

Generalized Nash Equilibrium and incomplete energy markets: Market Coupling in the European Power System

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The context: market integration in the European Community

Market coupling as a market design:

Implemented in electricity since 2006 (in discussion for gas these days (e.g. Florence 11 March 2011))

- Day ahead and real time markets:
 - ① Market coupling deals with the day-ahead market;
 - ② Real time is seen as a deviation management mechanism and agents are incentivised not to resort to it.
- Integration of energy and transmission:
 - ① Market coupling partially integrates energy and transmission;
 - ② The zonal energy market clears on an ATC (available transmission capacity) representation of the network;
 - ③ Counter-trading, if necessary, takes care of the real network.
- Counter-trading:
 - ① Counter-trading is operated by zonal System Operators;
 - ② Without clear indication on how they coordinate.

Organisation of Cross-zonal Trade of Electricity

The energy market

- Two groups of agents:
 - ① Zonal (national) Power Exchanges (PXs) that clear the intra and inter zone energy markets;
 - ② Zonal (national) Transmission System Operators (TSOs) that guarantee the security of the transmission system.

Market coupling concentrates on the energy market and is organized as follows:

- TSOs provide the energy market with a simplified representation of the grid (today the ATC);
- PXs jointly clear the energy markets taking into account the ATC received from the TSOs;
- PXs find the equilibrium electricity quantities and prices;
- In presence of saturation of ATCs, electricity prices differ per zone.

Organisation of Cross-Border Trade of Electricity

The transmission market

THE CONTEXT: A contribution to the never ending debate between zonal and nodal systems:

- first in electricity, resolved in favour of nodal in the US, good arguments for zonal in EU.
- beginning in gas in EU again (point to point transmission rights will be illegal in EU.)
- in economic terms: what is the impact of an incomplete pricing of transmission.

THE TALK: The flows resulting from the PXs' market clearing may not be feasible for the grid:

- TSOs **restore feasibility** by buying and selling incremental or decremental injections at the different nodes, while **maintaining the zonal electricity demand and production levels unchanged**. They socialized the cost of that **activity**. They can do that with different degree of coordination.

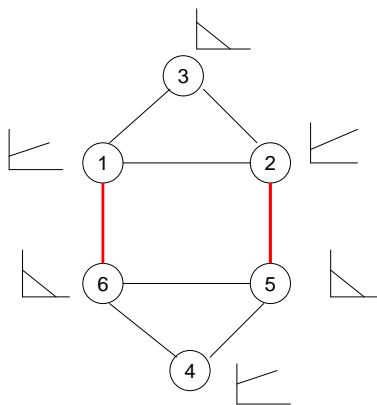
Assess the impact of this incomplete pricing of transmission services?

- 1 Methodological discussion: Generalized Nash Equilibrium and market incompleteness
- 2 A prototype case study
- 3 Conclusion.

Methodological discussion,
Generalized Nash Equilibrium and
market incompleteness

The illustrative example (1)

Six Node Market



SOURCE: Chao, H.P., S.C. Peck. 1998. Reliability Management in Competitive Electricity Markets. *Journal of Regulatory Economics*, **14**, 198-200.

The illustrative example (2)

DATA

- Demand and cost functions

Node	Function Type	Function
1	Marginal Cost	$10+0.05q$
2	Marginal Cost	$15+0.05q$
3	Inverse Demand	$37.5-0.05q$
4	Marginal Cost	$42.5+0.025q$
5	Inverse Demand	$75-0.1q$
6	Inverse Demand	$80-0.1q$

SOURCE: Chao, H.P., S.C. Peck. 1998. Reliability Management in Competitive Electricity Markets. *Journal of Regulatory Economics*, **14**, 198-200.

The illustrative Example (3)

DATA

- PTDF Matrix

Power (1 MW) Injected at Node	Power flow on link 1 \rightarrow 6 (MW)	Power flow on link 2 \rightarrow 5 (MW)
1	0.625	0.375
2	0.5	0.5
3	0.5625	0.4375
4	0.0625	-0.0625
5	0.125	-0.125
6 (hub)	0	0

Capacity link 1 \rightarrow 6 = 200 MW

Capacity link 2 \rightarrow 5 = 250 MW

SOURCE: Chao, H.P., S.C. Peck. 1998. Reliability Management in Competitive Electricity Markets. *Journal of Regulatory Economics*, **14**, 198-200.

The illustrative Example (4)

Notation

- **Sets**

- $l = (1 - 6), (2 - 5)$: Set of lines of the transmission grid;
- $n = 1, \dots, 6$: Set of nodes;
- $i = 1, 2, 4$: Subset of production nodes;
- $j = 3, 5, 6$: Subset of consumption nodes

- **Variables and Parameters**

- \bar{I} : Imports/export limits among zones;
- $PTDF_{n,l}$: Power Transfer Distribution Factor matrix of node n on line l ;
- \bar{F}_l : Limit of flow through line l ;
- q_n : Power generated or consumed in node n ;
- $c(q_i)$: Cost function of generator located in node i ;
- $w(q_j)$: Inverse demand function of consumer located in node j ;
- I : Imports/exports in the PX's problem;
- $\lambda_l^{+, -}$: Marginal value of the interconnection line l ;
- $\Delta q_n^{N,S}$: Demand and generation variations (counter-trading services) in node n operated by TSO^N or TSO^S

NOTE: The red lines (1-6) and (2-5) have limited capacity.

1. **Full integration of energy and transmission markets: the reference nodal system (Model 1)**
2. **Imperfect integration of energy and transmission markets: Market Coupling and centralized Counter-Trading (Model 2)**
3. **Imperfect integration of energy and transmission markets: Market Coupling and decentralized Counter-Trading (Model 3)**

The complete market: the nodal model

The reference model:

$$\mathbf{Min}_{\mathbf{q}_n} \quad \sum_{i=1,2,4} \int_0^{q_i} c_i(\xi) d\xi - \sum_{j=3,5,6} \int_0^{q_j} w_j(\xi) d\xi$$

s.t.

$$\bar{F}_l - \left(\sum_{i=1,2,4} PTDF_{i,l} q_i - \sum_{j=3,5,6} PTDF_{j,l} q_j \right) \geq 0 \quad (\lambda_l^+)$$

$$\bar{F}_l + \left(\sum_{i=1,2,4} PTDF_{i,l} q_i - \sum_{j=3,5,6} PTDF_{j,l} q_j \right) \geq 0 \quad (\lambda_l^-)$$

where $l = (1 - 6), (2 - 5)$

$$\sum_{i=1,2,4} q_i - \sum_{j=3,5,6} q_j = 0 \quad (\gamma)$$

$$q_n \geq 0 \quad \forall n \quad (\nu_n)$$

- **Welfare**

Social welfare: 23,000 €

- **Congested line**

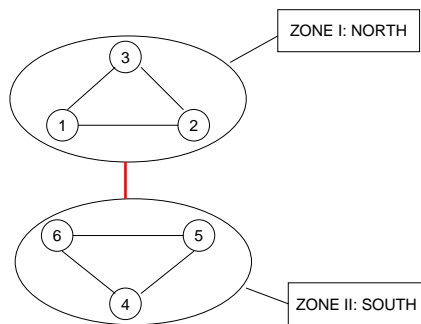
Both lines (1-6) and (2-5) transfer 200 MW of energy.

Line (1-6) is congested and its marginal value is 40 €/MWh.

Market Coupling and counter-trading

Market coupling: defining zones

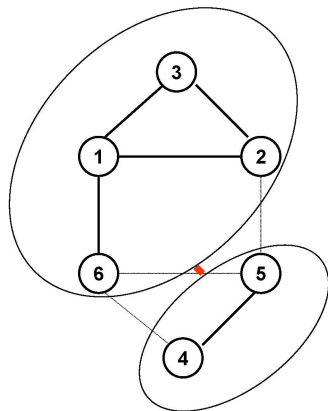
The market is subdivided into two zones (North and South), each controlled by a TSO (here a 3/3 case):



The TSOs compute the ATC between the two zones.

A second example: the 4/2 case

An alternative zonal organization:



Market coupling: clearing the energy market (depends on zonal decomposition)

The PXs solve the following problem for the 3/3 configuration:

$$\mathbf{Min}_{q_n} \quad \sum_{i=1,2,4} \int_0^{q_i} (\alpha + c_i(\xi)) d\xi - \sum_{j=3,5,6} \int_0^{q_j} w_j(\xi) d\xi$$

s.t.

$$q_1 + q_2 - q_3 - I = 0$$

$$q_4 - q_5 - q_6 + I = 0$$

$$q_n \geq 0 \quad \forall n$$

$$-\bar{I} \leq I \leq \bar{I}$$

- **Welfare before re-dispatching costs**

Welfare: 24,146 € (compared to 23,000 € in the nodal model)

- **Demand and generation**

Total demand is 800 as in the nodal system.

- **Interconnecting line**

The interconnection is saturated. Its marginal value is 18.33 €/MWh and the import/export is 450 MWh from North to South.

Market Coupling: optimal cross-border Counter-Trading

$$\begin{aligned} \text{Min}_{\Delta q_n} \quad & \sum_{i=1,2,4} \int_{q_i}^{q_i + \Delta q_i} c_i(\xi) d\xi - \sum_{j=3,5,6} \int_{q_j}^{q_j + \Delta q_j} w_j(\xi) d\xi \\ \text{s.t.} \quad & \end{aligned}$$

$$-\bar{F}_l \leq \sum_{i=1,2,4} (PTDF_{i,l}(q_i + \Delta q_i)) - \sum_{j=3,5,6} (PTDF_{j,l}(q_j + \Delta q_j)) \leq \bar{F}_l \quad (\lambda_l^\pm)$$

where $l = (1 - 6), (2 - 5)$

$$\sum_{i=1,2,4} \Delta q_i + \sum_{j=3,5,6} \Delta q_j = 0 \quad (\mu^1)$$

$$\sum_{i=1,2,4} \Delta q_i - \sum_{j=3,5,6} \Delta q_j = 0 \quad (\mu^2)$$

$$q_n + \Delta q_n \geq 0 \quad \forall n \quad (\nu_n)$$

- **Total re-dispatching cost at equilibrium**

The total re-dispatching cost is 1,146 €

- **Average re-dispatching costs**

The average re-dispatching cost is 1.43 €/MWh

- **Net Welfare**

Net welfare is 23,000 €;

- **Welfare loss**

Welfare loss is 0 € w.r.t. to Model 1 (23,000 €)

Incomplete transmission pricing and socializing counter-trading costs

A fixed point problem

The average re-dispatching/counter-trading cost α incurred by the TSOs is:

$$\alpha = \frac{\sum_{i=1,2,4} \int_{q_i}^{q_i + \Delta q_i} c_i(\xi) d\xi - \sum_{j=3,5,6} \int_{q_j}^{q_j + \Delta q_j} w_j(\xi) d\xi}{\sum_{i=1,2,4} q_i}$$

This cost is charged to the users of the system. One assumes here that it is paid by the generators selling on the PXs (this is a stylized view of the problem):

Formulation: Suppose that the average counter-dispatching cost adds to the constant term (10, 15 and 42.5) of the marginal cost functions

- The fixed point problem can be solved by looping between the PX and TSO models
- Alternative arrangements can have counter-trading paid by demand nodes or by both demand and supply nodes.
- From here on we only report the results at equilibrium between the PX (market coupling) and the TSO (counter-trading)

Results of optimal cross-border counter-trading (2)

	Configuration 3/3		Configuration 4/2	
	Prod/Cons	Prod	Prod/Cons	Prod
Welfare loss	30	125	8	2,320
TRC	1,146	1,235	5,079	7,065
ARC	1.51	1.63	6.51	9.56
Net welfare	22,970	22,875	22,992	20,680
MV line (1-6)	40.00	42.22	40.00	57.05
MV line (2-5)	0.00	0.00	0.00	0.00

NOTATION:

- Welfare loss (€) are computed w.r.t. Model 1 (23,000 €);
- TRC: Total Re-dispatching Costs in €;
- ARC: Average Re-dispatching Costs in €/MWh;
- Net Welfare: welfare value at equilibrium in €;
- MV: marginal value of transmission lines in €/MWh

- **The law (third package) says that TSOs must coordinate**
 - But it does not say how
- **EU documents do not envisage an optimal cross border counter-trading**
 - (e.g. impact assessments of infrastructure document of November 2010)
- **It thus makes sense to make assumptions on lack of optimal cross border counter-trading**
 - National TSOs are not coordinated (Model 3):
 - A. National TSOs have full access to all re-dispatching resources: an internal market of counter-trading resources (model 3.1);
 - B. National TSOs have only a limited access to all re-dispatching resources: a limited internal market of counter-trading resources (model 3.2)
 - C. National TSOs manage only the re-dispatching resources in their control area: national markets of counter-trading resources (model 3.3)

Imperfect counter-trading

- 1 Nodal pricing: optimization;
- 2 Energy market clearing and optimized cross-border counter-trading: sequence of optimization or complementarity problems;
- 3 Imperfect coordination of TSOs: Generalized Nash equilibrium problems solved by optimization (Nabetani, Tseng, Fukushima 2009).

- ① Access to counter-trading resources: create an internal market of counter-trading resources (by (close) analogy with discussion on internal market of balancing resources);
- ② Create a market of interconnection line capacity (by analogy with PJM MISO interconnection);
- ③ Merger or coordination contracts between TSOs (as taking place on the market).

MODEL 3.1 an internal market of counter-trading resources; no market of line capacity (1)

Assume that each TSO can buy counter-trading services in both zones. Note $\Delta q_i^{N,S}$ where $i = 1, 2, \dots, 6$ these actions of both TSOs.

- TSO^N (with a similar problem for TSO^S)

$$\begin{aligned} \text{Min}_{\Delta q_i^N} \quad & \sum_{i=1,2,4} \int_{q_i + \Delta q_i^S}^{q_i + \Delta q_i^S + \Delta q_i^N} c_i(\xi) d\xi - \sum_{j=3,5,6} \int_{q_j + \Delta q_j^S}^{q_j + \Delta q_j^S + \Delta q_j^N} w_j(\xi) d\xi \\ \text{s.t.} \quad & \end{aligned}$$

$$\bar{F}_l - \left(\sum_{i=1,2,4} PTDF_{i,l}(q_i + \Delta q_i^N + \Delta q_i^S) - \sum_{i=3,5,6} PTDF_{i,l}(q_i + \Delta q_i^N + \Delta q_i^S) \right) \geq 0 \quad (\lambda_l^{N,+})$$

where $l = (1 - 6), (2 - 5)$

$$\sum_{i=1,2,4} \Delta q_i^N + \sum_{j=4,5,6} \Delta q_j^N = 0 \quad (\mu_l^{N,1})$$

$$\sum_{i=1,2,4} \Delta q_i^N - \sum_{j=4,5,6} \Delta q_j^N = 0 \quad (\mu_l^{N,2})$$

$$q_n + \Delta q_n^N + \Delta q_n^S \geq 0 \quad \forall n \quad (\nu_n^N)$$

MODEL 3.1 An internal market of counter-trading resources; no market of line capacity (2)

Assume that $q_n + \Delta q_n^N + \Delta q_n^S > 0$ for $\forall n$ and define the dual variables $\lambda_l^N = (-\lambda_l^{N,+} + \lambda_l^{N,-})$ for $l = ((1-6), (2-5))$. We obtain the dual conditions:

$$c_i - \sum_l \lambda_l^N \cdot PTDF_{i,l} - \mu^{N,1} + \mu^{N,2} = 0 \quad i = 1, 2, 4$$

$$-w_j + \sum_l \lambda_l^N \cdot PTDF_{j,l} - \mu^{N,1} - \mu^{N,2} = 0 \quad j = 3, 5, 6$$

Writing the same relations for TSO^S

$$c_i - \sum_l \lambda_l^S \cdot PTDF_{i,l} - \mu^{S,1} + \mu^{S,2} = 0 \quad i = 1, 2, 4$$

$$-w_j + \sum_l \lambda_l^S \cdot PTDF_{j,l} - \mu^{S,1} - \mu^{S,2} = 0 \quad j = 3, 5, 6$$

we find, if there are enough equalities (here six equalities for four variables), that $\lambda_l^N = \lambda_l^S$.

MODEL 3.1 An internal market of counter-trading resources; no market of line capacity (3)

PROPOSITION: The internal market of counter-trading resources restores the perfect counter-trading: (i) different agents resorting to the same counter-trading resource at the same price induces a price arbitrage that forces the equality of the dual variables of the common constraints (the transmission lines (ii) which has an effect equivalent to a market of line capacity) and hence (iii) leads to a single GNE in counter-trading. (iv) In mathematical terms, the solution set of the QVI is identical to the solution set of the associated VI!!

Technical note: finding solutions of QVI/GNE

The Nabetani, Tseng, Fukushima's parametrized approach is as follows:

$$\begin{aligned}
 \text{Min}_{\Delta \mathbf{q}_n^{N,S}} \quad & \sum_{i=1,2,4} \int_{q_i}^{q_i + \Delta q_i^S + \Delta q_i^N} c_i(\xi) d\xi - \sum_{j=3,5,6} \int_{q_j}^{q_j + \Delta q_j^S + \Delta q_j^N} w_j(\xi) d\xi + \\
 & + \sum_l (\gamma_l^{N,+} - \gamma_l^{N,-}) \cdot \left(\sum_{i=1,2,4} PTDF_{i,l} \cdot \Delta q_i^N - \sum_{j=3,5,6} PTDF_{j,l} \cdot \Delta q_j^N \right) \\
 & + \sum_l (\gamma_l^{S,+} - \gamma_l^{S,-}) \cdot \left(\sum_{i=1,2,4} PTDF_{i,l} \cdot \Delta q_i^S - \sum_{j=3,5,6} PTDF_{j,l} \cdot \Delta q_j^S \right) \\
 \text{s.t.} \quad & \\
 \bar{F}_l - \left(\sum_{i=1,2,4} PTDF_{i,l}(q_i + \Delta q_i^N + \Delta q_i^S) - \sum_{j=3,5,6} PTDF_{j,l}(q_j + \Delta q_j^N + \Delta q_j^S) \right) \geq 0 \quad & (\lambda_l^+) \\
 \sum_{i=1,2,4} \Delta q_i^Z + \sum_{j=3,5,6} \Delta q_j^Z = 0 \quad & Z = N, S \quad (\mu_l^{Z,1}) \\
 \sum_{i=1,2,4} \Delta q_i^Z + \sum_{j=3,5,6} \Delta q_j^Z = 0 \quad & Z = N, S \quad (\mu_l^{Z,2}) \\
 q_n + \Delta q_n^N + \Delta q_n^S \geq 0 \quad \forall n \quad & (\nu_n^Z) \quad Z = N, S
 \end{aligned}$$

MODEL 3.2: A restricted internal market of counter-trading resources

(1)

Each TSO can buy counter-trading services in both zones, but purchase in other zone is limited.

- **TSO^N (with a similar problem for TSO^S)**

$$\text{Min}_{\mathbf{q}_n^N} \sum_{i=1,2,4} \int_{q_i + \Delta q_i^S}^{q_i + \Delta q_i^N + \Delta q_i^S} c_i(\xi) d\xi - \sum_{j=3,5,6} \int_{q_j + \Delta q_j^S}^{q_j + \Delta q_j^N + \Delta q_j^S} w_j(\xi) d\xi \quad s.t.$$

$$\bar{F}_l - \left(\sum_{i=1,2,4} PTDF_{i,l}(q_i + \Delta q_i^N + \Delta q_i^S) - \sum_{j=3,5,6} PTDF_{j,l}(q_j + \Delta q_j^N + \Delta q_j^S) \right) \geq 0 \quad (\lambda_l^{N,+})$$

where $l = (1 - 6), (2 - 5)$

$$\begin{aligned} \sum_{i=1,2,4} \Delta q_i^N + \sum_{j=3,5,6} \Delta q_j^N &= 0 && (\mu_l^{N,1}) \\ \sum_{i=1,2,4} \Delta q_i^N - \sum_{j=3,5,6} \Delta q_j^N &= 0 = 0 && (\mu_l^{N,2}) \\ q_n + \Delta q_n^N + \Delta q_n^S &\geq 0 \quad \forall n && (\nu_n^N) \\ -\Delta q_n^N \leq \Delta q_n^N \leq \Delta q_n^N &&& n = 4, 5, 6 \quad (\eta_n^{N,\pm}) \end{aligned}$$

MODEL 3.2: A restricted internal market of counter-trading resources (2)

A FIRST RESULT: The implicit market of interconnection line capacity is lost when TSOs have limited access to counter-trading resources in other zones. This introduces inefficiencies; these can be more or less important depending on whether one does or does not introduce a market for transmission.

MAIN QUESTION: How far can one go in deteriorating the efficiency of counter-trading and hence the overall efficiency of market coupling?

Results of Model 3.2 (1)

Market configuration 3/3 with a market of interconnection capacity

Trading interconnection capacities among TSOs (setting $\gamma_i^{N/S,\pm} = 0$) under the following counter-trading resource restrictions, counter-trading remains relatively efficient:

$\overline{\Delta q_1^S}$	$\overline{\Delta q_2^S}$	$\overline{\Delta q_3^S}$	$\overline{\Delta q_4^N}$	$\overline{\Delta q_5^N}$	$\overline{\Delta q_6^N}$
33.33	16.67	8.33	16.67	8.33	16.67

	Configuration 3/3	
	Prod/Cons	Prod
Welfare loss	30	125
TRC	1,146	1,235
ARC	1.51	1.63
Net welfare	22,970	22,875
MV line (1-6)	40.00	42.22
MV line (2-5)	0.00	0.00
$\gamma_i^{N/S,\pm}$	0.00	0.00

Results of Model 3.2 (2)

Market configuration 3/3 without market of line capacity

Eliminating trade of transmission capacities (setting $\gamma_{(1-6)}^{N,+} = 60$ and $\gamma_{(1-6)}^{S,+} = 0$) and keeping the same limits on counter-trading resources, restrictions degrades the efficiency of counter-trading:

	Configuration 3/3	
	Prod/Cons	Prod
Welfare loss	396	494
TRC	1,490	1,580
ARC	2	2.13
Net welfare	22,604	22,506
MV line (1-6)	22.67	27.68
MV line (2-5)	0.00	0.00
$\gamma_{(1-6)}^{N,+}$	60.00	60.00
$\gamma_{(1-6)}^{S,+}$	0.00	0.00

Results of Model 3.2 (3)

Market configuration 4/2 with a market of line capacity

Setting $\gamma_i^{N/S,\pm} = 0$ under the following counter-trading resource restrictions, the result can be very bad depending on how one organizes counter-trading, even in presence of a transmission market:

$\overline{\Delta q_1^S}$	$\overline{\Delta q_2^S}$	$\overline{\Delta q_3^S}$	$\overline{\Delta q_4^N}$	$\overline{\Delta q_5^N}$	$\overline{\Delta q_6^S}$
72.48	22.48	94.96	94.96	34.98	59.98

	Configuration 4/2	
	Prod/Cons	Prod
Welfare loss	8	infeasible
TRC	5,079	infeasible
ARC	6.51	infeasible
Net welfare	22,992	infeasible
MV line (1-6)	40.00	infeasible
MV line (2-5)	0.00	infeasible
$\gamma_l^{N/S,\pm}$	0.00	0.00

Results of Model 3.2 (4)

Market configuration 4/2 without market of line capacity

Setting $\gamma_{(1-6)}^{N,+} = 60$ and $\gamma_{(1-6)}^{S,+} = 0$ and keeping the same limits on counter-trading resources restrictions, one has for configuration 4/2:

	Configuration 4/2	
	Prod/Cons	Prod
Welfare loss	2,472	infeasible
TRC	7,191	infeasible
ARC	9.76	infeasible
Net welfare	20,528	infeasible
MV line (1-6)	18.16	infeasible
MV line (2-5)	0.00	infeasible
$\gamma_{(1-6)}^{N,+}$	60.00	60.00
$\gamma_{(1-6)}^{S,+}$	0.00	0.00

MODEL 3.2: Quantitative constraints on counter-trading resources (3)

A SECOND RESULT: Not only the implicit coordination is lost when TSOs have limited access to counter-trading resources in other zones, but counter-trading can become impossible in some zonal markets (in this case example 4/2) (as encountered in the single zone Sweden).

A THIRD RESULT: Even when counter-trading is possible (examples 3/3 and 4/2) it can become extremely inefficient in the absence of a market for transmission capacities (different γ).

MODEL 3.3: Domestic counter-trading resources (1)

Assume that each TSO can only buy counter-trading services in its zone.

- **TSO^N (similar problem for the TSO^S)**

$$\text{Min}_{\Delta q_n^N} \quad \sum_{i=1,2} \int_{q_i}^{q_i + \Delta q_i^N} c_i(\xi) d\xi - \int_{q_3}^{q_3 + \Delta q_3^N} w_3(\xi) d\xi$$

s.t.

$$\begin{aligned} \bar{F}_l - \left(\sum_{i=1,2} PTDF_{i,l}(q_i + \Delta q_i^N) + PTDF_{4,l}(q_4 + \Delta q_4^S) + \right. \\ \left. - PTDF_{3,l}(q_3 + \Delta q_3^N) - \sum_{j=5,6} PTDF_{j,l}(q_j + \Delta q_j^S) \right) \geq 0 \quad (\lambda_l^+) \end{aligned}$$

where $l = (1 - 6), (2 - 5)$

$$\Delta q_1^N + \Delta q_2^N + \Delta q_3^N = 0 \quad (\mu_l^{N,1})$$

$$\Delta q_3^N - \Delta q_1^N - \Delta q_2^N = 0 \quad (\mu_l^{N,2})$$

$$q_n + \Delta q_n^N \geq 0 \quad n = 1, 2, 3$$

Results of Model 3.3 (1)

Only imposing that each TSO remains in balance, even when assuming a transmission market (setting all the weight $\gamma_i^{N/S,\pm} = 0$) can make the situation difficult:

	Configuration 3/3		Configuration 4/2	
	Prod/Cons	Prod*	Prod/Cons*	Prod
Welfare loss	1,454	3,096	3,009	infeasible
TRC	2,442	3,781	7,629	infeasible
ARC	3.45	5.88	10.50	infeasible
Net welfare	21,546	19,904	19,991	infeasible
MV line (1-6)	146.67	220.00	82.30	infeasible
MV line (2-5)	0.00	0.00	0.00	infeasible
$\gamma_{N/S,\pm}$	0.00	0.00	0.00	infeasible

* These scenarios admit always the same solution whatever γ considered.

Results of Model 3.3 (2)

When setting $\gamma_{(1-6)}^{N,+} = 60$ and $\gamma_{(1-6)}^{S,+} = 0$ (eliminating the transmission market), the situation becomes dramatic:

	Configuration 3/3		Configuration 4/2	
	Prod/Cons	Prod	Prod/Cons	Prod
Welfare loss	1,555	3,096	3,009	infeasible
TRC	2,529	3,781	7,629	infeasible
ARC	3.60	5.88	10.50	infeasible
Net welfare	21,445	19,904	19,991	infeasible
MV line (1-6)	106.67	160.00	82.30	infeasible
MV line (2-5)	0.00	0.00	0.00	infeasible
$\gamma_{(1-6)}^{N,+}$	60.00	60.00	60.00	60.00
$\gamma_{(1-6)}^{S,+}$	0.00	0.00	0.00	0.00

MODEL 3.3: Segmented market of counter-trading resources (2)

A GENERAL OBSERVATION: Counter-trading efficiency further and dramatically deteriorates when one completely segments the counter-trading resources market.

AN ADDITIONAL RESULT: Even when counter-trading is possible (example 3/3) it can become extremely inefficient in the absence of a market for transmission capacities (different γ).

Summing up on this example and barring incentives to game counter-trading

Nodal pricing is, as expected, the best system.

Integrating counter-trading services and TSOs does well.

Integrating counter-trading resources, even without a transmission market does as well (but requires drastic harmonization of market design between zones).

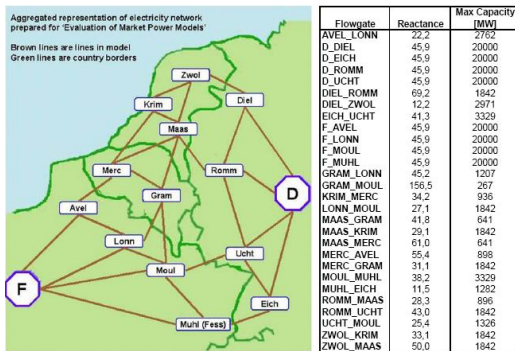
Partially segmenting the counter-trading resources, with or without a transmission market can seriously degrade efficiency and even make counter-trading impossible.

Totally segmenting counter-trading resources, with or without a transmission market further deteriorates efficiency.

Case Study

A toy model of Central Western European (CWE) Market:

Market coupling is currently operated among Belgium, France and the Netherlands and Germany.



SOURCE: Energy research Centre of the Netherlands (ECN) website

Model 1: Nodal Model

Central Western European Market

MAIN RESULTS

Considering different demand scenarios of the nodal model, we obtain the following results:

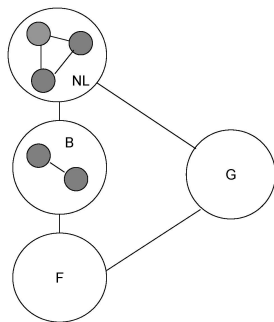
Demand level	Social Welfare (M€)
Reference	267,124
Increase 5%	279,254
Increase 10%	291,080
Increase 20%	313,592

Table: Welfare of different nodal model scenarios

Market Coupling

Stylized Central Western European Market

PXs solve a welfare maximization problem while taking into account the following stylized representation of the transmission network:



The social welfare resulting from the clearing of the energy market, before removing violations of line constraints, amounts to 267,571 M€.

MAIN RESULTS

All TSOs coordinate counter-trading. Results for different demand scenarios:

Demand level	Total Re-dispatching costs (M€)	Average Re-dispatching costs (€/MWh)	Welfare (PX) (M€)
Reference	450	0.37	267,120
Increase 5%	431	0.35	279,249
Increase 10%	550	0.43	291,066
Increase 20%	322	0.24	313,590

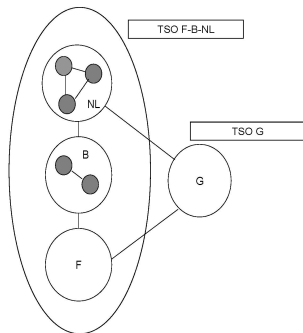
Table: Welfare and re-dispatching costs

Welfare losses respectively amount to 4, 5, 14 and 2 million €/year w.r.t. the values obtained in Models 1.

Model 3.1: Model A Trilateral TSO (1)

Uncoordinated Counter-Trading

Only one TSO operates in the market. This coordinates the re-dispatching activities inside and on the interconnections of France, Belgium and the Netherlands. This market organization is depicted as follows:



Model 3.1: A Trilateral TSO (2)

Uncoordinated Counter-Trading

MAIN RESULTS

Total Re-dispatching costs (M€)	Average Re-dispatching costs (€/MWh)	Welfare (PX) (M€)
455	0.38	267,116

Table: Welfare and re-dispatching costs

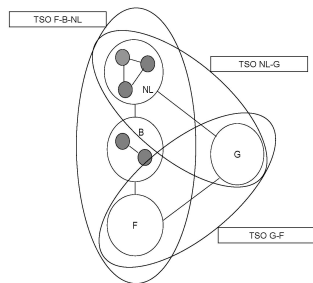
Welfare losses amount to 4 and 8 million €/year w.r.t. the reference values obtained in Models 1 and 2 respectively.

Multilateral Arrangement: Model 3.2 (1)

Uncoordinated Counter-Trading

Three TSOs operate in the market:

- (F-B-NL) TSO manages the re-dispatching activities in France, Belgium and the Netherlands;
- (G-NL) TSO manages the re-dispatching activities in Germany and in the Netherlands;
- (G-F) TSO manages the re-dispatching activities in Germany and in France



Multilateral Arrangement: Model 3.2 (2)

Uncoordinated Counter-Trading

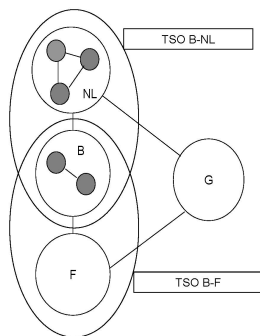
MAIN RESULT: one restores the efficiency of an integrated counter-trading

This model creates arbitrage possibilities between TSOs that have un-discriminatory access to common counter-trading resources. This assumption allows TSOs to implicitly coordinate their action: we fall back on the results of Model 2 where we consider an explicit coordination.

Two Bilateral TSOs: Model 3.3 (1)

Uncoordinated Counter-Trading

Two TSOs operate in the market. They manage congestion on the interconnection lines between France and Belgium (**note** as is the case between RTE (F) and Elia (B)) and Belgium and the Netherlands (as is not the case between Elia (B) and TenneT (NL)). One is the (F-B) TSO and the other is the (B-NL) TSO. They share counter-trading resources in Belgium as illustrated in the following picture:



Two Bilateral TSOs: Model 3.3 (2)

Uncoordinated Counter-Trading

MAIN RESULTS

Variation limits for (B-NL) TSO	Total Re-dispatching cost (M€)	Average Re-dispatching costs (€/MWh)	Welfare (PX) (M€)
936	455	0.38	267,116
936*0.5	455	0.38	267,116
936*0.1	460	0.38	267,111

Table: (B-NL) has limited action in Belgium: degradation with respect to Model 2

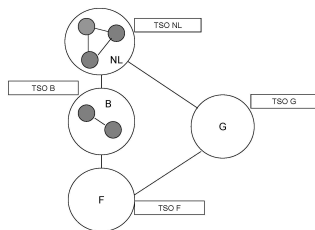
Variation limits for (F-B) TSO	Total Re-dispatching cost (M€)	Average Re-dispatching costs (€/MWh)	Welfare (PX) (M€)
898	455	0.38	267,116
898*0.5	455	0.38	267,116
898*0.1	656	0.55	266,914

Table: (F-B) has limited action in Belgium: degradation with respect to Model 2
Welfare losses amount to 5 and 202 million € for the cases “936*0.1” and

An Uncoordinated Counter-Trading with Four TSOs: Model 3.4 (1)

Uncoordinated Counter-Trading

There are four TSOs: one per each national market. None of the TSOs controls the interconnection lines:



This problem is **infeasible**, but feasibility can be restored with a significant investment in the grid (in practice by reducing ATC for the PXs).

MAIN RESULTS

This segmentation of the TSOs' action implies market inefficiencies as results show:

- Welfare amounts to 264,182 € (loss of 2.9 billion €/year w.r.t. the welfare of Model 1);
- High average re-dispatching costs in Belgium (4.32 €/MWh) and in the Netherlands (35.67 €/MWh);
- No re-dispatching costs in France and in Germany

Conclusions

- ① Counter-trading can be costly: this has indeed been observed in practice e.g. ERCOT;
- ② As expected the less coordination, the more costly it can be;
- ③ Counter-trading can even be impossible (also observed in practice (e.g. PECO, Sweden))