On-line Booking and Revenue Management: Evidence from a Low-Cost Airline

Claudio Piga

Loughborough University and Rimini Centre for Economic Analysis

Seminar at Fondazione Eni Enrico Mattei

Introduction

- In three influential papers, Dana analysed how revenue management can be effectively used when capacity is costly and firms set prices BEFORE demand is known.
- In all these papers, price dispersion arises as a consequence of the assumptions of the model, and it does not imply a carrier's intention to price discriminate.
- A crucial assumption is that the airlines have to commit to a pricing schedule and will not update it; i.e., the solutions are not sub-game perfect.

Price Dispersion & Demand uncertainty – Dana (1999, Rand)

- Costly capacity and prices set before the actual realisation of demand is known;
- in practice, the firm has to decide the level of prices and the associated number of seats it will sell for each possible realization of demand.
- For the case of two-states demand (low and high), the firm will set two prices and the corresponding number of tickets available at each price.
- The analysis consider the case in which the firm operates in different market structures.

Dana (1999, Rand)

- Dana shows that regardless of the market structure, the firm should determine different ``batches'' of seats, and that fares should increase as fewer batches remain unsold.
- That is, the profile of fare should be an increasing function of the number of sold seats.
- The domain over which this function is distributed should increase with the degree of competition on a route or market
- There is no room for intertemporal price discrimination in Dana's work.

Eq. Supply Price Distributions

FIGURE 5

CUMULATIVE PRICE DISTRIBUTIONS AND MARKET DEMAND



Price support increases with competition.

Further from Dana (1999)

- Another important feature of the model is the commitment of the firm to the schedule of prices it set before demand is known.
- Such a price rigidity may arise because the firm must incur a very high cost in tracking the evolution of demand for all the flights it operates and adjust fares to reflect demand conditions.
- This appears to run contrary to the current standard practice in the industry.

Literature

- There are no studies that try to link the paid fare for a seat on a flight with the number of available seats on that flight.
- Escobari and Li Gan (2006, NBER) and Puller, Sengupta and Wiggins (2009, NBER) try to obtain this information by merging two different dataset; their analysis is complicated by the complexity of Full Service Carriers' Yield Management, that considers a number of ticket classes that are open all at the same time.
- This work benefits from dealing with the simpler system of a Low Cost Carrier, and allows a more direct test of the implications of Dana's model.

Literature

- Implicitly, this paper studies the effect of (stochastic) peak load pricing on Fare Dispersion;
- Previous literature has mainly looked into the relationship between Price Discrimination and Price Dispersion (Gerardi and Shapiro, JPE 2009; Borenstein and Rose, 1994; Gaggero and Piga, 2010)

A quote from EU CC investigation of the FR and AL takeover

- The first software type which both companies use is a system that tracks the booking status of each flight, provides forecasts for the further development and makes proposals for the pricing pattern.
- This software allows the responsible "yield manager" or "analyst" to verify the booking status for any given Ryanair or Aer Lingus flight.
- With the help of the program, the analyst can compare the actual booking status (or "load factor") of a flight with the booking forecast which is provided by the system.
- This booking forecast is based on previous experience with the same route at the relevant dates or on similar routes. The forecasts are adjusted according to forecasted growth and other relevant changes of the factors affecting supply and demand on the route.

Study objectives

- Derive a pricing curve for Ryanair, a European Low Cost Carrier;
- Test the hypothesis of the relationship between price dispersion and market structure.
- Assess whether and how the adjustment to a "pricing" template are made, i.e., assess whether the commitment story by Dana has important implications

LCA Business Model Characteristics



THE FLIGHT IS ONLY 99p ... BUT IT WILL BE ANOTHER ÉIZO IF YOU WANT TO DO IT INSIDE THE PLANE !

LCA Business Model Characteristics

- 1. Simple pricing structures **one passenger class**; fares only cover basic transport
- 2. Each leg priced independently;
- **3.** Direct selling internet bookings, electronic tickets, no seat reservations
- 4. Point-to-point networks using cheaper, less congested airports
- 5. Intensive aircraft usage (25-min turnaround times)
- 6. Multiple role employees (flight attendants-cleaners-gate agents)
- Highly standardised fleets (Ryanair operates only Boeing 737 with 189 seats each)

Data Collection #1

- Primary data on posted fares and secondary data on routes' traffic
- posted fares collected using an "electronic spider" from main LCAs (inc, Ryanair, Buzz, Easyjet, GoFly)
- Only for Ryanair, data on seats availability could be obtained for up to 50 seats
- This was possible due to the features of the carrier's on-line reservation system
- Period for this study: 2004-June 2005

Data Collection #2

- Fares cover routes from/to UK, inc.
 domestic and main European destinations
- LCA fares collected for "booking days before departure" at intervals of 1, 4, 7, 10, 14, 21, 28, 35, 42, 49, 56, 63 and 70 days
- Data on routes' traffic (inc load factors) obtained from the CAA

An example of data

| reserve | Restore | Sort << |) >> H | ide De | lete | | | | | | |
|---------|------------|---------------|---------------------------------------|--------|---------|----------|----------|--------------|------------|--------|---|
| | | are[345346] = | · · · · · · · · · · · · · · · · · · · | | | | | | | | |
| | datedepart | booking_day | priceuk | fare | avseats | inv_seat | max_fare | discrimina~2 | arbitrage2 | d_fare | |
| 345346 | 03ju12004 | 1 | 99.99 | 139.99 | 10 | 40 | 139.99 | | | 40 | |
| 345347 | 03ju12004 | 4 | 59.99 | 139.99 | 16 | 34 | 139.99 | | | 80 | |
| 345348 | 03ju12004 | 7 | 34.99 | 139.99 | 23 | 27 | 139.99 | | | 105 | |
| 345349 | 03ju12004 | 10 | 29.99 | 139.99 | 29 | 21 | 139.99 | 82 | | 110 | |
| 345350 | 03ju12004 | 14 | 11.99 | 139.99 | 35 | 15 | 139.99 | | | 128 | |
| 345351 | 03ju12004 | 21 | 19.99 | 139.99 | 44 | 6 | 139.99 | | | 120 | |
| 345352 | 03ju12004 | 28 | 34.99 | 139.99 | 47 | 3 | 139.99 | 82 | | 105 | |
| 345353 | 03ju12004 | 35 | 29.99 | 99.99 | 50 | 0 | 139.99 | | • | 70 | - |
| 345354 | 03ju12004 | 42 | 34.99 | 79.99 | 50 | 0 | 139.99 | <u>ja</u> | | 45 | |
| 345355 | 03ju12004 | 49 | 34.99 | 59.99 | 50 | 0 | 139.99 | | | 25 | |
| 345356 | 03ju12004 | 56 | 34.99 | 59.99 | 50 | 0 | 139.99 | | | 25 | |
| 345357 | 03ju12004 | 63 | | 59.99 | 50 | 0 | 139.99 | 14 | - | 12 | |
| 345358 | 03jul2004 | 70 | 19.99 | 59.99 | 50 | 0 | 139.99 | | | 40 | |
| 345359 | 10jul2004 | 1 | 99.99 | 139.99 | 10 | 40 | 139.99 | | | 40 | |
| 345360 | 10jul2004 | 4 | 79.99 | 139.99 | 14 | 36 | 139.99 | 82 | | 60 | |
| 345361 | 10jul2004 | 7 | 29.99 | 139.99 | 15 | 35 | 139.99 | | | 110 | |
| 345362 | 10jul2004 | 10 | 44.99 | 139.99 | 21 | 29 | 139.99 | 34 | | 95 | |
| 345363 | 10jul2004 | 14 | 39.99 | 139.99 | 24 | 26 | 139.99 | | | 100 | |
| 345364 | 10jul2004 | 21 | 39.99 | 139.99 | 31 | 19 | 139.99 | | | 100 | |
| 345365 | 10jul2004 | 28 | 44.99 | 139.99 | 32 | 18 | 139.99 | 14 | | 95 | |
| 345366 | 10jul2004 | 35 | 39.99 | 139.99 | 40 | 10 | 139.99 | | | 100 | |
| 345367 | 10jul2004 | 42 | 29.99 | 119.99 | 50 | 0 | 139.99 | | | 90 | |
| 345368 | 10jul2004 | 49 | 34.99 | 99.99 | 50 | 0 | 139.99 | 82 |) a (| 65 | |
| 345369 | 10jul2004 | 56 | 29.99 | 59.99 | 50 | 0 | 139.99 | | | 30 | |
| 345370 | 10jul2004 | 63 | 29.99 | 59.99 | 50 | 0 | 139.99 | 5. | | 30 | |
| 345371 | 10jul2004 | 70 | <u> </u> | 49.99 | 50 | 0 | 139.99 | 14 | 1 | | |
| 345372 | 17jul2004 | 1 | | | | 50 | 149.99 | | | | |
| 345373 | 17jul2004 | 4 | 129.99 | 149.99 | 14 | 36 | 149.99 | 14 | | 20 | |
| 345374 | 17jul2004 | 7 | 129.99 | 149.99 | 14 | 36 | 149.99 | | | 20 | |
| 345375 | 17jul2004 | 10 | 129.99 | 149.99 | 14 | 36 | 149.99 | | • | 20 | |
| 345376 | 17jul2004 | 14 | 19.99 | 149.99 | 23 | 27 | 149.99 | 8 | S | 130 | |
| 345377 | 17jul2004 | 21 | 39.99 | 149.99 | 43 | 7 | 149.99 | | | 110 | |
| 345378 | 17jul2004 | 28 | 39.99 | 149.99 | 50 | 0 | 149.99 | 3 4 | | 110 | |
| 345379 | 17jul2004 | 35 | 39.99 | 129.99 | 50 | 0 | 149.99 | 1 | | 90 | |

Fixed Upper Boundary



The revenue management software defines a maximum threshold which corresponds to the price of the last seat.

This can be obtained by any query that closes the flight.

The threshold is independent of the current occupancy rate.

Fixed Upper Boundary



Gatwick - Dublin



Gatwick – Dublin - Lnprice



London Stansted-Berlin



London Stansted-Berlin - Inprice



Bristol - Dublin



Bristol- Dublin - Lnprice



Monotonic Prices? Not always!

Table 1: Percentage of price decreases relative to previous booking day, by booking day and remaining capacity.

| Days from | Available | | | | | | | |
|-----------|-----------|---------|-------|---------|-------|--|--|--|
| Take-off | | seats | | | | | | |
| | 1-9 | 10 - 19 | 20-29 | 30 - 39 | 40-49 | | | |
| 1 | 0.04 | 0.02 | 0.02 | 0.01 | 0.01 | | | |
| 4 | 0.05 | 0.06 | 0.05 | 0.05 | 0.05 | | | |
| 7 | 0.07 | 0.10 | 0.10 | 0.11 | 0.11 | | | |
| 10 | 0.09 | 0.11 | 0.12 | 0.12 | 0.14 | | | |
| 14 | 0.14 | 0.16 | 0.18 | 0.22 | 0.24 | | | |
| 21 | 0.08 | 0.13 | 0.13 | 0.19 | 0.21 | | | |
| 28 | 0.09 | 0.10 | 0.14 | 0.18 | 0.19 | | | |
| 35 | 0.06 | 0.05 | 0.12 | 0.16 | 0.13 | | | |
| 42 | 0.10 | 0.13 | 0.11 | 0.15 | 0.15 | | | |
| 49 | 0.04 | 0.06 | 0.07 | 0.13 | 0.12 | | | |
| 56 | 0.00 | 0.15 | 0.07 | 0.09 | 0.16 | | | |
| 63 | 0.05 | 0.06 | 0.11 | 0.13 | 0.21 | | | |

Note: percentages were calculated only if two consecutive available seats were below the censored value of 50.

Monotonic Prices

Table 2: Percentage of price decreases relative to previous booking day, by booking day and season.

| • | | | | | |
|-----------|--------|--------|--------|--------|--------|
| Days from | Aug03- | Nov03- | Apr04- | Nov04- | Apr05- |
| Take-off | Oct03 | Mar04 | Oct04 | Mar05 | Jun05 |
| 1 | 0.04 | 0.03 | 0.02 | 0.02 | 0.03 |
| 4 | 0.06 | 0.09 | 0.04 | 0.02 | 0.03 |
| 7 | 0.17 | 0.12 | 0.07 | 0.10 | 0.07 |
| 10 | 0.16 | 0.18 | 0.08 | 0.10 | 0.07 |
| 14 | 0.30 | 0.29 | 0.20 | 0.25 | 0.23 |
| 21 | 0.31 | 0.30 | 0.20 | 0.28 | 0.27 |
| 28 | 0.35 | 0.33 | 0.21 | 0.30 | 0.29 |
| 35 | 0.34 | 0.34 | 0.20 | 0.32 | 0.26 |
| 42 | 0.31 | 0.33 | 0.19 | 0.31 | 0.21 |
| 49 | 0.28 | 0.35 | 0.18 | 0.31 | 0.21 |
| 56 | 0.30 | 0.37 | 0.18 | 0.30 | 0.19 |
| 63 | 0.32 | 0.36 | 0.17 | 0.25 | 0.18 |

Note: percentages were calculated without controlling for available seats.

Estimation

- Available seats are measured from 49 to 1
- So av_seat is censored.
- The variable used in the estimation is
- Inv_seat=50 av_seat (this gives a positive slope).
- Estimates are obtained assuming that inv_seat (or av_seat) is exogenous
- But consider the following:

Panel Fixed Effect

We want to estimate

$$p_{it} = \beta_1 Q_{it} + \beta_2 X_{it} + \delta_i + \varepsilon_{it}$$

i is a flight, *t* identifies booking days. We cannot rule out that Q_{it} and p_{it} , are both correlated with ε_{it} and that they are jointly determined; hence we treat Q_{it} as endogenous.

Following Wooldridge, the instrument used is the *expected value* of av_seat, obtained from a Tobit model that includes as regressors many factors which could be interpreted as demand shifters. These are:

i.booking_day d_base_both d_promo i.day_week shr_fli_city_subp ln_dist d_deptime ///

n_route_comp_in_city n_flights_tot_route n_flights_tot_city
n_flights_comp_city n_flights_comp_route

Any correlation with δ_i is taken care of by the fixed effect estimator.

Basic Model – FE Dependent: Ln(Price)

| | xtreg1 | xtiv1 | xtreg2 | xtiv2 | xtreg3 | xtiv3 |
|------------|----------|----------|----------|----------|----------|----------|
| inv coot | 0.0440 | 0.043a | 0.036a | 0.042a | 0.030a | 0.040a |
| inv_seat | 0.044a | 0.043a | | | | |
| book_day1 | | | 0.232a | 0 | 0.360a | 0 |
| book_day4 | | | -0.026 | -0.230a | 0.085 | -0.233a |
| book_day7 | | | -0.228a | -0.399a | -0.118b | -0.384a |
| book_day10 | | | -0.222a | -0.362a | -0.130b | -0.349a |
| book_day14 | | | -0.369a | -0.474a | -0.214a | -0.380a |
| book_day21 | | | -0.277a | -0.337a | -0.167a | -0.261a |
| book_day28 | | | -0.180a | -0.207a | -0.120b | -0.164a |
| book_day35 | | | -0.104b | -0.110a | -0.076 | -0.085a |
| book_day42 | | | -0.064 | -0.061 | -0.029 | -0.025 |
| book_day49 | | | -0.025 | -0.017 | 0.01 | 0.022 |
| book_day56 | | | 0.031 | 0.045 | 0.035 | 0.056c |
| book_day63 | | | -0.017 | -0.019 | -0.007 | -0.01 |
| d_promo1 | | | | | -4.625a | -4.563a |
| Constant | 2.850a | 2.871a | 3.172a | 3.164a | 3.240a | 3.228a |
| R-2w | 0.42 | 0.42 | 0.47 | 0.46 | 0.72 | 0.71 |
| r2_o | 0.220705 | 0.220705 | 0.278009 | 0.272155 | 0.563943 | 0.545522 |

Does Ryanair update? Maybe yes

| • | | xtreg4 | xtiv4 | xtreg5 | xtiv5 | xtreg6 | xtiv6 | |
|---|-------------|---------|---------|---------|---------|---------|---------|--------|
| • | | | | | | | | |
| • | inv_seat | 0.030a | 0.041a | 0.029a | 0.038a | 0.028a | 0.037a | |
| • | book_day1 | 0.274a | 0 | 0.261a | 0 | 0.264a | 0 | |
| • | book_day4 | -0.003 | -0.231a | -0.022 | -0.241a | -0.021 | -0.248a | |
| ٠ | book_day7 | -0.208a | -0.379a | -0.232a | -0.402a | -0.235a | -0.416a | |
| • | book_day10 | -0.221a | -0.341a | -0.251a | -0.376a | -0.259a | -0.398a | |
| • | book_day14 | -0.317a | -0.397a | -0.342a | -0.431a | -0.337a | -0.440a | |
| • | book_day21 | -0.277a | -0.316a | -0.278a | -0.330a | -0.257a | -0.319a | |
| • | book_day28 | -0.187a | -0.194a | -0.189a | -0.209a | -0.175a | -0.203a | |
| • | book_day35 | -0.073 | -0.088a | -0.079c | -0.090a | -0.084c | -0.093a | |
| • | book_day42 | -0.021 | -0.021 | -0.026 | -0.024 | -0.03 | -0.027 | |
| • | book_day49 | 0.018 | 0.024 | 0.016 | 0.023 | 0.013 | 0.022 | |
| • | book_day56 | 0.042 | 0.061c | 0.043 | 0.059c | 0.039 | 0.056c | |
| • | book_day63 | -0.005 | -0.009 | -0.005 | -0.01 | -0.006 | -0.009 | |
| ٠ | d_promo1 | -4.630a | -4.578a | -4.628a | -4.578a | -4.634a | -4.582a | |
| • | uncert21_30 | 0.171a | 0.185a | | | | | |
| • | uncert14_30 | 0.034c | 0.005 | | | | | |
| • | uncert10_30 | -0.044b | -0.146a | | | | | |
| • | uncert21_25 | | | 0.132a | 0.152a | | | |
| • | uncert14_25 | | | 0.088a | 0.070a | | | |
| • | uncert10_25 | | | 0.014 | -0.072a | | | |
| ٠ | uncert21_20 | | | | | 0.082a | 0.107a | |
| ٠ | uncert14_20 | | | | | 0.076a | 0.065a | |
| • | uncert10_20 | | | | | 0.117a | 0.049a | |
| ٠ | Constant | | 3.314a | 3.252a | 3.336a | 3.289a | 3.342a | 3.308a |
| ٠ | R-2w | 0.72 | 0.71 | 0.72 | 0.71 | 0.72 | 0.71 | |
| • | r2 n | 0.58 | 0 55 | 0 58 | 0.56 | 0.58 | 0.56 | |

Maybe No

| | xtreg4 | xtiv4 | xtreg5 | xtiv5 | xtreg6 | xtiv6 |
|---|------------------------|---|------------------------|------------------------------|----------------------------|-----------------------------|
| inv_seat d_promo1 uncert21_30 uncert14_30 uncert10_30 | | 0.047a -4.603a 0.057a -0.147a -0.222a | 0.042a -4.637a | 0.044a -4.614a | 0.041a -4.640a | 0.041a -4.629a |
| uncert21_25 uncert14_25 uncert10_25 | -0.100a | -0.2224 | | 0.033b -0.092a -0.157a | 0.000 | 0.011 |
| uncert21_20 uncert14_20 uncert10_20 | | | | | 0.008 -0.092a -0.016 | 0.011 -0.094a -0.034a |
| Constant R2w r2_o | 2.989a 0.68 0.50 | 2.937a 0.68 0.50 | 2.985a 0.68 0.50 | 2.950a 0.68 0.50 | 2.995a 0.67 0.50 | 2.979a 0.67 0.50 |

Market Structure? Maybe no

| | Mono | opoly | Duo-Ti | riopoly |
|------------|---------|---------|---------|---------|
| | xtreg3 | xtiv3 | xtreg4 | xtiv4 |
| | | | | |
| inv_seat | 0.029a | 0.040a | 0.035a | 0.039a |
| book_day1 | 0.400a | 0 | 0.175c | 0 |
| book_day4 | 0.122c | -0.230a | -0.094 | -0.248a |
| book_day7 | -0.077 | -0.373a | -0.303a | -0.431a |
| book_day10 | -0.087 | -0.330a | -0.322a | -0.430a |
| book_day14 | -0.164b | -0.347a | -0.430a | -0.513a |
| book_day21 | -0.114c | -0.218a | -0.383a | -0.430a |
| book_day28 | -0.08 | -0.128a | -0.285a | -0.309a |
| book_day35 | -0.064 | -0.070b | -0.145b | -0.156a |
| book_day42 | -0.026 | -0.019 | -0.051 | -0.052 |
| book_day49 | 0.017 | 0.034 | -0.031 | -0.032 |
| book_day56 | 0.047 | 0.077b | -0.039 | -0.04 |
| book_day63 | 0.017 | 0.017 | -0.131b | -0.141c |
| d_promo1 | -4.687a | -4.617a | -4.391a | -4.362a |
| Constant | 3.251a | 3.231a | 3.235a | 3.240a |
| R-2w | 0.71 | 0.7 | 0.75 | 0.75 |
| r2_o | 0.55 | 0.53 | 0.63 | 0.62 |

Market Structure? Maybe yes

| | Mone | opoly | Duo-Triopoly | | |
|----------|---------|---------|--------------|---------|--|
| | xtreg3 | xtiv3 | xtreg4 | xtiv4 | |
| | | | | | |
| inv_seat | 0.038a | 0.039a | 0.044a | 0.042a | |
| d_promo1 | -4.707a | -4.700a | -4.435a | -4.463a | |
| Constant | 3.057a | 3.047a | 2.818a | 2.854a | |
| | | | | | |
| R-2w | 0.66 | 0.66 | 0.71 | 0.71 | |
| r2_o | 0.5 | 0.5 | 0.56 | 0.56 | |

FULL SAMPLE

| | xtreg1 | xtiv1 | xtreg2 | xtiv2 | xtreg3 | xtiv3 |
|------------|--------|--------|---------|---------|---------|---------|
| inv_seat | 0.046a | 0.084a | 0.004a | 0.083a | 0.012a | 0.061a |
| book_day1 | | | 2.158a | 0 | 1.370a | 0 |
| book_day4 | | | 1.724a | 0.245a | 1.009a | 0.065a |
| book_day7 | | | 1.052a | -0.175a | 0.555a | -0.225a |
| book_day10 | | | 0.952a | -0.047a | 0.491a | -0.147a |
| book_day14 | | | 0.184a | -0.540a | 0.170a | -0.282a |
| book_day21 | | | 0.003 | -0.370a | 0.101a | -0.129a |
| book_day28 | | | -0.074b | -0.257a | 0.051a | -0.059a |
| book_day35 | | | -0.070a | -0.159a | 0.038b | -0.014c |
| book_day42 | | | -0.048b | -0.099a | 0.042a | 0.012c |
| book_day49 | | | -0.113a | -0.156a | -0.003 | -0.026a |
| book_day56 | | | -0.130a | -0.161a | -0.033a | -0.050a |
| book_day63 | | | -0.079a | -0.105a | -0.020a | -0.035a |
| d_promo1 | | | | | -3.909a | -4.028a |
| Constant | 2.265a | 2.012a | 2.145a | 2.164a | 2.695a | 2.724a |
| R-2w | 0.14 | 0.05 | 0.28 | 0.07 | 0.7 | 0.62 |
| r2_o | 0.16 | 0.16 | 0.16 | 0.18 | 0.72 | 0.69 |

Full Sample & Market Structure

| | Monopoly | | Duo-Tri | opoly |
|------------|----------|---------|---------|---------|
| | xtiv1 | xtiv2 | xtiv3 | xtiv4 |
| inv_seat | 0.058a | 0.063a | 0.053a | 0.055a |
| d_promo1 | -4.099a | -4.066a | -3.865a | -3.841a |
| book_day1 | | 0 | | 0 |
| book_day4 | | 0.070a | | 0.045a |
| book_day7 | | -0.235a | | -0.165a |
| book_day10 | | -0.150a | | -0.121a |
| book_day14 | | -0.281a | | -0.276a |
| book_day21 | | -0.124a | | -0.150a |
| book_day28 | | -0.053a | | -0.087a |
| book_day35 | | -0.011 | | -0.027 |
| book_day42 | | 0.016c | | -0.005 |
| book_day49 | | -0.027a | | -0.024 |
| book_day56 | | -0.043a | | -0.079a |
| book_day63 | | -0.027a | | -0.072a |
| Constant | 2.710a | 2.738a | 2.597a | 2.648a |
| R-2w | 0.62 | 0.61 | 0.68 | 0.67 |
| r2_o | 0.69 | 0.69 | 0.72 | 0.71 |

Using a monopoly dummy

| | Cense | ored | Full Sa | ample |
|---------------|---------|---------|---------|---------|
| | xtiv1 | xtiv2 | xtiv3 | xtiv4 |
| inv_seat | 0.043a | 0.042a | 0.055a | 0.051a |
| inv_seat_mono | -0.003a | -0.004a | 0.008a | 0.007a |
| book_day1 | 0 | | 0 | |
| book_day4 | -0.233a | | 0.066a | |
| book_day7 | -0.384a | | -0.224a | |
| book_day10 | -0.349a | | -0.146a | |
| book_day14 | -0.379a | | -0.281a | |
| book_day21 | -0.259a | | -0.129a | |
| book_day28 | -0.162a | | -0.059a | |
| book_day35 | -0.085a | | -0.014c | |
| book_day42 | -0.026 | | 0.012c | |
| book_day49 | 0.022 | | -0.026a | |
| book_day56 | 0.056c | | -0.049a | |
| book_day63 | -0.011 | | -0.035a | |
| d_promo1 | -4.562a | -4.648a | -4.029a | -4.061a |
| Constant | 3.229a | 3.006a | 2.723a | 2.691a |
| R-2w | 0.71 | 0.67 | 0.62 | 0.63 |
| r2_o | 0.54 | 0.50 | 0.69 | 0.70 |