

# Inequalities and the Social Cost of Carbon

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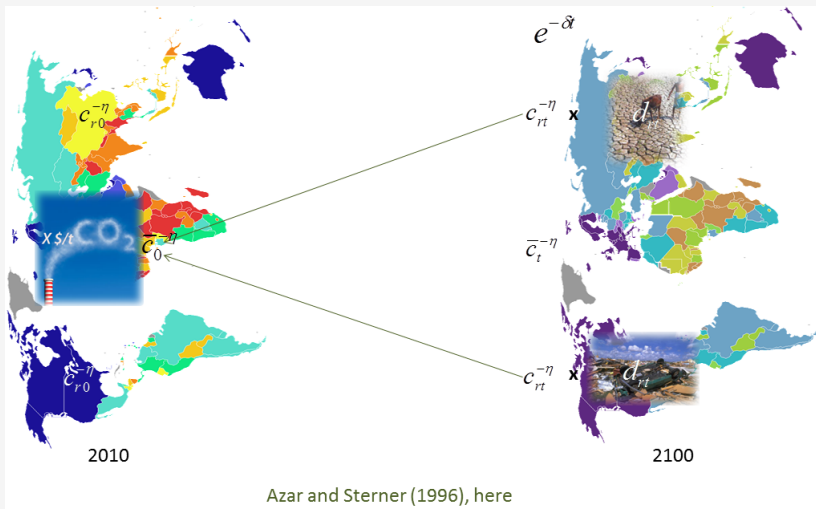
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# Motivation

- Equity aspects in the evaluation of Climate Change
  - Inter-generational Equity (“**discounting**”, alternative approaches (maxmin, LRS))
  - Intra-generational Equity (“**equity weighting**”)
- Social preferences in the two dimensions might be different (Atkinson et al. 2009)
- Integrated Assessment Models capture inequity aversion through a single utility function
- Inequality is considered only between (arbitrarily cut) regions

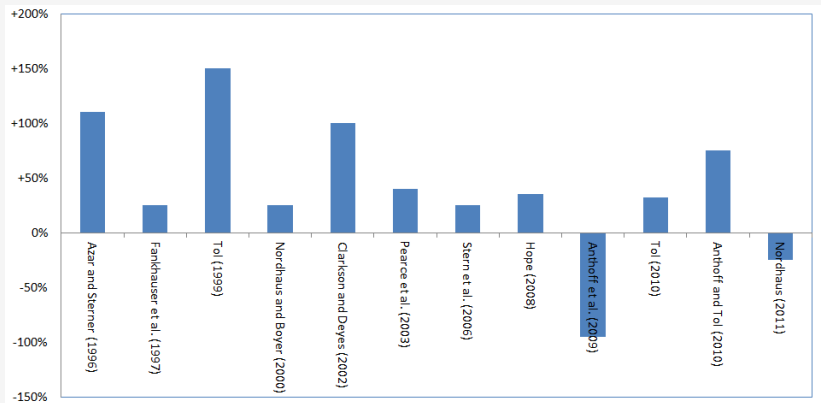
# Motivation

- Discounting and equity weighting *jointly* is a complex picture



# The effect of Equity Weighting

- Does equity weighting increase or decrease the Social Cost of Carbon?



- Different approaches, inequality aversion parameters, discount rates

# Contributions of the paper

- Inequality aversion between and within generations (Nordhaus, 2011)
- Disentangling resistance to intertemporal substitution ( $\eta$ ) and inequality aversion ( $\gamma$ )
  - $\implies$  allows discounting and equity weighting to be separable
- The level of disaggregation
  - Inequality on the between-country level, not between (arbitrary) regions
  - Allow for non-constant per-capita damages within regions

# Outline

- 1 Introduction
- 2 Discounting and Equity Weighting
- 3 Inequality between countries
- 4 Numerical results
- 5 Conclusion

# What does utility as log of consumption imply?

- Intertemporal Substitution:

- Completely altruistic Social Planner should discount future cash flows just at the growth rate of consumption

- Risk aversion

- The lottery of having 1 or 2 Mio. with equal probability is equivalent to a certain amount of 1.41 Mio.

- Inequality aversion

- One dollar to a Chinese is around ten times “worth” a dollar to an American

# Discounting and Inequality

- Discount factor: weight based on marginal utility

$$DF_{rt} = \frac{c_{rt}^{-\eta}}{c_{r0}^{-\eta}} (1 + \rho)^{-t}$$

- Choice of the appropriate discount rate not obvious when considering inequality

⇒ inequality-adjusted discount rate (Gollier 2010, Emmerling 2010)  $r_t^{in}$

- Convergence ⇒ higher discount rate ⇒ SCC lower



# Equity weighting

- Reasons for the use of Equity Weights in CBA
  - income distribution might not be optimal
  - transfers implied by optimality might not be carried out
  - one dollar = one vote
- Equity Weighting:
  - weighty based on a Utilitarian SWF and CRRA utility
  - weights  $w_{it} = \frac{U'(c_{it})}{U'(\bar{c}_t)} = \left(\frac{\bar{c}_t}{c_{it}}\right)^\eta$  based on marginal utility of income
- similar to the discount factors presented before

# Equity weighting

- Consider  $R$  different regions  $r$  at time  $t$ : marginal impacts or “damages”  $d_{rt}$  to compute the Social Cost of Carbon  $V_x$

$$V_x = \sum_{t=1}^T \sum_{r=1}^R P_{rt} \underbrace{(1+\rho)^{-t} \frac{c_{rt}^{-\eta}}{c_{r0}^{-\eta}}}_{e^{-r_{rt}t}} \underbrace{\frac{c_{rt}^{-\eta}}{c_{rt}^{-\eta}}}_{\text{weights } w_{rt}} d_{rt}$$

- The use of region-specific discount rates does not seem justifiable
- “Intertemporal approach”

$$V_x = \sum_{t=1}^T \sum_{r=1}^R P_{rt} \frac{c_{rt}^{-\eta}}{c_{x0}^{-\eta}} (1+\rho)^{-t} d_{rt}$$

- Monetarization with marginal utility of consumption in region  $x$  today

## Disentangling both concepts

- The curvature of  $U$ , i.e.,  $\eta$ , determines risk aversion, inequality aversion, and resistance to intertemporal substitution
- Separation of the three dimensions in the spirit of Kreps-Porteus (1978) / Epstein-Zin (1989, 1991)

- Standard Welfare function:

$$W = \sum_{t=1}^T \sum_{r=1}^R P_{rt} U(c_{rt}) (1 + \rho)^{-t}$$

- Disentangling:

$$W^R = \sum_{t=1}^T V \left[ P_t U^{-1} \left( \sum_{r=1}^R \frac{P_{rt}}{P_t} U(c_{rt}) \right) \right] (1 + \rho)^{-t}$$

- Isoelastic specification to disentangle inequality aversion across space( $\gamma$ ) and time( $\eta$ )

# Disentangling both concepts

$$S^R = \sum_{t=1}^T \sum_{r=1}^R P_{rt} \underbrace{\left( \frac{c_{rt}/c_t^{ede}}{c_{r0}/c_0^{ede}} \right)^{\eta-\gamma}}_{\Omega_{rt}} \underbrace{\frac{c_{r0}^{-\gamma}}{c_{x0}^{-\gamma}} \frac{c_{rt}^{-\eta}}{c_{r0}^{-\eta}}}_{EW} \underbrace{(1+\rho)^{-t}}_{DF_{rt}} d_{rt}$$

- Standard discount factor and equity weights as before for  $\eta = \gamma$
- If  $\gamma \neq \eta$ :
  - If  $\gamma < \eta$ :  $\Omega_{rt} > 1$  for regions that are relatively richer in the future
  - If  $\gamma > \eta$ :  $\Omega_{rt} > 1$  for *relatively poorer* regions at  $t \implies$  equity weighting becomes more important
- As  $\gamma \rightarrow 0$ , normalization disappears, implying a unique carbon price

# Inequality between countries

- Spatial resolution of IAMs very broad (RICE: 13, PAGE: 8, FUND: 16)
- (downward?) biased estimate of the optimal Social Cost of Carbon
- Geographical distribution should be taken into account of
  - **income** (Stern (2006), Anthoff et al. (2009), , UNDP (2010))
  - **impacts** (Kverndokk and Rose (2008), Mendelsohn (1994, 2011))
- Disaggregate region  $r$  by assuming a distribution of consumption:  
$$c_{rt} \sim F_{rt}$$

# Inequality between countries

- Measure inequality using Atkinson class of inequality indices

$$I_{rt}(\gamma) = 1 - \frac{c_{rt}^{ede}}{c_{rt}} \text{ where } c_{rt}^{ede} = \left( \int c^{1-\gamma} dF_{rt} \right)^{\frac{1}{1-\gamma}}$$

- $c_{rt}^{ede}$ : equally-distributed equivalent consumption
- Consistent with using a Utilitarian SWF with isoelastic utility function
- Analytical solutions: Taylor Approx. or lognormal income distribution (Atkinson and Brandolini, 2010)

## Equal distribution of impacts

- SCC formula: Only equity weights are changed

$$\frac{c_{rt}^{-\gamma}}{c_{x0}^{-\gamma}} \Rightarrow \frac{c_{rt}^{-\gamma}}{c_{x0}^{-\gamma}} (1 - I_{rt}(\gamma))^{-(\gamma+1)}$$

- Role of Prudence ( $RP = \gamma + 1$ ) or “downside inequality aversion”
- For negative impacts, higher inequality implies unambiguously a higher SCC ( $\frac{\partial S^{RC}}{\partial I_{rt}} > 0$ )
- So far: impacts are assumed to be equally distributed between countries (on per-capita basis)

# Un-equal distribution of impacts

- Impacts modeled as damage function:  $d_{rt} = D(c_{rt})$ , e.g.,  $D(c_{rt}) \propto c_{rt}^{\alpha}$
- can be combined to finally yield for the SCC

$$S^{RCD} = \sum_{t=1}^T \sum_{r=1}^R P_{rt} \left( \frac{c_t^{ede}}{c_0^{ede}} \right)^{\gamma-\eta} \frac{c_{rt}^{-\gamma}}{c_{x0}^{-\gamma}} \underbrace{(1 - I(\gamma)_{rt})^{-\frac{(\gamma-\alpha)((\gamma-\alpha)+1)}{\gamma}}}_{\Delta_{rt}} (1+\rho)^{-t} d_{rt}$$

- equivalent to adjusting damages  $d_{rt}$  by the factor  $\Delta_{rt}$
- Depending on inequality aversion and the impact elasticity  $\alpha$ :
  - $\alpha = 0$ :  $\Delta_{rt} < 1$  (as before: overall lower weights of impacts, i.e., lower SCC)
  - $\alpha \in [\gamma, \gamma+1]$ :  $\Delta_{rt} < 1$  (most realistic case)
  - $\gamma = 1$  and  $\alpha = 1$ :  $\Delta_{rt} = 1$  (within-region inequality does not matter)

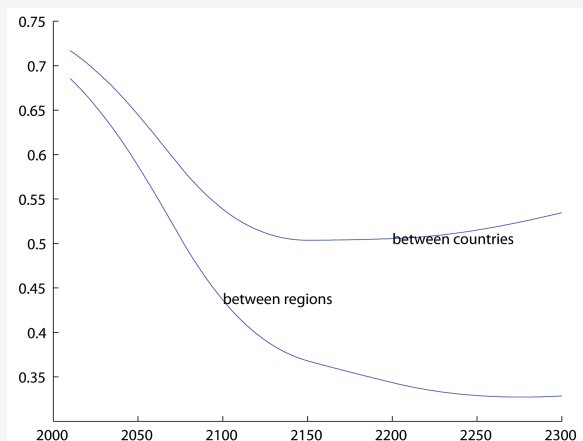


# Values for $\eta$ and $\gamma$

- From survey data/experiments: large variability  
Atkinson et al., 2009:  $\eta \sim 9$ ,  $\gamma \sim 2 - 3$  (and  $RRA \sim 3 - 5$ )
- Climate change literature: typically  $\eta = 1 - 2$ , recent tendency towards  $\eta = 1.5$
- From revealed social preferences (income tax schedule, ODA):
  - $\gamma \sim 1.4$  (Evans 2005)
  - $\gamma = 0.5 - 1.5$  (Clarkson and Deyes, 2002)
  - $\gamma = 0.25 - 0.75$  (U.S. Bureau, 2006)
  - $\gamma \sim 0.7$  (Tol 2010)
- A lower value for  $\gamma$  than for  $\eta$  and  $RRA$  seems a robust finding
- Elasticity of impacts ( $\alpha$ ) between 0.9 and 1.3, mean very close to one (Anthoff and Tol, 2011)

# Income inequality predictions

- Convergence mainly between world regions
- Forecasting increasing inequality within regions based on historical variance of log income ( $\sigma^2$ )

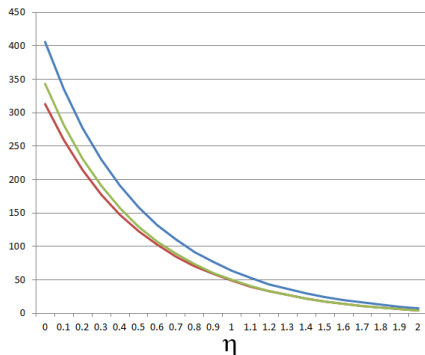


# FUND model

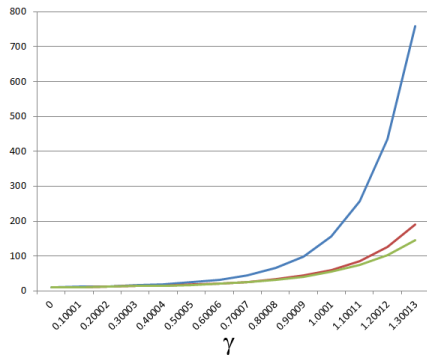
- IAM focussing on impacts and evaluation of climate change
- rather complex damage module (energy, weather related events, health, biodiversity, migration)
- 16 regions
- GDP and Population scenario based on EMF14 Stand. Scen.
- SCC as optimal carbon tax/permit price
- Optimal Policy and Welfare optimization  $\implies$  future work!

# Results

Discounting ( $\rho = 1.5\%$ ,  $\gamma = 0.5$ )



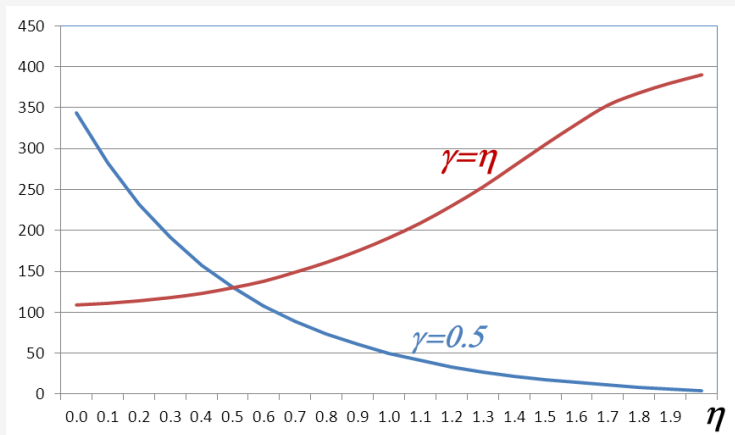
Equity weighting ( $\rho = 1.5\%$ ,  $\eta = 1.5$ )



regional weights disaggregated non-constant damages

# Results

- Standard SCC vs. disentangled discount rate and equity weights



# Results

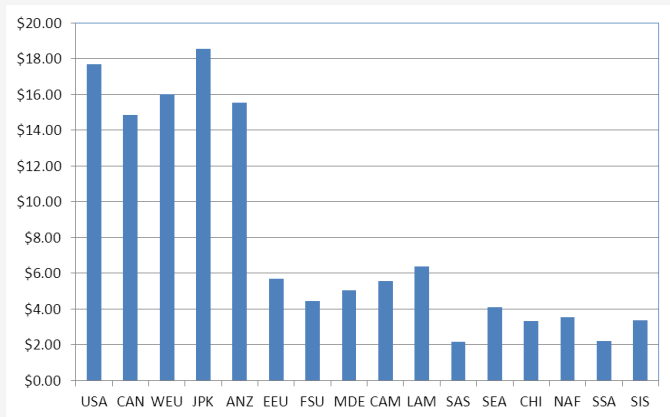
- Using the FUND model to compute the Social Cost of Carbon in  $\$/tC$  ( $\eta = 1.5, \rho = 1.5\%$ ):

type of equity weights	$\gamma = 1.5$	$\gamma = 0.5$
no equity weighting ( $\gamma = 0$ )	10.2\$	10.2\$
regional equity weights	304.7\$	17.7\$
individual equity weights	2479\$	24.5\$
constant relative impacts ( $\alpha = 1$ )	458.1\$	17.8\$

- Standard regional equity weights imply a higher SCC
- Considering inequality within regions, the SCC increases; non-constant impacts reduce the effect
- Effect of equity weighting is significantly lower if the discount rate is left unchanged

# Results

- Equity weighted SCC estimates according to region ( $\rho = 1.5\%$ ,  $\eta = 1.5$ ,  $\gamma = 0.5$ ,  $\alpha = 1$ )



# Conclusion

- The welfare specification has a dramatic impact on the optimal climate policy
- Social preferences in different dimensions typically do not coincide, in particular  $\gamma < \eta$
- Equity weightys increase the SCC, but the effect is reduced if disentangled from the discount rate, and thus lower than previous estimates
- The spatial resolution of models matters and finer resolution seems to increase the SCC



# Conclusion

Thank you!