NRM	62.2004	<i>Elissaios PAPYRAKIS and Reyer GERLAGH</i> : <u>Resource-Abundance and Economic Growth in the U.S.</u>
NRM	63.2004	<i>Györgyi BELA, György PATAKI, Melinda SMALE and Mariann HAJDÚ</i> (Ixvi): <u>Conserving Crop Genetic Resources on Smallholder Farms in Hungary: Institutional Analysis</u>
NRM	64.2004	<i>E.C.M. RUIJGROK and E.E.M. NILLESEN</i> (Ixvi): <u>The Socio-Economic Value of Natural Riverbanks in the Netherlands</u>
NRM	65.2004	<i>E.C.M. RUIJGROK</i> (Ixvi): <u>Reducing Acidification: The Benefits of Increased Nature Quality. Investigating the Possibilities of the Contingent Valuation Method</u>
ETA	66.2004	<i>Giannis VARDAS and Anastasios XEPAPADEAS</i> : <u>Uncertainty Aversion, Robust Control and Asset Holdings</u>
GG	67.2004	<i>Anastasios XEPAPADEAS and Constadina PASSA</i> : <u>Participation in and Compliance with Public Voluntary Environmental Programs: An Evolutionary Approach</u>
GG	68.2004	<i>Michael FINUS</i> : <u>Modesty Pays: Sometimes!</u>
NRM	69.2004	<i>Trond BJØRNDAL and Ana BRASÃO</i> : <u>The Northern Atlantic Bluefin Tuna Fisheries: Management and Policy Implications</u>
CTN	70.2004	<i>Alejandro CAPARRÓS, Abdelhakim HAMMOUDI and Tarik TAZDAÏT</i> : <u>On Coalition Formation with Heterogeneous Agents</u>
IEM	71.2004	<i>Massimo GIOVANNINI, Margherita GRASSO, Alessandro LANZA and Matteo MANERA</i> : <u>Conditional Correlations in the Returns on Oil Companies Stock Prices and Their Determinants</u>
IEM	72.2004	<i>Alessandro LANZA, Matteo MANERA and Michael MCALEER</i> : <u>Modelling Dynamic Conditional Correlations in WTI Oil Forward and Futures Returns</u>
SIEV	73.2004	<i>Margarita GENIUS and Elisabetta STRAZZERA</i> : <u>The Copula Approach to Sample Selection Modelling: An Application to the Recreational Value of Forests</u>
CCMP	74.2004	<i>Rob DELLINK and Ekko van IERLAND</i> : <u>Pollution Abatement in the Netherlands: A Dynamic Applied General Equilibrium Assessment</u>
ETA	75.2004	<i>Rosella LEVAGGI and Michele MORETTO</i> : <u>Investment in Hospital Care Technology under Different Purchasing Rules: A Real Option Approach</u>
CTN	76.2004	<i>Salvador BARBERÀ and Matthew O. JACKSON</i> (Ixx): <u>On the Weights of Nations: Assigning Voting Weights in a Heterogeneous Union</u>
CTN	77.2004	<i>Àlex ARENAS, Antonio CABRALES, Albert DÍAZ-GUILERA, Roger GUIMERA and Fernando VEGA-REDONDO</i> (Ixx): <u>Optimal Information Transmission in Organizations: Search and Congestion</u>
CTN	78.2004	<i>Francis BLOCH and Armando GOMES</i> (Ixx): <u>Contracting with Externalities and Outside Options</u>

- (lix) This paper was presented at the ENGIME Workshop on “Mapping Diversity”, Leuven, May 16-17, 2002
- (lx) This paper was presented at the EuroConference on “Auctions and Market Design: Theory, Evidence and Applications”, organised by the Fondazione Eni Enrico Mattei, Milan, September 26-28, 2002
- (lxi) This paper was presented at the Eighth Meeting of the Coalition Theory Network organised by the GREQAM, Aix-en-Provence, France, January 24-25, 2003
- (lxii) This paper was presented at the ENGIME Workshop on “Communication across Cultures in Multicultural Cities”, The Hague, November 7-8, 2002
- (lxiii) This paper was presented at the ENGIME Workshop on “Social dynamics and conflicts in multicultural cities”, Milan, March 20-21, 2003
- (lxiv) This paper was presented at the International Conference on “Theoretical Topics in Ecological Economics”, organised by the Abdus Salam International Centre for Theoretical Physics - ICTP, the Beijer International Institute of Ecological Economics, and Fondazione Eni Enrico Mattei – FEEM Trieste, February 10-21, 2003
- (lxv) This paper was presented at the EuroConference on “Auctions and Market Design: Theory, Evidence and Applications” organised by Fondazione Eni Enrico Mattei and sponsored by the EU, Milan, September 25-27, 2003
- (lxvi) This paper has been presented at the 4th BioEcon Workshop on “Economic Analysis of Policies for Biodiversity Conservation” organised on behalf of the BIOECON Network by Fondazione Eni Enrico Mattei, Venice International University (VIU) and University College London (UCL), Venice, August 28-29, 2003
- (lxvii) This paper has been presented at the international conference on “Tourism and Sustainable Economic Development – Macro and Micro Economic Issues” jointly organised by CRENoS (Università di Cagliari e Sassari, Italy) and Fondazione Eni Enrico Mattei, and supported by the World Bank, Sardinia, September 19-20, 2003
- (lxviii) This paper was presented at the ENGIME Workshop on “Governance and Policies in Multicultural Cities”, Rome, June 5-6, 2003
- (lxix) This paper was presented at the Fourth EEP Plenary Workshop and EEP Conference “The Future of Climate Policy”, Cagliari, Italy, 27-28 March 2003
- (lxx) This paper was presented at the 9th Coalition Theory Workshop on "Collective Decisions and Institutional Design" organised by the Universitat Autònoma de Barcelona and held in Barcelona, Spain, January 30-31, 2004

2003 SERIES

CLIM	<i>Climate Change Modelling and Policy</i> (Editor: Marzio Galeotti)
GG	<i>Global Governance</i> (Editor: Carlo Carraro)
SIEV	<i>Sustainability Indicators and Environmental Valuation</i> (Editor: Anna Alberini)
NRM	<i>Natural Resources Management</i> (Editor: Carlo Giupponi)
KNOW	<i>Knowledge, Technology, Human Capital</i> (Editor: Gianmarco Ottaviano)
IEM	<i>International Energy Markets</i> (Editor: Anil Markandya)
CSR	<i>Corporate Social Responsibility and Management</i> (Editor: Sabina Ratti)
PRIV	<i>Privatisation, Regulation, Antitrust</i> (Editor: Bernardo Bortolotti)
ETA	<i>Economic Theory and Applications</i> (Editor: Carlo Carraro)
CTN	<i>Coalition Theory Network</i>

2004 SERIES

CCMP	<i>Climate Change Modelling and Policy</i> (Editor: Marzio Galeotti)
GG	<i>Global Governance</i> (Editor: Carlo Carraro)
SIEV	<i>Sustainability Indicators and Environmental Valuation</i> (Editor: Anna Alberini)
NRM	<i>Natural Resources Management</i> (Editor: Carlo Giupponi)
KTHC	<i>Knowledge, Technology, Human Capital</i> (Editor: Gianmarco Ottaviano)
IEM	<i>International Energy Markets</i> (Editor: Anil Markandya)
CSR	<i>Corporate Social Responsibility and Management</i> (Editor: Sabina Ratti)
PRA	<i>Privatisation, Regulation, Antitrust</i> (Editor: Bernardo Bortolotti)
ETA	<i>Economic Theory and Applications</i> (Editor: Carlo Carraro)
CTN	<i>Coalition Theory Network</i>